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CSE 331

# Software Design & Implementation

Autumn 2023

Section 5 – Functional Programming III

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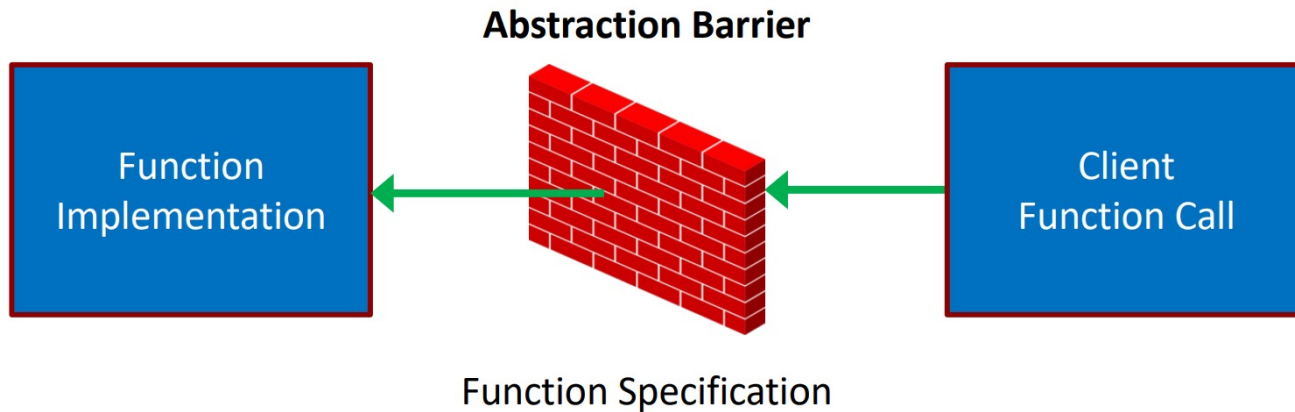
# Administrivia

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- HW5 released later today
  - Due Wednesday (11/1) @ 11:00pm
  - Remember to check that the autograder passes! Helps make sure you turned in the right files, pass the linter, etc.
- Can resubmit as many times as you'd like until the deadline.
  - Use the autograder as a tool if you're not sure if your code/tests have bugs

# Abstraction Barrier – Review

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- Specifications acts as the “barrier” between each side
  - improves understandability, changeability, and modularity
- Clients can only depend on the spec
- Implementer can write any code that satisfies the spec

# Specifications for ADTs – Review

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- New Terminology for specifying ADTs:
  - **Concrete State / Representation (Code)**
    - Actual fields of the record and the data stored
    - Ex: { list: `List`, last: `number` | `undefined` }
  - **Abstract State / Representation (Math)**
    - How clients should understand the object
    - Ex: List (nil or cons)

# Specifications for ADTs – Review

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```
/**
 * A list of integers that can retrieve the last
 * element in O(1) time.
 */
export interface FastList {
  ...
  /**
   * Returns the object as a regular list of items.
   * @returns obj ← obj is the abstract state
   */
  toList: () => List<number>;
}
```

- Talk about functions in terms of the abstract state
- Hide the representation details (i.e. real fields) from the client

# Documenting ADTs – Review

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**Abstract Function (AF)** – defines what abstract state the field values represent

- Maps field values → the object they represent
- Output is math, this is a mathematical function

**Representation Invariants (RI)** – facts about the field values that must always be true

- Constructor must always make sure RI is true at runtime
- Can assume RI is true when reasoning about methods
- AF only needs to make sense when RI holds
- Must ensure that RI *always* holds

# Documenting ADTs – Review

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```
class FastLastList implements FastList {  
  // RI: this.last = last(this.list)  
  // AF: obj = this.list  
  ...  
  // @returns last(obj)  
  getLast = (): number | undefined => {  
    return this.last;  
  };  
}
```

Prove correctness of `last(obj) = this.last` using both

`Last(obj) = last(this.list)`  
`= this.last`

**by AF**  
**by RI**

# Defining Interfaces

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Typescript

```
interface FastList {  
  getLast: () => number | undefined;  
  toList: () => List<number>;  
}
```



Java

```
interface FastList {  
  int getLast() throws EmptyList;  
  List<Integer> toList();  
}
```



# Readonly – Typescript

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- The prefix **readonly** is used to make a property read-only
  - Value cannot be changed
  - Protects variables from unwanted mutations
  - Should be our default

**Ex:**

```
class FastLastListImpl implements FastList {  
    readonly last: number | undefined;  
    readonly list: List<number>;  
}
```

# Abstract Data Class – Example

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```
class FastLastListImpl implements FastList {
    readonly last: number | undefined;
    readonly list: List<number>;

    constructor(list: List<number>) {
        this.last = last(list);
        this.list = list;
    }

    getLast = () => { return this.last; }
    toList = () => { return this.list; }
}
```

Can create new record using “new”:

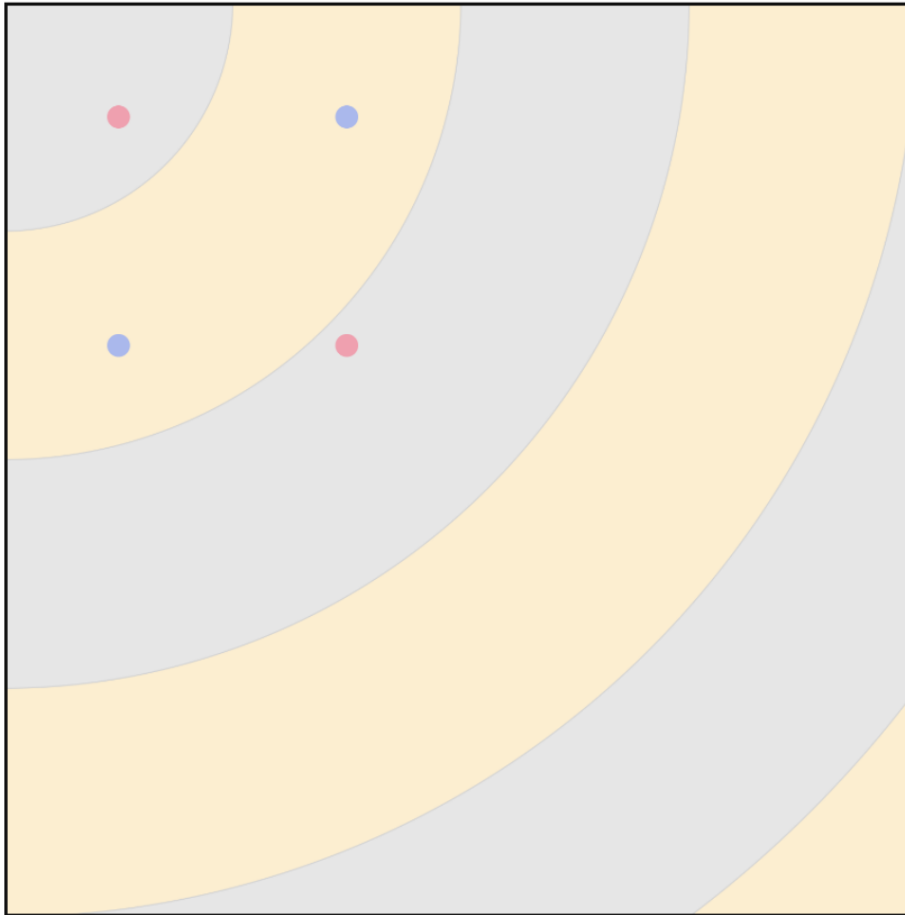
```
new FastLastListImpl(list);
```

```
interface FastList {
    getLast: () => number | undefined;
    toList: () => List<number>;
}
```

# Question 1 & 2 – Coding

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Run `npm run start` in `sec-highlight` to check it out!



input the points:

```
100 100
100 300
300 100
300 300
```

# Questions 1 & 2 – Recap

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- From concrete implementation → ADT, writing specs shouldn't be too hard
  - the specs already exist
  - just need to adjust what objects they're operating on:  
parameters → 'obj'
  - and add appropriate AF and RI
- Only did 1 in this example, but we're able to have multiple classes implement the same interface, all with the same spec
  - Implementation can be switched out as needed, but expected inputs and behavior (spec) will be consistent

# Question 4

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Prove by structural induction that, for any left-leaning tree  $T$ , we have:  $\text{size}(T) \leq 2^{\text{height}(T)+1} - 1$

## Hints:

- 1) Define the tree in your IH according to the definition of tree `node(x, S, T)` so you can access the left and right trees
- 2) Remember the exponent rule:  $x^y \times x = x^{y+1}$

```
func size(empty)      := 0
      size(node(x, S, T)) := 1 + size(S) + size(T)
func height(empty)   := -1
      height(node(x, S, T)) := 1 + height(S)   for any  $x : \mathbb{Z}$  and  $S, T : \text{Tree}$ 
```

## Question 3 – Preface

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sep takes a list  $L$  and a value  $x$ , and returns two lists,  $A$  containing all values  $\leq x$  and  $B$  containing all values  $> x$ .

```
func sep(nil, x)           := (nil, nil)
    sep(cons(y, L), x)    := (cons(y, A), B)           if  $y \leq x$ 
    sep(cons(y, L), x)    := (A, cons(y, B))          if  $x < y$ 
                        where  $(A, B) := \text{sep}(L, x)$ 
```

**Note:** in the recursive case, you:

- make a call to **sep**( $L, x$ )
- take the return value of that call ( $A, B$ )
- **cons**( $y$  on to  $A$  or  $B$  and returns  $(A, \text{cons}(y, B))$  or  $(\text{cons}(y, A), B)$ )
- Making an additional step to make our recursive result cleaner and avoid multiple recursive calls