
CSE 331
Software Design & Implementation

Winter 2026
Section 8 – Arrays

Administrivia

- HW7 released tonight - **Due @ 11:59pm next Wed**



Array Notation: Indexing

- Arrays are treated like Lists *mathematically*
 - They are an alternative way to represent Lists in *code*
- To get the j th element, use $\text{at}(L, j)$, abbreviated “ $L[j]$ ”

$$\begin{aligned} \text{at} &: (\text{List}, \mathbb{N}) \rightarrow \mathbb{Z} \\ \text{at}(\text{nil}, n) &:= \text{undefined} \\ \text{at}(x :: L, 0) &:= x \\ \text{at}(x :: L, n+1) &:= \text{at}(L, n) \end{aligned}$$

- Must ensure that $0 \leq j < \text{length of array}$

More Array Notation

- **Prefix:** All elements from the start to $j+1$ (exclusive):
 - $A[..j] = \text{prefix}(A, j+1)$
 - **Add note about this not matching Python**
- **Suffix:** All elements starting at j (inclusive) to the end:
 - $A[j..] = \text{suffix}(A, j)$
- Thus, $A[..j-1] ++ A[j..] = A$
 - 331 notation is inclusive of both indices

Other useful facts:

- $A[\text{len}(A)..] = \text{nil}$
- $A[..-1] = \text{nil}$
- $A[..j-1] \# A[j] = A[..j]$
- $A[.. \text{len}(A)-1] = A$

'For Any' Facts

- Necessary facts about arbitrary parts of an array
- Ex: To show an array is sorted in asc formally:
 - $A[j] < A[j+1]$ for any $0 \leq j < \text{len}(A) - 1$

```
// @requires A[i] < A[i+1] for any 0 <= i < len(A)-1
// @returns false if A[i] != y for any 0 <= i < len(A)
//           true otherwise
public boolean bsearch(int[] A, int y) { ... }
```

Array Mutation

- Array mutation can change “for any” facts!

- Ex:

$\{ \{ A[j] < A[j+1] \text{ for any } 0 \leq j \leq 9 \} \}$

$A[0] = 100;$

↓
 $\{ \{ (A[j] < A[j+1] \text{ for any } 1 \leq j \leq 9) \text{ and } A[0] = 100 \} \}$

- Old facts about $A[0]$ could be invalidated!
 - Need to update the range of “for any” facts

Mutating Arrays (add/remove)

- Adding to the end of an array

↓	{{ P(A) }}	↑	{{ P(A + [100]) }}
	A.add(100);		A.add(100);
	{{ P(A_0) and A = A_0 + [100] }}		{{ P(A) }}

- Removing from the end of an array

↓	{{ P(A) }}	↑	{{ P(A[..len(A) - 2]) }}
	A.remove(A.size() - 1);		A.remove(A.size() - 1);
	{{ P(A_0) and A = A_0[..len(A_0) - 2] }}		{{ P(A) }}