

CSE 331: Software Design & Implementation

Practice Midterm

Name: _____

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This exam contains 10 pages and 7 problems, worth 73 points total.

Instructions

- Do not open the exam until instructed to do so.
- This is a closed-book, closed-notes exam. No electronic devices.
- Write your name and UW email at the top of this page.
- For every question involving proofs, assertions, and invariants, assume each numeric quantity is an unbounded integer: overflow cannot happen and numbers have no fractional parts. Integer division truncates as in Java, so $5/3$ evaluates to 1.
- If you need more room, continue on the back of the page and write “continued on back” next to the problem.
- If a problem is ambiguous, write down the interpretation you chose and answer under that interpretation.
- Many of these problems have short answers even when the problem itself is long. Don’t be alarmed.
- Budget your time. Point values are a rough guide to how long each problem should take.

Problem	Topic	Points	Score
1	Forward reasoning	5	
2	Backward reasoning	8	
3	ADT, rep invariant, abstraction function	10	
4	Writing specifications	12	
5	Loop invariant proof	16	
6	Testing	12	
7	Comparing specifications	10	
Total		73	

Problem 1: Forward reasoning (5 points)

Starting from the given assertion, fill in an appropriate assertion at each blank. Simplify your final answer where possible, but do not weaken it in the process.

{ $x \geq 5$ }

$y = 3 * x;$

{ _____ }

$x = x + 2;$

{ _____ }

$y = y + 1;$

{ _____ }

Problem 2: Backward reasoning (8 points)

Find the weakest precondition under which the code below establishes the given postcondition. Fill in an appropriate assertion at each blank and simplify your final answer where possible.

```
{ _____ }  
if (x > 0) {  
    { _____ }  
    x = y + 1;  
    { _____ }  
} else {  
    { _____ }  
    y = x - 1;  
    { _____ }  
}  
{ x > 0 and y > 0 }
```

Reference code for Problems 3–6

Problems 3 through 6 all concern the two classes below. Problem 7 is independent of them.

Point

Point is an immutable 2-D point on the plane in rectangular coordinates.

```
public class Point {
    // instance variables -- coordinates
    private final int x, y;

    // constructor
    public Point(int x, int y) {
        this.x = x;
        this.y = y;
    }

    // observer methods
    public int getX() { return this.x; }
    public int getY() { return this.y; }

    public boolean equals(Object o) {
        // you may assume this works properly
    }
} // end class Point
```

FinitePointBag

FinitePointBag is a mutable unordered collection of Point objects, possibly containing duplicates, with a finite capacity.

```
public class FinitePointBag {
    // instance variables: uses an array and size instead of a List
    private Point[] points;
    private int size;

    // construct a new FinitePointBag with given capacity, which
    // cannot be negative
    public FinitePointBag(int maxItems) {
        points = new Point[maxItems];
        size = 0;
    }
    // = capacity of this
    public int capacity() { return points.length; }
    // = current number of items in this
    public int size() { return size; }
    // add a new point if space available; return true if succeeded
    public boolean add(Point p) {
        if (size < capacity()) {
            points[size] = p;
            size++;
            return true;
        } else {
            return false;
        }
    }
    // return true if p is contained in this, otherwise false
    public boolean contains(Point p) {
        for (int k = 0; k < size(); k++) {
            if (points[k].equals(p)) {
                return true;
            }
        }
        return false;
    }
    // remove all copies of p from this
    public void removeAll(Point p) {
        int i, k;
        i = 0;
        k = 0;
        while (k != size) {
            if (!points[k].equals(p)) {
                points[i] = points[k];
                i = i + 1;
            }
            k = k + 1;
        }
        size = i;
    }
} // end of FinitePointBag
```

Problem 3: ADT, rep invariant, abstraction function (10 points)

Before we can work with `FinitePointBag` we need to understand the ADT it represents. Your answers must be consistent with the instance variables and code given above.

(a) (3 points) Give a suitable description of the `FinitePointBag` ADT and its abstract value, as would normally appear in the Javadoc comment directly above the class definition. (Hint: the answer might be quite short.)

(b) (4 points) Give a suitable representation invariant (RI) for `FinitePointBag`.

(c) (3 points) Give a suitable abstraction function (AF) for `FinitePointBag`.

Problem 4: Writing specifications (12 points)

As usual, whoever writes these exams doesn't provide proper specifications for things. Write a correct CSE 331-style specification for the `contains` and `removeAll` methods of `FinitePointBag`. Your answers must be consistent with the given code and what it actually does when executed.

```
/** Return true if p is contained in this, otherwise false
```

```
*
```

```
* _____
```

```
* _____
```

```
* _____
```

```
*/
```

```
public boolean contains(Point p) { ... }
```

```
/** Remove all copies of a point from this FinitePointBag
```

```
*
```

```
* _____
```

```
* _____
```

```
* _____
```

```
* _____
```

```
*/
```

```
public void removeAll(Point p) { ... }
```

Problem 5: Loop invariant proof (16 points)

We think `removeAll` is correct, but we would like to prove that it really does remove every point equal to `p`.

To keep this manageable, you do **not** need to track history variables or anything else required to prove that the values copied are the original values from the array. Just show that the `FinitePointBag` contains no copies of `p` after the method executes.

You may write `{inv}` to refer to the loop invariant rather than restating it each time.

```
// remove all copies of p from this FinitePointBag
public void removeAll(Point p) {
    { p != null and RI }
    int i, k;
    i = 0;
    k = 0;
    {inv: _____
      _____ }
    while (k != size) {
        { _____ }
        if (!points[k].equals(p)) {
            { _____ }
            points[i] = points[k];
            { _____ }
            i = i + 1;
            { _____ }
        } else { // no code -- place for any needed assertions
            { _____ }
        } // end if
        { _____ }
        k = k + 1;
        { _____ }
    } // end while
    { _____ }
    size = i;
    { _____ }
}
```

Problem 6: Testing (12 points)

The proof gives us good confidence that `removeAll` works, but we still need to test it. Write tests for this method. Then explain your approach to testing.

Problem 7: Comparing specifications (10 points)

Here are four possible specifications for a method that allocates an `int` array whose length is given by the parameter `n` and returns a reference to the newly allocated array.

- A. `@param n`
`@return` a new `int` array with `n` elements if `n > 0`,
otherwise return `null`
- B. `@param n`
`@requires n > 0`
`@return` a new `int` array with `n` elements
- C. `@param n`
`@requires n >= 0`
`@return` a new `int` array with `n` elements if `n > 0`,
otherwise return `null`
- D. `@param n`
`@return` a new `int` array with `n` elements
`@throws IllegalArgumentException` if `n <= 0`

- List all specifications stronger than A (do not include A): _____
- List all specifications stronger than B (do not include B): _____
- List all specifications stronger than C (do not include C): _____
- List all specifications stronger than D (do not include D): _____
- Is it possible for a single implementation to satisfy both A and B? (yes or no) _____
- Is it possible for a single implementation to satisfy both B and C? (yes or no) _____