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# CSE 331

## Software Design & Implementation

Winter 2026  
Section 3 – ADTs

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# Administrivia

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- HW3 released tonight - **Due next Wed 11:59pm**



# Specifications for ADTs – Review

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- New Terminology for specifying ADTs:
  - **Abstract State / Representation (Math)**
    - How clients should understand the object
    - Ex: `List(nil or cons)`
  - **Concrete State / Representation (Code)**
    - Actual fields of the record and the data stored
    - Ex: 

```
public class List {  
    final int hd;  
    final List tl;
```

# State Representations

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- We've had different abstract and concrete types all along!
  - in our math, `List` is an inductive type (abstract)
  - in our code, `List` is a class with two fields (concrete)
- Term “object” (or “obj”) will refer to abstract state
  - “object” means mathematical object (representative of the class as a whole or as an idea)
  - “obj” is the mathematical value that the record represents (similar to a specific instance of a class)

# Internally Documenting ADTs – Review

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**Abstract Function (AF)** – defines what abstract state the field values represent

- Maps field values  $\rightarrow$  the object they represent
- Output is math, this is a mathematical function

**Representation Invariants (RI)** – facts about the field values that must always be true

- Constructor must always make sure RI is true at runtime
- Can assume RI is true when reasoning about methods
- AF only needs to make sense when RI holds
- Must ensure that RI *always* holds

# Documenting ADTs – Example

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// A list of integers that can retrieve the last element in  $O(1)$

```
interface FastList {
```

```
    /**
```

```
     * Returns the object as a regular list
```


```
     * @returns obj
```

```
    */
```

```
    List toList();
```

```
}
```

Talk about functions in terms of the abstract state (obj)



Hide the representation details (i.e. real fields) from the client

```
class FastLastList implements FastList {
```

```
    // RI: this.last = last(this.list);
```

```
    // AF: obj = this.list;
```

```
    // @returns last(obj)
```

```
    int getLast() {
```

```
        return this.last;
```

```
    };
```

```
}
```