



CSE 331

Mutation of Heap State

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331 So Far...

- Saw how to implement ADTs without mutation
- Introducing more mutation going forward
 - core idea is that mutation makes things harder
- Introduced **local variable** mutation last time
 - causes **some** difficulty for *implementers*
 - need to reason line-by-line for any variable that is mutated
 - causes **no** difficulty for *clients*
 - they literally cannot tell the difference

When we mutate objects and arrays...

- Objects and arrays are "heap" data
 - can still be in use after the call returns
- Mutation of heap data is different
 - clients can see that mutation occurred!
- So, we must also update specifications
 - need to explain any possible mutation that may happen
 - by default, nothing is being mutated
 - higher likelihood of potential bugs
 - miscommunication between programmers is a common cause
 - these will be harder to debug

Plan for today

Learn how to specify heap mutation for clients

1. Mutation in simple functions (revisit Topic 1)
2. Mutation in ADTs (revisit Topic 3)

Mutation of Arguments

Recall: Writing Method Specifications in Java

- Every input falls in one of three cases:
 1. input is disallowed
 2. input is allowed and will return something
 3. input is allowed and will throw something
- Item 1 is the **precondition**
 - explained in **@param** and **@requires**
- Items 2-3 are the **postcondition**
 - explained in **@return** and **@throws**

Writing Method Specifications in Java

- Every input falls in one of three cases:
 1. input is disallowed
 2. input is allowed and will return something
 3. input is allowed and will throw something
- The **postcondition** can also include **mutation**
 - client will see that something argument was changed
 - explained in **@modifies** and **@effects**

Describing Mutation in Specifications

- List anything that may change in `@modifies`
 - anything not listed is assumed not modified
 - no `@modifies` means nothing is mutated
- Results of the mutation listed in `@effects`
 - promises about the state when the call returns
 - no `@effects` means any change is possible

```
// @modifies A
// @effects all entries of A set to zero
void clear(int[] A)
```


Example 1

```
/**
 * Changes the first instance of v in A to w
 * @param A The list to look in. Must be non-null
 * @param v The value to look for
 * @param w The value to replace the first v with
 * @modifies A
 * @effects changes A[i] to w, where i is the
 *           smallest index with A[i] = v, and leaves
 *           A[j] unchanged for all j != i
 * @throws NotFound if no such index i exists
 */
void changeFirst(List<Integer> A, int v, int w)
```

Recall: Example 2

```
/**
 * Returns the concatenation of two lists.
 * @param A The first list. Must be non-null
 * @param B The second list. Must be non-null
 * @return A ++ B
 */
List<Integer> concat(
    List<Integer> A, List<Integer> B)
```

How would we change this to mutate instead?

Example 2

```
/**
 * Returns the concatenation of two lists.
 * @param A The first list. Must be non-null
 * @param B The second list. Must be non-null
 * @modifies A
 * @effects A = A_0 ++ B
 */
void concat(List<Integer> A, List<Integer> B)
```

We are now using Floyd logic in the spec!

What about a version that modifies B instead?

Is there any scenario where *both* arguments are modified?

Example 3

```
/**
 * Returns the number of common elements in both
 * A and B. Sorts A and B in the process.
 * @param A The first list. Must be non-null
 * @param B The second list. Must be non-null
 *
 *
 *
 *
 */
int commonElems (List<Integer> A, List<Integer> B)
```

How should we specify this?

Example 3

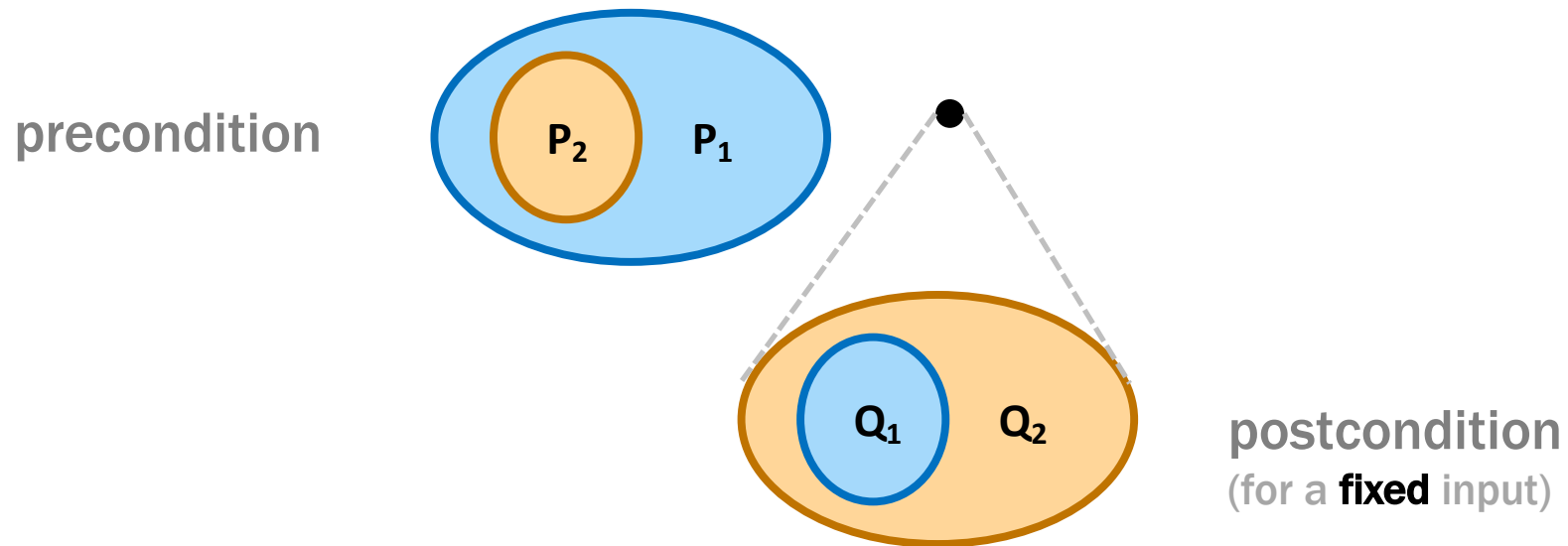
```
/**
 * Returns the number of common elements in both
 * A and B. Sorts A and B in the process.
 * @param A The first list. Must be non-null
 * @param B The second list. Must be non-null
 * @modifies A, B
 * @effects A is sorted and B is sorted
 * @returns the number of indexes i such that
 *           A[i] also appears in B somewhere
 */
int commonElements (List<Integer> A, List<Integer> B)
```

Recall: Comparing Specifications

- Specification S_1 is **stronger** than S_2 ...
 - whenever S_1 is satisfied, S_2 is also satisfied
 - i.e., satisfying S_1 implies satisfying S_2
- Changing from S_2 to S_1 (**strengthening**)...
 - cannot break any clients!
 - client works with any implementation satisfying S_2 and that includes anything satisfying S_1
- But what does this mean...
 - in terms of **precondition** and **postcondition**

Recall: Comparing Specifications

- Specification S_1 is **stronger** than S_2 if it has...
 - a **weaker** precondition and the same postcondition
 - a **stronger** postcondition and the same precondition
 - (or both)



Comparing Specifications With Mutation

- Specification S_1 is **stronger** than S_2 if it has...
- A **stronger** postcondition:
 - adds more to **@returns**
 - adds more to **@effects**
 - removes from **@modifies**
promise is **not** to modify anything not listed
- A **weaker** precondition:
 - no change here

Example 4

```
int commonElems (List<Integer> A, List<Integer> B)
```

```
// Specification S1
```

```
// @modifies A, B
```

```
// @effects A is sorted and B is sorted
```

```
// @returns the number of indexes i such that
```

```
//      A[i] also appears in B somewhere
```

```
// Specification S2
```

```
// @modifies A, B
```

```
// @effects
```

```
// @returns the number of indexes i such that
```

```
//      A[i] also appears in B somewhere
```

How does S_1 relate to S_2 ?

Example 5

```
int commonElems (List<Integer> A, List<Integer> B)
```

```
// Specification S3
```

```
// @modifies A, B
```

```
// @effects A is sorted
```

```
// @returns the number of indexes i such that
```

```
//      A[i] also appears in B somewhere
```

```
// Specification S4
```

How does S_3 relate to S_4 ?

```
// @modifies A
```

```
// @effects A is sorted
```

```
// @returns the number of indexes i such that
```

```
//      A[i] also appears in B somewhere
```

Example 5

```
int commonElems (List<Integer> A, List<Integer> B)
```

```
// Specification S1
```

```
// @modifies A, B
```

```
// @effects A is sorted and B is sorted
```

```
// @returns the number of indexes i such that
```

```
//      A[i] also appears in B somewhere
```

```
// Specification S4
```

How does S_1 relate to S_4 ?

```
// @modifies A
```

```
// @effects A is sorted
```

```
// @returns the number of indexes i such that
```

```
//      A[i] also appears in B somewhere
```

Mutation in ADTs

Recall: Mutable vs Immutable ADTs

	<u>Immutable</u>	<u>Mutable</u>
observers	✓	✓
mutators	✗	✓
producers	✓	✗ (usually not)

- **Sensible to pick one or the other**
 - would be dangerous to provide both
 - will see why later on

Recall: Specifying FastList

```
/**
 * A list of integers that can retrieve the last
 * element in O(1) time.
 */
interface FastList {

    // Returns the last element of the list (O(1) time)
    // @requires obj != nil
observer // @return last(obj)
    int getLast();

    // Returns the object as a regular list of items.
    // @return obj
observer //
    List getList();
```

Recall: Specifying FastList

```
/**
 * A list of integers that can retrieve the last
 * element in O(1) time.
 */
interface FastList {
  ...
  /**
   * Returns a new list with x in front of this list.
producer  * @return x :: obj
   */
  FastList cons(int x);
}
```

- How do we make this a mutator?

Specifying a Mutable FastList

```
/**
 * A mutable list of integers that can retrieve the
 * last element in O(1) time.
 */
interface MutableFastList {
    ...
    /**
     * Adds x to the front of this list.
     * @modifies obj
     * @effects obj = x :: obj_0
     */
    void cons(int x);
```

- Changes obj to have x at the beginning

Recall: Specifying Point

```
/** Represents an (x, y) point in 2D space. */  
interface Point {  
  
    /** @return x */  
    double getX();  
  
    /** @return y */  
    double getY();  
}
```

- Abstract state *is* a pair (x, y)
 - i.e., we have $(x, y) := \text{obj}$
 - so, we can refer to "x" and "y"

Recall: Specifying Point

```
/** Represents an (x, y) point in 2D space. */  
interface Point {  
  
    /** @return  $(x^2 + y^2)^{1/2}$  */  
    double getR();  
  
    /** @return  $\arctan(y/x)$  */  
    double getTheta();  
}
```

- Imperative specifications
 - code may or may not actually do these calculations
 - `PolarPoint` just returns the value in a field

Recall: Specifying Point

```
/** Represents an (x, y) point in 2D space. */  
interface Point {  
  
    /** @return (x + dx, y + dy) */  
    Point shiftBy(double dx, double dy);  
}
```

- How do we make this a mutator?

Specifying a Mutable Point

```
/** Represents a mutable (x, y) point in 2D space. */
interface MutablePoint {

    /**
     * Moves the point right by dx and up by dy
     * @modifies obj
     * @effects obj = (x_0 + dx, y_0 + dy)
     */
    void shiftBy(double dx, double dy);
}
```

Recall: Immutable Queue

- A queue is a list that can *only* be changed two ways:
 - add elements to the front
 - remove elements from the back

```
// List that only supports adding to the front and  
// removing from the end
```

```
interface NumberQueue {
```

```
    // @return len(obj)
```

```
    int size();
```

```
    // @return [x] ++ obj
```

```
    NumberQueue enqueue(int x);
```

```
    // @requires len(obj) > 0
```

```
    // @return (x, Q) with obj = Q ++ [x]
```

```
    DequeueParts dequeue();
```

```
}
```

Which method(s) change
in a mutable version?

```
class DequeueParts {  
    public final NumberQueue Q;  
    public final int x;  
}
```

Mutable Queue

```
// @return [x] ++ obj  
NumberQueue enqueue (int x);
```

- How do we make this mutable?

```
// @modifies obj  
// @effects obj = [x] ++ obj_0  
void enqueue (int x);
```

Mutable Queue

```
// @requires len(obj) > 0
// @return (x, Q) with obj = Q ++ [x]
DequeParts dequeue();
```

- How do we make this mutable?

```
// @modifies obj
// @effects obj_0 = obj ++ [x]
// @return x
int dequeue();
```

Mutable Queue

- Note the symmetry between these operations:

```
// @modifies obj
// @effects obj = [x] ++ obj_0
void enqueue(int x);
```

```
// @modifies obj
// @effects obj_0 = obj ++ [x]
// @return x
int dequeue();
```

Which one of these is declarative?

Converting Between Mutators and Producers

- We can transform between these in general
 - assume that "T" is our interface

```
// @return f(obj, x)
T produce(int x);
```



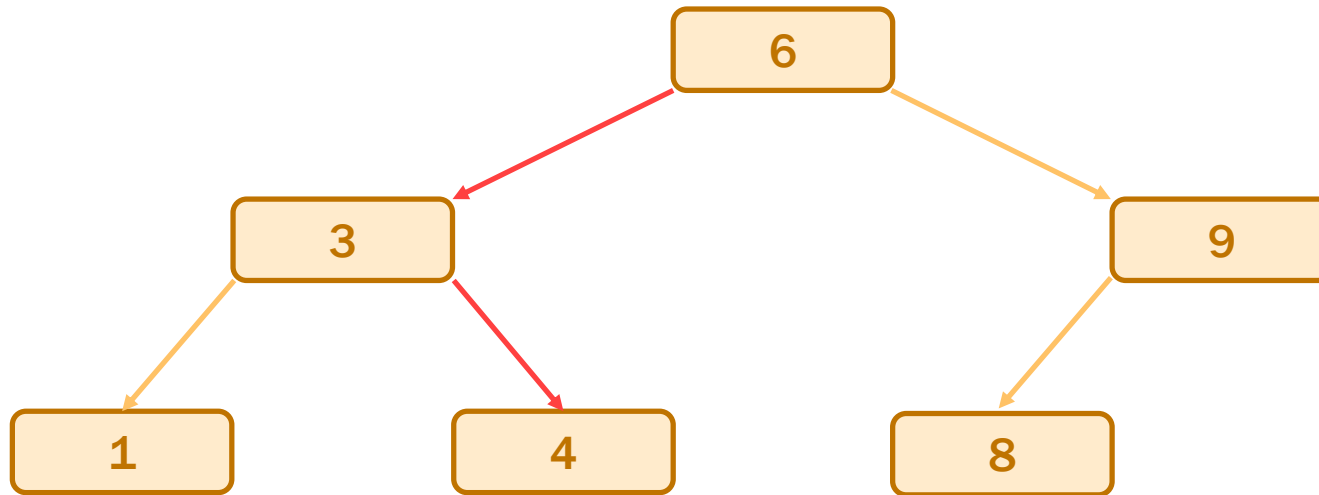
```
// @modifies obj
// @effects obj = f(obj_0, x)
void mutate(int x);
```

1. change return type
2. change @return expression into @effects obj = expression

Aliasing

Recall: Binary Search Trees

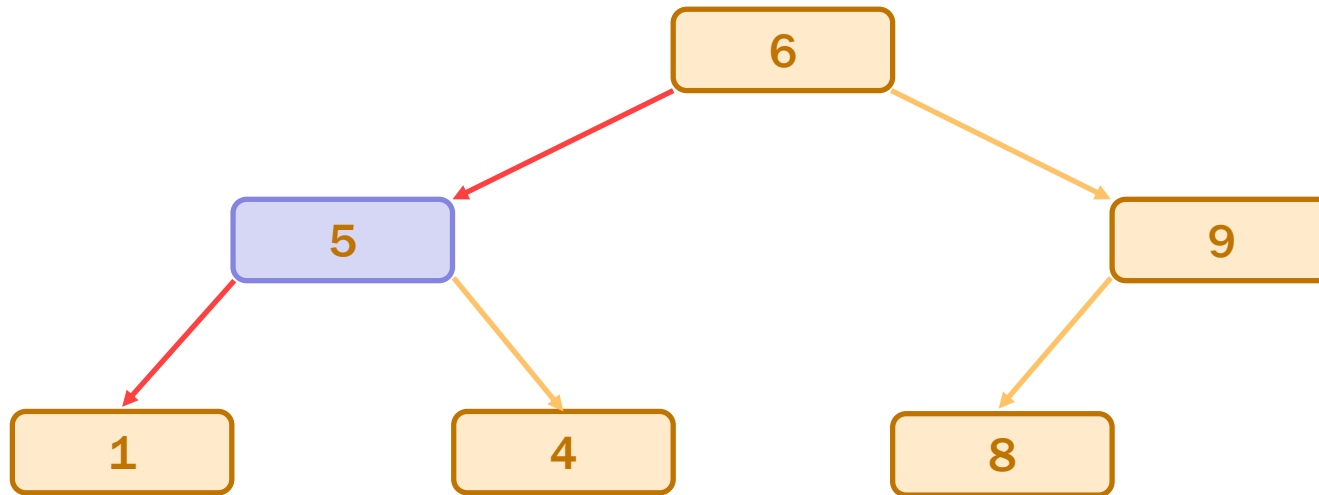
- Consider the following tree
 - searching for "4" proceeds as follows:



- Suppose someone changed "3" into "5"...

Recall: Binary Search Trees

- Suppose someone changed "3" into "5"...
 - now this happens when we search for "4":



- It can no longer be found!
Doesn't crash. It's just not found.
- Problem doesn't occur on the line with the change

Scary Bugs

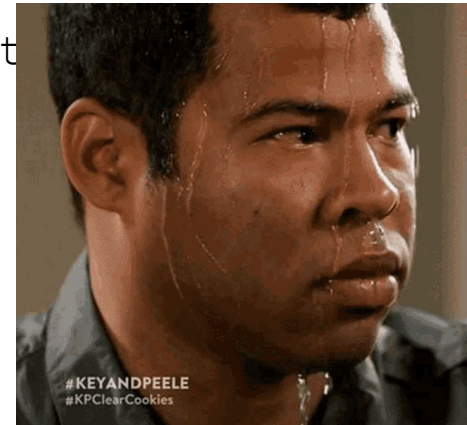
- **Do not fear crashes**
 - often no debugging at all
 - get a stack trace that tells you exactly where it went wrong
- **Do fear unexpected mutation**
 - failure will give you no clue what went wrong
 - will take a long time to realize the BST invariant was violated by mutation
 - bug could be almost anywhere in the code
 - anyone who mutates a `TreeNode` could have caused it
 - could take *weeks* to track it down

Another Example

```
class Name {  
    private String first;  
    private String last;  
  
    public String toString() {  
        return first + " " + last;  
    }  
  
    public void capitalize() {  
        this.first = first.substring(0, 1).toUpperCase()  
            + first.substring(1);  
        this.second = second.substring(0, 1).t  
            + second.substring(1);  
    }  
}
```

Somewhere else...

Map<Name, Integer> M;



Even Worse in C/C++

- C/C++ strings are **mutable**
 - commonly used as map keys
 - this sort of bug is still very common
- Java strings are immutable
 - was hugely controversial at the time
 - in retrospect, it was clearly a good idea
 - other mutable types can still be used as keys

Aliases

- Extra references to an object are called "aliases"
 - possible for any reference type
- Aliases are fine when objects are *immutable*
 - we don't care if someone else reads the data
 - we only care if someone mutates it
- Aliases are scary when objects are mutable...
 - creates the potential for failures far from bugs
 - that means **painful** debugging

Mutable Heap State

- “With great power, comes great responsibility”
 - Uncle Ben
- With aliases to mutable heap state:
 - gain efficiency in some cases
 - must keep track of every alias that could mutate that state
 - any alias, anywhere in the *entire* program could cause a bug
- **EJ 17**: minimize mutability in classes

Easy Ways to Stay Safe

1. Do not mutate heap state

- don't need to think about aliasing at all
- any number of aliases is fine

2. Do not allow aliases...

- create the state in your constructor and don't share it

```
class MyClass {  
    // RI: vals is sorted  
    private String[] vals;  
  
    public MyClass() {  
        this.vals = new String[10];    // only reference  
        ...  
    }  
}
```

Easy Ways to Stay Safe

- Not enough just to declare it "**private**"

```
class MyClass {  
    // RI: vals is sorted  
    private String[] vals;  
  
    ...  
  
    public String[] values() {  
        return this.vals;  
    };  
};
```

this is "representation exposure"
we wil treat it as a bug

- anyone can get an alias by calling `values()`
- "**private**" is a clue that aliases might be bad

Easy Ways to Stay Safe

2. Do not allow aliases

- (b) make a copy of anything you want to keep
 - does not matter if the caller mutates the original

```
class MyClass {  
    // RI: vals is sorted  
    private String[] vals;  
    ...  
    // @requires A is sorted  
    public MyClass(String[] A) {  
        this.vals = A; // unsafe!  
        this.vals = Arrays.copyOf(A, // make a copy  
            A.length);  
    };  
};
```

Easy Ways to Stay Safe

1. Do not use mutable state

- don't need to think about aliasing at all
- any number of aliases is fine

2. Do not allow aliases to *mutable* state

- a) do not hand out aliases yourself
- b) make a copy of anything you want to keep

ensures only one reference to the object (no aliases)

- For 331, mutable aliasing across files is a bug!
 - gives other parts the ability to break your code
 - we will stick to these simple strategies for avoiding it

An Advanced (Two-Stage) Approach

- **Mutable object has only one reference (**owner**)**
 - one reference that is allowed to use & mutate it
- **Object is eventually “frozen”, making it immutable**
 - no longer necessary to track ownership
- **Example: Java’s `StringBuilder` vs `String`**
 - `StringBuilder` **is mutable (be careful!)**
 - `StringBuilder.toString` **returns the value as a `String`**
 - `String` **is immutable**

Rules of Thumb

Client Side

1. Data is small
 - anything on screen is $O(1)$
2. Aliasing is common
 - UI design forces modules
 - data is widely shared

Rule: avoid mutation

- create new values instead
- performance will be fine

Server Side

1. Data is large
 - efficiency matters
2. Aliasing is avoidable
 - you decide on modules
 - data is not widely shared

Rule: avoid aliases

- do not allow aliases to your data
- hand out copies not aliases
- (good enough for us in 331)

Using List

- Same issue arises with `List` as with arrays

```
class MyClass {  
    // RI: vals is sorted  
    private List<String> vals;  
  
    public List<String> values() {  
        return this.vals; // unsafe  
    };  
}
```

- since a `List` is mutable, we cannot create aliases

Another Alternative

- With `List`, a third option is sometimes used:

```
class MyClass {  
    // RI: vals is sorted  
    private List<String> vals;  
  
    public List<String> values() {  
        return Collections.unmodifiableList(this.vals);  
    };  
}
```

- throws an exception when mutators are called
- runs in $O(1)$ time instead of $O(n)$ to copy

Can this change break the client?

Another Alternative

- **This can break clients**
 - this works with a copy

```
MyClass m = ...;  
List<String> list = m.values()  
list.add("another");
```

- **but not with** `UnmodifiableList`
- **Specification must make clear the behavior**
 - how do the two options relate?

Another Alternative

- **These two are incomparable**
 - they have differing behavior
 - client can work with one but not the other and v.v.
- **How is this possible when both return `List`?**
 - **the unmodifiable list does not implement `List`!**
the spec doesn't let you throw on any call to `add`
 - **this is a terrible idea**
but occasionally necessary in extreme circumstances
- **Really these are different return types**
 - would be better to make them different interfaces

Unmodifiable View

- **Unmodifiable list is a "view" of the underlying list**
- **It changes whenever the underlying list changes**
 - updates to that list show up in the view immediately
 - it is not a copy of the data at that point
- **This can lead to difficult bugs**
 - do not use such a view as a key in a map
 - any alias to it can mutate it at any point

Unmodifiable View

- Why would someone do this?
- Like most CS bugs, it is for performance
 - we all know that $O(1)$ is better than $O(n)$
- But most client uses are $O(n)$ anyway!
 - client probably wants to loop through the list
 - in that case, there is no $O(..)$ gain to
- We will stick to immutable or copying (no aliases)

Module Design

Module Design

"Designing modules is the heart of software design."

— Michael Ernst

- **In Java, a "module" is a file or a top-level class**
- **Module design is an enormous subject**
 - **can look for many properties such as decomposability, composability, understandability, continuity, isolation**
- **We will keep things simpler...**

Module Design

- Modules should have
 - high **cohesion**
 - low **coupling**
- **Cohesion**: the parts go together
 - they all serve one purpose or represent one concept
 - examples: an ADT, `java.util.Arrays`
 - non-example: one class for sorting, drawing, & printing
 - primarily about the **specification**

Module Design

- Modules should have
 - high **cohesion**
 - low **coupling**
- **Coupling**: the parts only understandable together
 - must learn both to understand either
 - example: an immutable ADT
 - non-example: a mutable ADT that allows aliases
 - must understand how all aliases are used to know if it's correct
 - primarily about the **implementation**
 - will see another non-example next time..

Coupling Is Bad

- Coupling makes the code less **understandable**
 - truth for both humans and AI
 - highly coupling becomes "spaghetti code"
 - often shows up as a "god class"
- Coupling makes the code hard to **change**
 - all the interrelated parts may require changes
- Coupling creates potential for **painful** debugging
 - bugs in one piece can cause failures in another
 - e.g., any misuse of an alias can break use by any other alias

Subclasses

Subclasses

- Subclassing is a means of sharing code
 - subclass gets parent fields & methods (unless overridden)

```
class Product {  
    private String name;  
    private int price;  
    public String getName() {return name; }  
    public int getPrice() { return price; }  
}  
  
class SaleProduct extends Product {  
    private float discount;  
    public int getPrice() {  
        return (1 - discount) * super.getPrice();  
    }  
}
```

Subclasses

- Subclassing is a surprisingly dangerous feature
- Subclassing tends to break modularity
 - creates **tight coupling** between super- and sub-class
 - often see the “fragile base class” problem
 - changes to super class often break subclasses
- Let's see some examples...

Example 1: Tight Coupling

```
class Product {  
    private int price;  
    public int getPrice() { return price; }  
  
    // @returns true iff obj's price < p's price  
    public boolean isCheaperThan(Product p) {  
        return getPrice() < p.getPrice();  
    }  
}  
  
class SaleProduct extends Product {  
    public int getPrice() {  
        return (1 - discount) * super.getPrice();  
    }  
}
```

– looks okay so far...

Example 1: Tight Coupling

```
class Product {  
    private int price;  
    public int getPrice() { return price; }  
  
    // @returns true iff obj's price < p's price  
    public boolean isCheaperThan(Product p) {  
        return this.price < p.price;  
    }  
}
```

Made it faster by eliminating a method call!

```
class SaleProduct extends Product {  
    public int getPrice() {  
        return (1 - discount) * super.getPrice();  
    }  
}
```

What's wrong?

Oops! Broke the subclass

Example 2: Tight Coupling

```
class InstrumentedHashSet extends HashSet<Integer> {  
    private static int count = 0;  
  
    public boolean add(Integer e) {  
        count += 1;  
        return super.add(e);  
    }  
  
    public boolean addAll(Collection<Integer> c) {  
        count += c.size();  
        return super.addAll(c);  
    }  
  
    public int getCount() { return count; }  
}
```

- what could possibly go wrong?

Example 2: Tight Coupling

```
InstrumentedHashSet S = new InstrumentedHashSet();  
System.out.println(S.getCount()); // 0  
S.addAll(Arrays.asList(1, 2));  
System.out.println(S.getCount()); // 4?!?
```

- what does this print?
- **What is printed depends on** `HashSet`'s `addAll`:
 - if it calls `add`, then this prints **4**
 - if it does not call `add`, then this prints **2**
- Also possible to be dependent on *order* of calls

Subclassing Creates Tight Coupling

- **Creates tight coupling between super- and sub-class**
- **Example 1: super-class needs to know about subclass**
 - direct field access in parent breaks subclass
- **Example 2: subclass needs to know about super-class**
 - subclass dependent on which methods call each other
- **But wait... There's more!**

Example 3: Tight Coupling

```
class WorkList {  
    // RI: len(names) = len(times) and total = sum(times)  
    protected ArrayList<String> names;  
    protected ArrayList<Integer> times;  
    protected int total;  
  
    public addWork(Job job) {  
        addToLists(job.getName(), job.getTime());  
        total += job.getTime();  
    }  
  
    protected addToLists(String name, int time) {  
        names.add(name);  
        times.add(time);  
    }  
}
```

Example 3: Tight Coupling

```
// Makes sure no task is too large compared to rest
class BalancedWorkList extends WorkList {
    protected addToLists(String name, int time) {
        if (times.size() <= 3 || 2*time < total)
            super.addToLists(name, time); // okay
        else {
            throw new ImbalancedWorkException(name, time);
        }
    }
}
```

- prevents item from being added if too big
- (also: this subclass is not a subtype!)

Example 3: Tight Coupling

```
class WorkList {  
    // RI: len(names) = len(times) and total = sum(times)  
    protected ArrayList<String> names;  
    protected ArrayList<Integer> times;  
    protected int total;  
  
    public addWork(Job job) {  
        int time = job.getTime(); // just one call  
        total += time;  
        addToLists(job.getName(), time);  
    }  
}
```

RI not true in method call

- reordering the updates breaks the subclass!
- subclass is using `total` that includes the new job

Example 3: Tight Coupling

- **RI can be false in calls to non-public methods**
 - only needs to hold at end of the public method
- **Requires extra care to get it right**
 - method is tightly coupled with the ones that call it
 - needs to know what is true in those methods
 - not enough to just know the RI
- **Hard for multiple people to communicate this clearly**
 - can be okay when it's all your code
 - very error prone when methods are written by others

Subclassing Creates Tight Coupling

- Creates tight coupling between super- and sub-class
 - direct field access can break subclass
 - subclass dependent on which methods call each other
 - subclass dependent on *order* of method calls
 - subclass can be called when RI is false
- Often see the “**fragile base class**” problem
- Subclassing is a surprisingly dangerous feature!
 - up to you to verify subclass method specs are stronger
 - up to you to prevent tight coupling

Subclassing is Best Avoided

- **EJ 19**: either design for subclassing or prohibit it
 - from Josh Bloch, author of (much of) the Java libraries
- We haven't used subclassing in our ADTs
 - we used interfaces and implemented them with classes
 - these problems are the main reason why we avoided it
- Subclassing is not necessary anyway
 - we have other ways to share code
 - **EJ 18**: prefer composition to inheritance

Equality

Equity of User-Defined Types

- For any type, useful to know which are “the same”
- Java “==” is not useful on records:

```
new Integer(1) == new Integer(1) // false!
```

- this is “reference equality”
 - tells you if they refer to the same object in memory
- Checking if the fields are the same is also wrong
 - different concrete states can have same abstract state

Storing a List In Two Parts

```
// Stores a list, split in two parts.  
class ListPair implements List {  
  
    // AF: obj = this.front ++ this.back  
    private List front;  
    private List back;
```

- three ways of representing the same abstract state:

front	back	front # back
[1, 2]	[]	[1, 2]
[1]	[2]	[1, 2]
[]	[1, 2]	[1, 2]

- same abstract states should be considered equal!

Recall: HW3

```
/**
 * Represents an immutable collection of integers.
 *
 * Clients can think of a set as a list of integers. However, they can only ask
 * if an integer is present or not. The order of the integers does not matter.
 * The number of times that an integer appears in the list does not matter.
 */
public interface IntSet {
    /**
     * Determines whether n is in the list.
     * @param n the number to look for in the list
     * @returns contains(n, obj), where
     *     contains(n, nil) := false
     *     contains(n, m :: L) := true if m = n
     *     contains(n, m :: L) := contains(n, L) if m /= n
     */
    public boolean contains(int n);

    /**
     * Creates and returns a new list containing n as well as all of obj.
     * @param n the number to add to the new list.
     * @returns n :: obj
     */
    public IntSet add(int n);
}
```

The abstract state allows duplicates,
but clients can't tell.

Equality on Sets

- Suppose our concrete representation is:

```
// RI: this.list has no duplicates
// AF: obj = this.list
private List list;
```

- Method `add` returns a different list than the spec
 - spec says `add(1)` on `[1]` returns `[1, 1]`
 - if the code add a second 1, abstract state is still `[1]`
- Need "equal" that says these states are "the same"
 - two abstract states are equal if they contain the same values

`equal(L, R) := true` iff `contains(x, L) = contains(x, R)` for any `x`

Equality

- **Often useful / necessary to define your own `equal`**
 - check if references point to records that are “the same”
- **Sensible definition should act like “=” in math:**
 1. $\text{equal}(a, a) = \text{True}$ for any $a : A$ **reflexive**
 2. $\text{equal}(a, b) = \text{equal}(b, a)$ for any $a, b : A$ **symmetric**
 3. if $\text{equal}(a, b)$ and $\text{equal}(b, c)$, then $\text{equal}(a, c)$ for any ... **transitive**
 - (311 alert: this is an “equivalence relation”)
 - Java has two more rules for `Object.equal`

Java Equals

- Java requires the following parts:

1. `a.equals(a) = true`

2. `a.equals(b) == b.equals(a)`

3. `a.equals(b)` and `b.equals(c)` means `a.equals(c)`

4. `a.equals(null) = false`

asymmetric with null

5. `a.equals(b)` cannot change value unless `a` or `b` is mutated

consistency

Equals in Java

- Every class inherits an `equals` method
 - this implements reference equality

```
public class Object {  
    public boolean equals(Object o) {  
        return this == o;  
    }  
}
```

- Make your own `equals` by overriding it:

```
public class MyClass {  
    public boolean equals(Object o) {  
        // ... new code here ...  
    }  
}
```

Example: Duration

- **Define Duration to be an amount of time in seconds**
 - one representation stores separate minutes and seconds

type Duration = {min : \mathbb{Z} , sec : \mathbb{Z} } with $0 \leq \text{sec} < 60$

- second part is a **rep invariant**
- **Can define equality on Duration this way:**

$\text{equal}(\{\text{min: } m, \text{sec: } s\}, \{\text{min: } n, \text{sec: } t\}) := (m = n) \text{ and } (s = t)$

- **true iff these are the same amount of time**
(wouldn't be true without the invariant)

Example: Duration

$\text{equal}(\{\text{min: } m, \text{sec: } s\}, \{\text{min: } n, \text{sec: } t\}) := (m = n) \text{ and } (s = t)$

- Does this have the required properties?

- reflexive

$\text{equal}(\{\text{min: } m, \text{sec: } s\}, \{\text{min: } m, \text{sec: } s\})$

$= (m = m) \text{ and } (s = s)$

$= \text{True} \text{ and True}$

$= \text{True}$

def of equal

proof by calculation
that it holds for any record

- symmetric

$\text{equal}(\{\text{min: } m, \text{sec: } s\}, \{\text{min: } n, \text{sec: } t\})$

$= (m = n) \text{ and } (s = t)$

$= (n = m) \text{ and } (t = s)$

$= \text{equal}(\{\text{min: } n, \text{sec: } t\}, \{\text{min: } m, \text{sec: } s\})$

def of equal

def of equal

Example: Duration

$\text{equal}(\{\text{min: } m, \text{sec: } s\}, \{\text{min: } n, \text{sec: } t\}) := (m = n) \text{ and } (s = t)$

- Does this have the required properties?
 - **reflexive** yes
 - **symmetric** yes
 - **transitive** also yes (but a little long for a slide)
- Good evidence that this is a reasonable definition

Non-Example: “==” in JavaScript

```
0 == "0"      true
0 == ""       true
0 == "  "     true
```

- Which property fails?
 - **transitivity**: "" != " "
- Good evidence that this is not a reasonable definition

Example: Duration in Java

```
// Represents an amount of time measured in seconds
class Duration {

    // RI: 0 <= sec < 60
    // AF: obj = 60 * this.min + this.sec
    private int min;
    private int sec;

    public boolean equals(Duration d) {
        return this.min == d.min && this.sec == d.sec;
    };
}
```

- What is wrong with this?
 - it doesn't override `equals(Object)`

Example: Duration in Java

```
// Represents an amount of time measured in seconds
class Duration {

    // RI: 0 <= sec < 60
    // AF: obj = 60 * this.min + this.sec
    private int min;
    private int sec;

    public boolean equals(Object o) {
        return this.min == o.min && this.sec == o.sec;
    };
}
```

- What is wrong with this?
 - it doesn't compile

Example: Duration in Java

```
// Represents an amount of time measured in seconds
class Duration {

    // RI: 0 <= sec < 60
    // AF: obj = 60 * this.min + this.sec
    private int min;
    private int sec;

    public boolean equals(Object o) {
        if (!(o instanceof Duration))
            return false;

        Duration d = (Duration) o;
        return this.min == d.min && this.sec == d.sec;
    }
}
```

- Correct and idiomatic Java

Example: NanoDuration

- Suppose a subclass also measures nanoseconds

```
class NanoDuration extends Duration {  
    // min: number (inherited)  
    // sec: number (inherited)  
    private int nano;  
    ...  
}
```

- How should we define `equal`?

Example: NanoDuration

```
class NanoDuration extends Duration {  
    // min: number (inherited)  
    // sec: number (inherited)  
    private int nano;  
  
    public boolean equals(Object o) {  
        if (!(o instanceof NanoDuration)) {  
            return false;  
        }  
  
        NanoDuration n = (NanoDuration) o;  
        return this.min === n.min &&  
            this.sec === n.sec &&  
            this.nano === n.nano;  
    }  
}
```

symmetry

- Which property does this lack?

Example: NanoDuration

```
Duration d = new Duration(2, 10);  
NanoDuration n = new NanoDuration(2, 10, 300);  
  
System.out.println(n.equals(d)); // false  
System.out.println(d.equals(n)); // true!
```

- NanoDuration **is only equal to other** NanoDuration**s**
- Duration **can be equal to a** NanoDuration
if they have the same minutes and seconds

Example: NanoDuration

```
class NanoDuration extends Duration {  
  
    public boolean equals(Object o) {  
        if (!(o instanceof Duration))  
            return false;  
  
        if (!(o instanceof NanoDuration)) {  
            Duration d = (Duration) o;  
            return this.min == d.min && this.sec == d.sec;  
        } else {  
            NanoDuration n = (NanoDuration) o;  
            return this.min === d.min &&  
                this.sec === d.sec && this.nano === d.nano;  
        }  
    }  
};
```

- Fixes symmetry! all good now?

No! It lacks transitivity

Example: NanoDuration

```
NanoDuration n1 = new NanoDuration(2, 10, 300);  
Duration d = new Duration(2, 10);  
NanoDuration n2 = new NanoDuration(2, 10, 400);
```

```
System.out.println(n1.equals(d)); // true  
System.out.println(d.equals(n2)); // true  
System.out.println(n1.equals(n2)); // false!
```

- **transitivity requires** `n1` **to equal** `n2` (but it doesn't)

Example: NanoDuration

- Can fix this instead as follows:
 - have both agree that `Duration` \neq `NanoDuration`

```
class Duration {  
    ...  
    public boolean equals(Object o) {  
        if (!(o instanceof Duration) ||  
            (o instanceof NanoDuration))  
            return false;  
  
        Duration d = (Duration) o;  
        return this.min == d.min && this.sec == d.sec;  
    }  
}
```

- This is arguably the most sensible answer...

Example: NanoDuration

- Should have spelled out the abstract states:

```
// Represents an amount of time in nanoseconds
class NanoDuration extends Duration {

    // RI: 0 <= sec < 60 and 0 <= nano < 10000
    // AF: obj = 60,000,000 * this.min +
    //           1,000,000 * this.sec +
    //           this.nano
    private int nano;

}
```

- Abstract states of the two types are **different**
 - time in seconds vs nanoseconds
 - two different types of things should not be equal

Duration and NanoDuration

- We fixed it... but at what cost?
- `Duration` **and** `NanoDuration` **are tightly coupled**
 - the two classes are tightly intertwined
- This **usually** happens with subclasses
 - saw several different ways they are interdependent
 - very hard to avoid coupling between subclasses
 - EJ 19: either design for subclassing or prohibit it
 - better to simply not use it
 - find other ways to share code (e.g., shared utility functions etc.)

HashCode in Java

- Java has another method called `hashCode`

```
public int hashCode();
```

- **Should override `hashCode` and `equals` together**
 - almost certainly a bug to only override `equals`

Java hashCode

- Java has another method called `hashCode`
 - provided to make `HashMap` etc. work

```
public int hashCode();
```

- Its spec has the following requirements:
 1. `a.hashCode()` cannot change value unless `a` is mutated
self-consistency
 2. `a.equals(b)` means `a.hashCode() == b.hashCode()`
consistent with equals
when equals changes, so does hashCode

Equals & hashCode in Java

- Every class inherits a `hashCode` method

```
public class Object {  
    public int hashCode() {  
        // ... consistent with reference equality ...  
    }  
}
```

- When you override `equals`, also override `hashCode`
 - almost certainly a bug to only override `equals`

```
public class MyClass {  
    public int hashCode() {  
        // ... something consistent with new equality ...  
    }  
}
```