

# CSE 331

## Mutation of Heap State

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## 331 So Far...

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- Saw how to implement ADTs without mutation
- Introducing more mutation going forward
  - core idea is that mutation makes things harder
- Introduced local variable mutation last time
  - causes **some** difficulty for *implementers*  
need to reason line-by-line for any variable that is mutated
  - causes **no** difficulty for *clients*  
they literally cannot tell the difference

# When we mutate objects and arrays...

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- Objects and arrays are "**heap**" data
  - can still be in use after the call returns
- Mutation of heap data is different
  - clients can see that mutation occurred!
- So, we must also update **specifications**
  - need to explain any possible mutation that may happen
    - by default, nothing is being mutated
  - **higher likelihood of potential bugs**
    - miscommunication between programmers is a common cause
  - these will be harder to debug

# Plan for today

---

**Learn how to specify heap mutation for clients**

- 1. Mutation in simple functions** (revisit Topic 1)
- 2. Mutation in ADTs** (revisit Topic 3)

# Mutation of Arguments

# Recall: Writing Method Specifications in Java

---

- Every input falls in one of three cases:
  1. input is disallowed
  2. input is allowed and will return something
  3. input is allowed and will throw something
- Item 1 is the **precondition**
  - explained in `@param` and `@requires`
- Items 2-3 are the **postcondition**
  - explained in `@return` and `@throws`

# Writing Method Specifications in Java

---

- Every input falls in one of three cases:
  1. input is disallowed
  2. input is allowed and will return something
  3. input is allowed and will throw something
- The **postcondition** can also include **mutation**
  - client will see that something argument was changed
  - explained in **@modifies** and **@effects**

# Describing Mutation in Specifications

---

- List anything that may change in `@modifies`
  - anything not listed is assumed not modified
  - no `@modifies` means nothing is mutated
- Results of the mutation listed in `@effects`
  - promises about the state when the call returns
  - no `@effects` means any change is possible

```
// @modifies A
// @effects all entries of A set to zero
void clear(int[] A)
```

# Example 1

---

```
/**  
 * Changes the first instance of v in A to w  
 * @param A The list to look in. Must be non-null  
 * @param v The value to look for  
 * @param w The value to replace the first v with  
 * @modifies A  
 * @effects changes A[i] to w, where i is the  
 * smallest index with A[i] = v, and leaves  
 * A[j] unchanged for all j != i  
 * @throws NotFound if no such index i exists  
 */  
void changeFirst(List<Integer> A, int v, int w)
```

## Recall: Example 2

---

```
/**  
 * Returns the concatenation of two lists.  
 * @param A The first list. Must be non-null  
 * @param B The second list. Must be non-null  
 * @return A ++ B  
 */  
List<Integer> concat(  
    List<Integer> A, List<Integer> B)
```

How would we change this to mutate instead?

## Example 2

---

```
/**  
 * Returns the concatenation of two lists.  
 * @param A The first list. Must be non-null  
 * @param B The second list. Must be non-null  
 * @modifies A  
 * @effects A = A_0 ++ B  
 */  
void concat(List<Integer> A, List<Integer> B)
```

We are now using Floyd logic in the spec!

What about a version that modifies B instead?

Is there any scenario where *both* arguments are modified?

## Example 3

---

```
/**  
 * Returns the number of common elements in both  
 * A and B. Sorts A and B in the process.  
 * @param A The first list. Must be non-null  
 * @param B The second list. Must be non-null  
 *  
 *  
 *  
 *  
 */  
int commonElems(List<Integer> A, List<Integer> B)
```

How should we specify this?

## Example 3

---

```
/**  
 * Returns the number of common elements in both  
 * A and B. Sorts A and B in the process.  
 * @param A The first list. Must be non-null  
 * @param B The second list. Must be non-null  
 * @modifies A, B  
 * @effects A is sorted and B is sorted  
 * @returns the number of indexes i such that  
 *           A[i] also appears in B somewhere  
 */  
int commonElems(List<Integer> A, List<Integer> B)
```

# Recall: Comparing Specifications

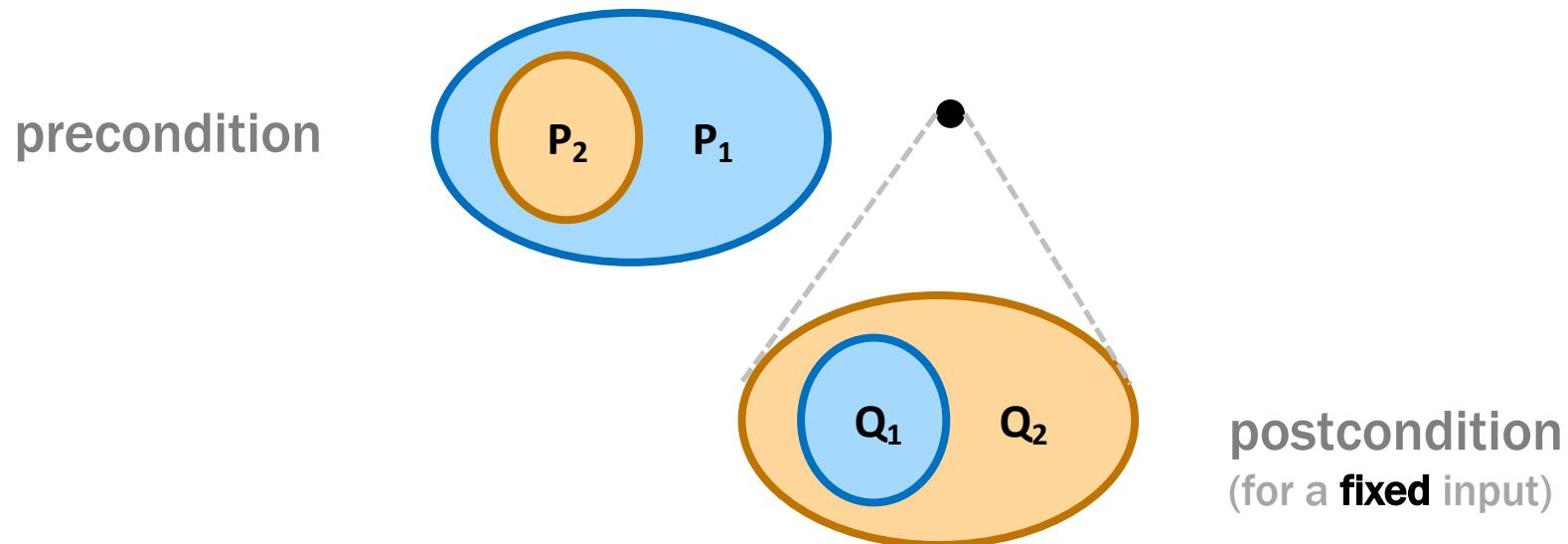
---

- Specification  $S_1$  is **stronger** than  $S_2$ ...
  - whenever  $S_1$  is satisfied,  $S_2$  is also satisfied
  - i.e., satisfying  $S_1$  implies satisfying  $S_2$
- Changing from  $S_2$  to  $S_1$  (**strengthening**)...
  - cannot break any clients!
  - client works with any implementation satisfying  $S_2$  and that includes anything satisfying  $S_1$
- But what does this mean...
  - in terms of **precondition** and **postcondition**

# Recall: Comparing Specifications

---

- Specification  $S_1$  is **stronger** than  $S_2$  if it has...
  - a **weaker** precondition and the same postcondition
  - a **stronger** postcondition and the same precondition
  - (or both)



# Comparing Specifications With Mutation

---

- Specification  $S_1$  is **stronger** than  $S_2$  if it has...
- A **stronger** postcondition:
  - adds more to `@returns`
  - adds more to `@effects`
  - removes from `@modifies`
    - promise is **not** to modify anything not listed
- A **weaker** precondition:
  - no change here

## Example 4

---

```
int commonElems(List<Integer> A, List<Integer> B)

// Specification S1
// @modifies A, B
// @effects A is sorted and B is sorted
// @returns the number of indexes i such that
//           A[i] also appears in B somewhere

// Specification S2
// @modifies A, B
// @effects
// @returns the number of indexes i such that
//           A[i] also appears in B somewhere
```

**How does  $S_1$  relate to  $S_2$ ?**

# Example 5

---

```
int commonElems(List<Integer> A, List<Integer> B)

// Specification S3
// @modifies A, B
// @effects A is sorted
// @returns the number of indexes i such that
//           A[i] also appears in B somewhere

// Specification S4
// @modifies A
// @effects A is sorted
// @returns the number of indexes i such that
//           A[i] also appears in B somewhere
```

**How does  $S_3$  relate to  $S_4$ ?**

# Example 5

---

```
int commonElems(List<Integer> A, List<Integer> B)

// Specification S1
// @modifies A, B
// @effects A is sorted and B is sorted
// @returns the number of indexes i such that
//           A[i] also appears in B somewhere

// Specification S4                                     How does S1 relate to S4?
// @modifies A
// @effects A is sorted
// @returns the number of indexes i such that
//           A[i] also appears in B somewhere
```

# Mutation in ADTs

# Recall: Mutable vs Immutable ADTs

---

	<u>Immutable</u>	<u>Mutable</u>
observers	✓	✓
mutators	✗	✓
producers	✓	✗ (usually not)

- **Sensible to pick one or the other**
  - would be dangerous to provide both  
will see why later on

# Recall: Specifying FastList

---

```
/**  
 * A list of integers that can retrieve the last  
 * element in O(1) time.  
 */  
interface FastList {  
  
    // Returns the last element of the list (O(1) time)  
    // @requires obj != nil  
observer // @return last(obj)  
    int getLast();  
  
observer // Returns the object as a regular list of items.  
    // @return obj  
    List getList();
```

# Recall: Specifying FastList

---

```
/**  
 * A list of integers that can retrieve the last  
 * element in O(1) time.  
 */  
interface FastList {  
    ...  
    /**  
     * Returns a new list with x in front of this list.  
producer     * @return x :: obj  
     */  
    FastList cons(int x);
```

- How do we make this a mutator?

# Specifying a Mutable FastList

---

```
/**  
 * A mutable list of integers that can retrieve the  
 * last element in O(1) time.  
 */  
interface MutableFastList {  
    ...  
    /**  
     * Adds x to the front of this list.  
     * @modifies obj  
     * @effects obj = x :: obj_0  
     */  
    void cons(int x);
```

- Changes obj to have x at the beginning

# Recall: Specifying Point

---

```
/** Represents an (x, y) point in 2D space. */
interface Point {

    /** @return x */
    double getX();

    /** @return y */
    double getY();
}
```

- Abstract state *is* a pair (x, y)
  - i.e., we have (x, y) := obj
  - so, we can refer to "x" and "y"

# Recall: Specifying Point

---

```
/** Represents an (x, y) point in 2D space. */
interface Point {

    /** @return (x^2 + y^2)^(1/2) */
    double getR();

    /** @return arctan(y/x) */
    double getTheta();
}
```

- **Imperative specifications**
  - code may or may not actually do these calculations
  - PolarPoint just returns the value in a field

# Recall: Specifying Point

---

```
/** Represents an (x, y) point in 2D space. */
interface Point {

    /** @return (x + dx, y + dy) */
    Point shiftBy(double dx, double dy);
```

- How do we make this a mutator?

# Specifying a Mutable Point

---

```
/** Represents a mutable (x, y) point in 2D space. */
interface MutablePoint {

    /**
     * Moves the point right by dx and up by dy
     * @modifies obj
     * @effects obj = (x_0 + dx, y_0 + dy)
     */
    void shiftBy(double dx, double dy);
}
```

# Recall: Immutable Queue

---

- A queue is a list that can *only* be changed two ways:
  - add elements to the front
  - remove elements from the back

```
// List that only supports adding to the front and
// removing from the end
interface NumberQueue {

    // @return len(obj)
    int size();

    // @return [x] ++ obj
    NumberQueue enqueue(int x);

    // @requires len(obj) > 0
    // @return (x, Q) with obj = Q ++ [x]
    DequeueParts dequeue();

}
```

Which method(s) change in a mutable version?

```
class DequeueParts {
    public final NumberQueue Q;
    public final int x;
}
```

# Mutable Queue

---

```
// @return [x] ++ obj
NumberQueue enqueue(int x);
```

- How do we make this mutable?

```
// @modifies obj
// @effects obj = [x] ++ obj_0
void enqueue(int x);
```

# Mutable Queue

---

```
// @requires len(obj) > 0
// @return (x, Q) with obj = Q ++ [x]
DequeueParts dequeue();
```

- How do we make this mutable?

```
// @modifies obj
// @effects obj_0 = obj ++ [x]
// @return x
int dequeue();
```

# Mutable Queue

---

- Note the symmetry between these operations:

```
// @modifies obj
// @effects obj = [x] ++ obj_0
void enqueue(int x);
```

```
// @modifies obj
// @effects obj_0 = obj ++ [x]
// @return x
int dequeue();
```

Which one of these is declarative?

# Converting Between Mutators and Producers

---

- We can transform between these in general
  - assume that "T" is our interface

```
// @return f(obj, x)  
T produce(int x);
```



1. change return type
2. change @return expression into @effects obj = expression

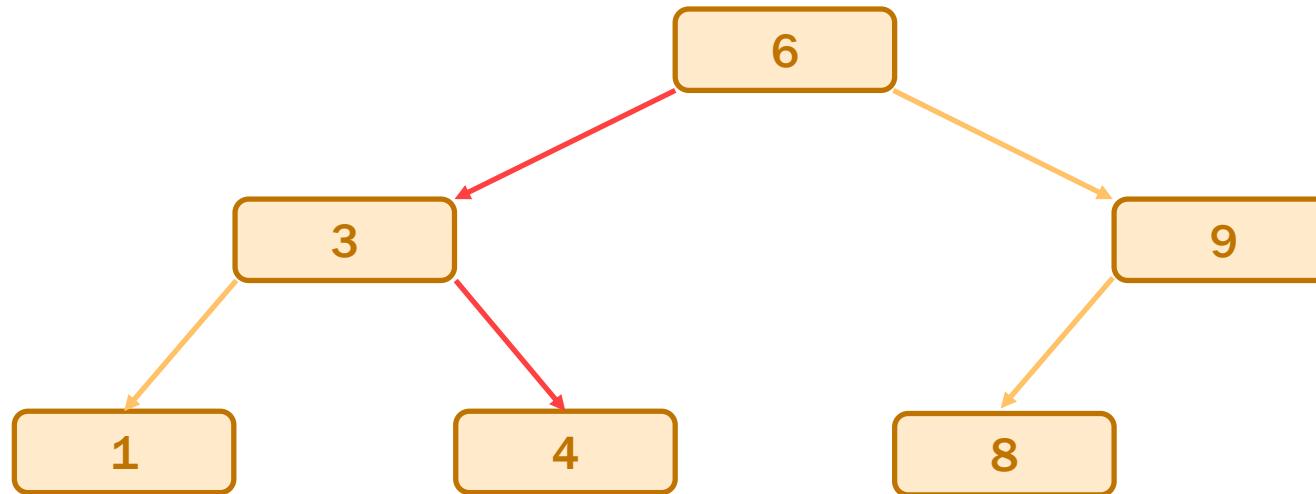
```
// @modifies obj  
// @effects obj = f(obj_0, x)  
void mutate(int x);
```

# Aliasing

# Recall: Binary Search Trees

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- Consider the following tree
  - searching for "4" proceeds as follows:

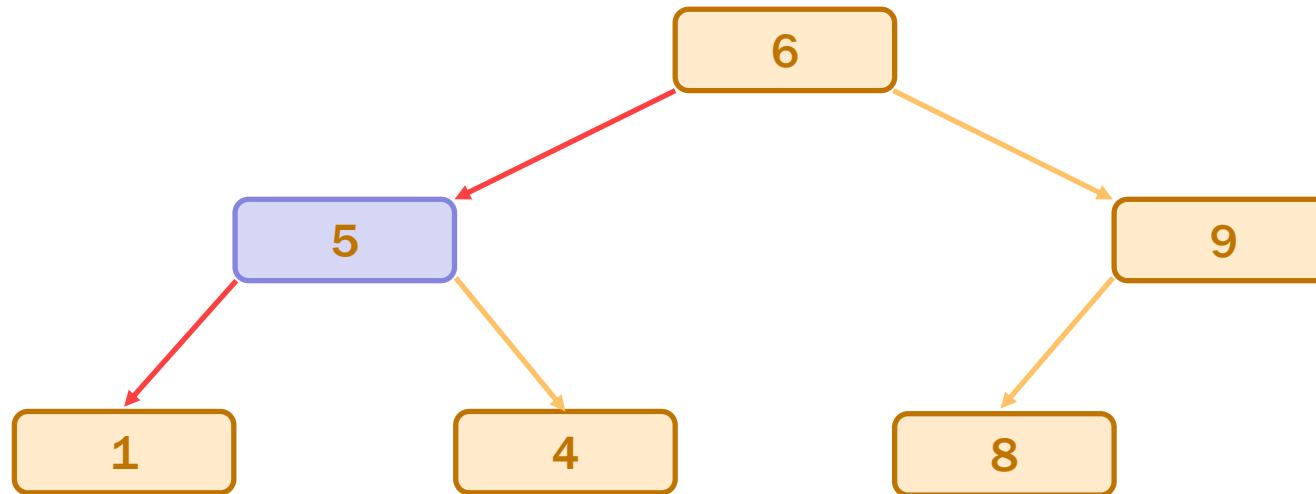


- Suppose someone changed "3" into "5"...

# Recall: Binary Search Trees

---

- Suppose someone changed "3" into "5"..."
  - now this happens when we search for "4":



- It can no longer be found!
  - Doesn't crash. It's just not found.
- Problem doesn't occur on the line with the change

# Scary Bugs

---

- **Do not fear crashes**
  - often no debugging at all
    - get a stack trace that tells you exactly where it went wrong
- **Do fear unexpected mutation**
  - failure will give you no clue what went wrong
    - will take a long time to realize the BST invariant was violated by mutation
  - bug could be almost anywhere in the code
    - anyone who mutates a `TreeNode` could have caused it
  - could take weeks to track it down

# Another Example

---

```
class Name {  
    private String first;  
    private String last;  
  
    public String toString() {  
        return first + " " + last;  
    }  
  
    public void capitalize() {  
        this.first = first.substring(0, 1).toUpperCase()  
            + first.substring(1);  
        this.second = second.substring(0, 1).t  
            + second.substring(1);  
    }  
}
```

Somewhere else...

Map<Name, Integer> M;



# Even Worse in C/C++

---

- C/C++ strings are **mutable**
  - commonly used as map keys
  - this sort of bug is still very common
- Java strings are immutable
  - was hugely controversial at the time
    - in retrospect, it was clearly a good idea
  - other mutable types can still be used as keys

# Aliases

---

- Extra references to an object are called "aliases"
  - possible for any reference type
- Aliases are fine when objects are *immutable*
  - we don't care if someone else reads the data
  - we only care if someone mutates it
- Aliases are scary when objects are mutable...
  - creates the potential for failures far from bugs
  - that means **painful** debugging

# Mutable Heap State

---

- “With great power, comes great responsibility”
  - Uncle Ben
- With aliases to mutable heap state:
  - gain efficiency in some cases
  - must keep track of every alias that could mutate that state
    - any alias, anywhere in the *entire* program could cause a bug
- EJ 17: minimize mutability in classes

# Easy Ways to Stay Safe

---

## 1. Do not mutate heap state

- don't need to think about aliasing at all
- any number of aliases is fine

## 2. Do not allow aliases...

- create the state in your constructor and don't share it

```
class MyClass {  
    // RI: vals is sorted  
    private String[] vals;  
  
    public MyClass() {  
        this.vals = new String[10]; // only reference  
        ...  
    }  
}
```

# Easy Ways to Stay Safe

---

- Not enough just to declare it "**private**"

```
class MyClass {  
    // RI: vals is sorted  
    private String[] vals;  
  
    ...  
  
    public String[] values() {  
        return this.vals;  
    };  
}
```

this is "representation exposure"  
we will treat it as a bug

- anyone can get an alias by calling `values()`
- "**private**" is a clue that aliases might be bad

# Easy Ways to Stay Safe

## 2. Do not allow aliases

**(a) do not hand out aliases yourself**

- return copies instead

# Easy Ways to Stay Safe

---

## 2. Do not allow aliases

- (b) make a copy of anything you want to keep
  - does not matter if the caller mutates the original

```
class MyClass {  
    // RI: vals is sorted  
    private String[] vals;  
  
    ...  
  
    // @requires A is sorted  
    public MyClass(String[] A) {  
        this.vals = A;                      // unsafe!  
        this.vals = Arrays.copyOf(A,           // make a copy  
                                 A.length);  
    };
```

# Easy Ways to Stay Safe

---

- 1. Do not use mutable state**
  - don't need to think about aliasing at all
  - any number of aliases is fine
- 2. Do not allow aliases to *mutable* state**
  - a) do not hand out aliases yourself
  - b) make a copy of anything you want to keep

ensures only one reference to the object (no aliases)

  - For 331, mutable aliasing across files is a bug!
    - gives other parts the ability to break your code
    - we will stick to these simple strategies for avoiding it

# An Advanced (Two-Stage) Approach

---

- **Mutable object has only one reference (owner)**
  - one reference that is allowed to use & mutate it
- **Object is eventually “frozen”, making it immutable**
  - no longer necessary to track ownership
- **Example: Java’s StringBuilder vs String**
  - StringBuilder **is mutable (be careful!)**
  - StringBuilder.toString **returns the value as a String**
  - String **is immutable**

# Rules of Thumb

---

## Client Side

- 1. Data is small**
  - anything on screen is  $O(1)$
- 2. Aliasing is common**
  - UI design forces modules
  - data is widely shared

### **Rule:** avoid mutation

- create new values instead
- performance will be fine

## Server Side

- 1. Data is large**
  - efficiency matters
- 2. Aliasing is avoidable**
  - you decide on modules
  - data is not widely shared

### **Rule:** avoid aliases

- do not allow aliases to your data
- hand out copies not aliases
- (good enough for us in 331)

# Using List

---

- Same issue arises with List as with arrays

```
class MyClass {  
    // RI: vals is sorted  
    private List<String> vals;  
  
    public List<String> values() {  
        return this.vals; // unsafe  
    };
```

- since a List is mutable, we cannot create aliases

# Another Alternative

---

- With List, a third option is sometimes used:

```
class MyClass {  
    // RI: vals is sorted  
    private List<String> vals;  
  
    public List<String> values() {  
        return Collections.unmodifiableList(this.vals);  
    };
```

- throws an exception when mutators are called
- runs in  $O(1)$  time instead of  $O(n)$  to copy

Can this change break the client?

# Another Alternative

---

- **This can break clients**
  - this works with a copy

```
MyClass m = ...;  
List<String> list = m.values()  
list.add("another");
```

- but not with `UnmodifiableList`
- **Specification must make clear the behavior**
  - how do the two options relate?

# Another Alternative

---

- **These two are incomparable**
  - they have differing behavior
  - client can work with one but not the other and v.v.
- **How is this possible when both return List?**
  - the unmodifiable list does not implement List!
    - the spec doesn't let you throw on any call to add
  - **this is a terrible idea**
    - but occasionally necessary in extreme circumstances
- **Really these are different return types**
  - would be better to make then different interfaces

# Unmodifiable View

---

- **Unmodifiable list is a "view" of the underlying list**
- **It changes whenever the underlying list changes**
  - updates to that list show up in the view immediately
  - it is not a copy of the data at that point
- **This can lead to difficult bugs**
  - do not use such a view as a key in a map
  - any alias to it can mutate it at any point

# Unmodifiable View

---

- Why would someone do this?
- Like most CS bugs, it is for performance
  - we all know that  $O(1)$  is better than  $O(n)$
- But most client uses are  $O(n)$  anyway!
  - client probably wants to loop through the list
  - in that case, there is no  $O(..)$  gain to
- We will stick to immutable or copying (no aliases)

# Module Design

# Module Design

---

**"Designing modules is the heart of software design."**

— Michael Ernst

- In Java, a "module" is a file or a top-level class
- Module design is an enormous subject
  - can look for many properties such as decomposability, compositability, understandability, continuity, isolation
- We will keep things simpler...

# Module Design

---

- Modules should have
  - high **cohesion**
  - low **coupling**
- **Cohesion:** the parts go together
  - they all serve one purpose or represent one concept
  - examples: an ADT, `java.util.Arrays`
  - non-example: one class for sorting, drawing, & printing
  - primarily about the **specification**

# Module Design

---

- **Modules should have**
  - high **cohesion**
  - low **coupling**
- **Coupling**: the parts only understandable together
  - must learn both to understand either
  - example: an immutable ADT
  - non-example: a mutable ADT that allows aliases
    - must understand how all aliases are used to know if it's correct
  - primarily about the **implementation**
  - will see another non-example next time..

# Coupling Is Bad

---

- Coupling makes the code less **understandable**
  - truth for both humans and AI
  - highly coupling becomes "spaghetti code"
  - often shows up as a "god class"
- Coupling makes the code hard to **change**
  - all the interrelated parts may require changes
- Coupling creates potential for **painful** debugging
  - bugs in one piece can cause failures in another
  - e.g., any misuse of an alias can break use by any other alias

# Subclasses

# Subclasses

---

- **Subclassing is a means of sharing code**
  - subclass gets parent fields & methods (unless overridden)

```
class Product {  
    private String name;  
    private int price;  
    public String getName() { return name; }  
    public int getPrice() { return price; }  
}  
  
class SaleProduct extends Product {  
    private float discount;  
    public int getPrice() {  
        return (1 - discount) * super.getPrice();  
    }  
}
```

# Subclasses

---

- Subclassing is a surprisingly dangerous feature
- Subclassing tends to break modularity
  - creates **tight coupling** between super- and sub-class
  - often see the “fragile base class” problem
    - changes to super class often break subclasses
- Let's see some examples...

# Example 1: Tight Coupling

---

```
class Product {  
    private int price;  
    public int getPrice() { return price; }  
  
    // @returns true iff obj's price < p's price  
    public boolean isCheaperThan(Product p) {  
        return getPrice() < p.getPrice();  
    }  
}  
  
class SaleProduct extends Product {  
    public int getPrice() {  
        return (1 - discount) * super.getPrice();  
    }  
}
```

- looks okay so far...

# Example 1: Tight Coupling

---

```
class Product {  
    private int price;  
    public int getPrice() { return price; }  
  
    // @returns true iff obj's price < p's price  
    public boolean isCheaperThan(Product p) {  
        return this.price < p.price;  
    }  
}
```

Made it faster by eliminating a method call!

```
class SaleProduct extends Product {  
    public int getPrice() {  
        return (1 - discount) * super.getPrice();  
    }  
}
```

What's wrong?

Oops! Broke the subclass

## Example 2: Tight Coupling

---

```
class InstrumentedHashSet extends HashSet<Integer> {  
    private static int count = 0;  
  
    public boolean add(Integer e) {  
        count += 1;  
        return super.add(e);  
    }  
  
    public boolean addAll(Collection<Integer> c) {  
        count += c.size();  
        return super.addAll(c);  
    }  
  
    public int getCount() { return count; }  
}
```

- what could possibly go wrong?

## Example 2: Tight Coupling

---

```
InstrumentedHashSet S = new InstrumentedHashSet();  
System.out.println(S.getCount()); // 0  
S.addAll(Arrays.asList(1, 2));  
System.out.println(S.getCount()); // 4?!?
```

- what does this print?
- What is printed depends on HashSet's addAll:
  - if it calls add, then this prints 4
  - if it does not call add, then this prints 2
- Also possible to be dependent on *order* of calls

# Subclassing Creates Tight Coupling

---

- Creates tight coupling between super- and sub-class
- Example 1: super-class needs to know about subclass
  - direct field access in parent breaks subclass
- Example 2: subclass needs to know about super-class
  - subclass dependent on which methods call each other
- But wait... There's more!

# Example 3: Tight Coupling

---

```
class WorkList {  
    // RI: len(names) = len(times) and total = sum(times)  
    protected ArrayList<String> names;  
    protected ArrayList<Integer> times;  
    protected int total;  
  
    public addWork(Job job) {  
        addToLists(job.getName(), job.getTime());  
        total += job.getTime();  
    }  
  
    protected addToLists(String name, int time) {  
        names.add(name);  
        times.add(time);  
    }  
}
```

## Example 3: Tight Coupling

---

```
// Makes sure no task is too large compared to rest
class BalancedWorkList extends WorkList {
    protected addToLists(String name, int time) {
        if (times.size() <= 3 || 2*time < total)
            super.addToLists(name, time); // okay
    } else {
        throw new ImbalancedWorkException(name, time);
    }
}
```

- prevents item from being added if too big
- (also: this subclass is not a subtype!)

# Example 3: Tight Coupling

---

```
class WorkList {  
    // RI: len(names) = len(times) and total = sum(times)  
    protected ArrayList<String> names;  
    protected ArrayList<Integer> times;  
    protected int total;  
  
    public addWork(Job job) {  
        int time = job.getTime(); // just one call  
        total += time;  
        addToLists(job.getName(), time);  
    }  
}  
RI not true in method call
```

- **reordering the updates breaks the subclass!**
- **subclass is using `total` that includes the new job**

## Example 3: Tight Coupling

---

- RI can be false in calls to non-public methods
  - only needs to hold at end of the public method
- Requires extra care to get it right
  - method is tightly coupled with the ones that call it
  - needs to know what is true in those methods
    - not enough to just know the RI
- Hard for multiple people to communicate this clearly
  - can be okay when it's all your code
  - very error prone when methods are written by others

# Subclassing Creates Tight Coupling

---

- Creates tight coupling between super- and sub-class
  - direct field access can break subclass
  - subclass dependent on which methods call each other
  - subclass dependent on *order* of method calls
  - subclass can be called when RI is false
- Often see the “**fragile base class**” problem
- Subclassing is a surprisingly dangerous feature!
  - up to you to verify subclass method specs are stronger
  - up to you to prevent tight coupling

# Subclassing is Best Avoided

---

- **EJ 19**: either design for subclassing or prohibit it
  - from Josh Bloch, author of (much of) the Java libraries
- We haven't used subclassing in our ADTs
  - we used interfaces and implemented them with classes
  - these problems are the main reason why we avoided it
- Subclassing is not necessary anyway
  - we have other ways to share code
  - **EJ 18**: prefer composition to inheritance

# Equality

# Equity of User-Defined Types

---

- For any type, useful to know which are “the same”
- Java “==” is not useful on records:

```
new Integer(1) == new Integer(1) // false!
```

- this is “reference equality”
- tells you if they refer to the same object in memory
- Checking if the fields are the same is also wrong
  - different concrete states can have same abstract state

# Storing a List In Two Parts

---

```
// Stores a list, split in two parts.  
class ListPair implements List {  
  
    // AF: obj = this.front ++ this.back  
    private List front;  
    private List back;
```

- three ways of representing the same abstract state:

front	back	front + back
[1, 2]	[]	[1, 2]
[1]	[2]	[1, 2]
[]	[1, 2]	[1, 2]

- same abstract states should be considered equal!

# Recall: HW3

---

```
/**  
 * Represents an immutable collection of integers.  
 *  
 * Clients can think of a set as a list of integers. However, they can only ask  
 * if an integer is present or not. The order of the integers does not matter.  
 * The number of times that an integer appears in the list does not matter.  
 */  
public interface IntSet {  
    /**  
     * Determines whether n is in the list.  
     * @param n the number to look for in the list  
     * @returns contains(n, obj), where  
     *          contains(n, nil)    := false  
     *          contains(n, m :: L) := true          if m = n  
     *          contains(n, m :: L) := contains(n, L) if m /= n  
     */  
    public boolean contains(int n);  
  
    /**  
     * Creates and returns a new list containing n as well as all of obj.  
     * @param n the number to add to the new list.  
     * @returns n :: obj  
     */  
    public IntSet add(int n);
```

The abstract state allows duplicates,  
but clients can't tell.

# Equality on Sets

---

- Suppose our concrete representation is:

```
// RI: this.list has no duplicates
// AF: obj = this.list
private List list;
```

- Method `add` returns a different list than the spec
  - spec says `add(1)` on `[1]` returns `[1, 1]`
  - if the code add a second 1, abstract state is still `[1]`
- Need "equal" that says these states are "the same"
  - two abstract states are equal if they contain the same values

$\text{equal}(L, R) := \text{true} \text{ iff } \text{contains}(x, L) = \text{contains}(x, R) \text{ for any } x$

# Equality

---

- Often useful / necessary to define your own `equal`
  - check if references point to records that are “the same”
- Sensible definition should act like “=” in math:
  1.  $\text{equal}(a, a) = \text{T}$  for any  $a : A$  reflexive
  2.  $\text{equal}(a, b) = \text{equal}(b, a)$  for any  $a, b : A$  symmetric
  3. if  $\text{equal}(a, b)$  and  $\text{equal}(b, c)$ , then  $\text{equal}(a, c)$  for any ... transitive
  - (311 alert: this is an “equivalence relation”)
  - Java has two more rules for `Object.equals`

# Java Equals

---

- Java requires the following parts:

1. `a.equals(a) = true`
2. `a.equals(b) == b.equals(a)`
3. `a.equals(b)` and `b.equals(c)` means `a.equals(c)`
4. `a.equals(null) = false` asymmetric with null
5. `a.equals(b)` cannot change value  
unless `a` or `b` is mutated consistency

# Equals in Java

---

- Every class inherits an `equals` method
  - this implements reference equality

```
public class Object {  
    public boolean equals(Object o) {  
        return this == o;  
    }  
}
```

- Make your own `equals` by overriding it:

```
public class MyClass {  
    public boolean equals(Object o) {  
        // ... new code here ...  
    }  
}
```

# Example: Duration

---

- Define Duration to be an amount of time in seconds
  - one representation stores separate minutes and seconds

`type Duration = {min :  $\mathbb{Z}$ , sec :  $\mathbb{Z}$ }` with  $0 \leq \text{sec} < 60$

- second part is a **rep invariant**
- Can define equality on Duration this way:

`equal({min: m, sec: s}, {min: n, sec: t}) := (m = n) and (s = t)`

- true iff these are the same amount of time  
(wouldn't be true without the invariant)

# Example: Duration

---

$\text{equal}(\{\text{min: } m, \text{sec: } s\}, \{\text{min: } n, \text{sec: } t\}) := (m = n) \text{ and } (s = t)$

- Does this have the required properties?

- reflexive

$\text{equal}(\{\text{min: } m, \text{sec: } s\}, \{\text{min: } m, \text{sec: } s\})$

$= (m = m) \text{ and } (s = s)$

**def of equal**

$= T \text{ and } T$

$= T$

proof by calculation  
that it holds for any record

- symmetric

$\text{equal}(\{\text{min: } m, \text{sec: } s\}, \{\text{min: } n, \text{sec: } t\})$

$= (m = n) \text{ and } (s = t)$

**def of equal**

$= (n = m) \text{ and } (t = s)$

$= \text{equal}(\{\text{min: } n, \text{sec: } t\}, \{\text{min: } m, \text{sec: } s\})$

**def of equal**

# Example: Duration

---

`equal({min: m, sec: s}, {min: n, sec: t}) := (m = n) and (s = t)`

- Does this have the required properties?
  - reflexive yes
  - symmetric yes
  - transitive also yes (but a little long for a slide)
- Good evidence that this is a reasonable definition

# Non-Example: “==” in JavaScript

---

```
0 == "0"      true
0 == ""       true
0 == " "      true
```

- Which property fails?
  - **transitivity**: “” != “ ”
- Good evidence that this is not a reasonable definition

# Example: Duration in Java

---

```
// Represents an amount of time measured in seconds
class Duration {

    // RI: 0 <= sec < 60
    // AF: obj = 60 * this.min + this.sec
    private int min;
    private int sec;

    public boolean equals(Duration d) {
        return this.min == d.min && this.sec == d.sec;
    }
}
```

- **What is wrong with this?**
  - it doesn't **override** equals (Object)

# Example: Duration in Java

---

```
// Represents an amount of time measured in seconds
class Duration {

    // RI: 0 <= sec < 60
    // AF: obj = 60 * this.min + this.sec
    private int min;
    private int sec;

    public boolean equals(Object o) {
        return this.min == o.min && this.sec == o.sec;
    };
}
```

- What is wrong with this?
  - it doesn't compile

# Example: Duration in Java

---

```
// Represents an amount of time measured in seconds
class Duration {

    // RI: 0 <= sec < 60
    // AF: obj = 60 * this.min + this.sec
    private int min;
    private int sec;

    public boolean equals(Object o) {
        if (!(o instanceof Duration))
            return false;

        Duration d = (Duration) o;
        return this.min == d.min && this.sec == d.sec;
    }
}
```

- Correct and idiomatic Java

# Example: NanoDuration

---

- Suppose a subclass also measures nanoseconds

```
class NanoDuration extends Duration {  
  
    // min: number (inherited)  
    // sec: number (inherited)  
    private int nano;  
  
    ...
```

- How should we define `equal`?

# Example: NanoDuration

---

```
class NanoDuration extends Duration {  
  
    // min: number (inherited)  
    // sec: number (inherited)  
    private int nano;  
  
    public boolean equals(Object o) {  
        if (!(o instanceof NanoDuration)) {  
            return false;  
  
        NanoDuration n = (NanoDuration) o;  
        return this.min === n.min &&  
               this.sec === n.sec &&  
               this.nano === n.nano;  
    }  
}
```

symmetry

- Which property does this lack?

# Example: NanoDuration

---

```
Duration d = new Duration(2, 10);
NanoDuration n = new NanoDuration(2, 10, 300);

System.out.println(n.equals(d)); // false
System.out.println(d.equals(n)); // true!
```

- NanoDuration **is only equal to other** NanoDuration**s**
- Duration **can be equal to a** NanoDuration  
if they have the same minutes and seconds

# Example: NanoDuration

---

```
class NanoDuration extends Duration {  
  
    public boolean equals(Object o) {  
        if (!(o instanceof Duration))  
            return false;  
  
        if (!(o instanceof NanoDuration)) {  
            Duration d = (Duration) o;  
            return this.min == d.min && this.sec == d.sec;  
        } else {  
            NanoDuration n = (NanoDuration) o;  
            return this.min == d.min &&  
                this.sec == d.sec && this.nano == d.nano;  
        }  
    };
```

- Fixes symmetry! all good now?

No! It lacks transitivity

# Example: NanoDuration

---

```
NanoDuration n1 = new NanoDuration(2, 10, 300);  
Duration d = new Duration(2, 10);  
NanoDuration n2 = new NanoDuration(2, 10, 400);  
  
System.out.println(n1.equals(d)); // true  
System.out.println(d.equals(n2)); // true  
System.out.println(n1.equals(n2)); // false!
```

- transitivity requires n1 to equal n2 (but it doesn't)

# Example: NanoDuration

---

- Can fix this instead as follows:
  - have both agree that Duration  $\neq$  NanoDuration

```
class Duration {  
    ...  
    public boolean equals(Object o) {  
        if (!(o instanceof Duration) ||  
            (o instanceof NanoDuration))  
            return false;  
  
        Duration d = (Duration) o;  
        return this.min == d.min && this.sec == d.sec;  
    }  
}
```

- This is arguably the most sensible answer...

# Example: NanoDuration

---

- Should have spelled out the abstract states:

```
// Represents an amount of time in nanoseconds
class NanoDuration extends Duration {

    // RI: 0 <= sec < 60 and 0 <= nano < 10000
    // AF: obj = 60,000,000 * this.min +
    //           1,000,000 * this.sec +
    //           this.nano
    private int nano;

}
```

- Abstract states of the two types are **different**
  - time in seconds vs nanoseconds
  - two different types of things should not be equal

# Duration and NanoDuration

---

- We fixed it... but at what cost?
- Duration **and** NanoDuration **are tightly coupled**
  - the two classes are tightly intertwined
- This **usually happens with subclasses**
  - saw several different ways they are interdependent
  - very hard to avoid coupling between subclasses
    - EJ 19: either design for subclassing or prohibit it
  - **better to simply not use it**
    - find other ways to share code (e.g., shared utility functions etc.)

# HashCode in Java

---

- Java has another method called hashCode

```
public int hashCode();
```

- Should override hashCode and equals together
  - almost certainly a bug to only override equals

# Java `HashCode`

---

- Java has another method called `hashCode`
  - provided to make `HashMap` etc. work

```
public int hashCode();
```

- Its spec has the following requirements:
  1. `a.hashCode()` cannot change value unless `a` is mutated
    - self-consistency
  2. `a.equals(b)` means `a.hashCode() == b.hashCode()`
    - consistent with `equals`
    - when `equals` changes, so does `hashCode`

# Equals & hashCode in Java

---

- Every class inherits a hashCode method

```
public class Object {  
    public int hashCode() {  
        // ... consistent with reference equality ...  
    }  
}
```

- When you override equals, also override hashCode
  - almost certainly a bug to only override equals

```
public class MyClass {  
    public int hashCode() {  
        // ... something consistent with new equality ...  
    }  
}
```