

CSE332 Week 2 Section Worksheet

1. Find values for c and n_0 (according to the definition of $O(\cdot)$) for $f(n)$ is $O(g(n))$, where

a.

$$f(n) = 7n^2 + 3n$$
$$g(n) = n^4$$

b.

$$f(n) = n + 2n \log n$$
$$g(n) = n \log n$$

c.

$$f(n) = 1000$$
$$g(n) = 3n^3$$

d.

$$f(n) = 7n$$
$$g(n) = n/10$$

2. True or false?

a. $f(n)$ is $\Theta(g(n))$ implies $f(n)$ is $O(g(n))$

b. $f(n)$ is $\Theta(g(n))$ implies $g(n)$ is $\Theta(f(n))$

c. $f(n)$ is $\Omega(g(n))$ implies $f(n)$ is $O(g(n))$

3. Find functions $f(n)$ and $g(n)$ such that $f(n)$ is $O(g(n))$ and the constant c for the definition of $O(\cdot)$ must be >1 . That is, find f & g such that c must be greater than 1, as there is no sufficient n_0 when $c=1$.

4. Write the $O(\cdot)$ run-time of the functions with the following recurrence relations

a. $T(n) = 3 + T(n-1)$, where $T(0) = 1$

b. $T(n) = 3 + T(n/2)$, where $T(1) = 1$

c. $T(n) = 3 + T(n-1) + T(n-1)$, where $T(0) = 1$

5. What's the $O(\cdot)$ run-time of this code fragment in terms of n :

```
int x=0;
for(int i=n; i>=0; i--)
    if((i%3)==0) break;
    else x+=i;
```