

CSE 331

Equality

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- Section tomorrow is final exam practice
 - will focus on problems not included in midterm mutable ADTs and writing loops given invariant
- Will email some reading tonight
 - problems reference an ADT definition
 - time in section is too short to read and do problems

final exam is 1 hour and 50 minutes, so there will be time to read then

Equality

Equity of User-Defined Types

- For any type, useful to know which are "the same"
- TypeScript "===" is not useful on records:

{a: 1} === {a: 1} // false!

- as in Java, this is "reference equality"
- tells you if they refer to the same object in memory
- deepStrictEquals would work here
 - checks that the records have the same fields and values
 - but that also is not perfect...

// Implements a queue using two lists.
class ListPairQueue implements NumberQueue {
 // AF: obj = concat(this.front, rev(this.back))
 readonly front: List<number>;
 readonly back: List<number>;

– two ways of representing the same abstract state:

{front: cons(1, cons(2, nil)), back: nil} // = 1, 2
{front: nil, back: cons(2, cons(1, nil))} // = 1, 2

– these should be considered equal!

- Often useful / necessary to define your own equal
 - check if references point to records that are "the same"
- Sensible definition should act like "=" in math:
 - 1. equal(a, a) = T for any a : A reflexive
 - 2. equal(a, b) = equal(b, a) for any a, b : A symmetric
 - 3. if equal(a, b) and equal(b, c), then equal(a, c) for any ...

transitive

- (311 alert: this is an "equivalence relation")
- Java has two more rules for equals (see Java docs)

• Define Duration representing an amount of time

type Duration = {min : \mathbb{Z} , sec : \mathbb{Z} } with $0 \le sec < 60$

- second part is an invariant

• Can define equality on Duration this way:

equal({min: m, sec: s}, {min: n, sec: t}) := (m = n) and (s = t)

 true iff these are the same amount of time (wouldn't be true without the invariant) equal({min: m, sec: s}, {min: n, sec: t}) := (m = n) and (s = t)

Does this have the required properties?

- reflexive

```
equal({min: m, sec: s}, {min: m, sec: s})

= (m = m) and (s = s) def of equal

= T and T

= T
```

proof by calculation

- symmetric

 $\begin{aligned} & \text{equal}(\{\min: m, \text{sec: }s\}, \{\min: n, \text{sec: }t\}) \\ &= (m = n) \text{ and } (s = t) & \text{def of equal} \\ &= (n = m) \text{ and } (t = s) \\ &= \text{equal}(\{\min: n, \text{sec: }t\}, \{\min: m, \text{sec: }s\}) & \text{def of equal} \end{aligned}$

equal({min: m, sec: s}, {min: n, sec: t}) := (m = n) and (s = t)

- Does this have the required properties?
 - reflexive yes
 - symmetric yes
 - transitive also yes (but a little long for a slide)
- Good evidence that this is a reasonable definition

• Can define equality on List type this way:

equal(nil, nil)	:=	Т	
equal(nil, cons(b, R))	:=	F	
equal(cons(a, L), nil)	:=	F	
equal(cons(a, L), cons(b, R))	:=	F	if a ≠ b
equal(cons(a, L), cons(b, R))	:=	equal(L, R)	if $a = b$

- Checks that the values in the list are all the same
 - this is a definition, so we can only check it on examples...

equal(
$$1 \rightarrow 2$$
, $1 \rightarrow 2$) = equal(2 , 2)
= equal(nil, nil)
= T

• Can define equality on List type this way:

equal(nil, nil)	:=	Т	
equal(nil, cons(b, R))	:=	F	
equal(cons(a, L), nil)	:=	F	
equal(cons(a, L), cons(b, R))	:=	F	if a ≠ b
equal(cons(a, L), cons(b, R))	:=	equal(L, R)	if $a = b$

- Checks that the values in the list are all the same
 - this is a definition, so we can only check it on examples...

equal(
$$1 \rightarrow 2$$
, $1 \rightarrow 3$) = equal(2 , 3)
= F

• Can define equality on List type this way:

equal(nil, nil)	:=	Т	
equal(nil, cons(b, R))	:=	F	
equal(cons(a, L), nil)	:=	F	
equal(cons(a, L), cons(b, R))	:=	F	if a ≠ b
equal(cons(a, L), cons(b, R))	:=	equal(L, R)	if $a = b$

- Has all three required properties
 - how would we prove this?

induction

Recall: Subtypes of Concrete Types

- We initially defined types as sets
- In math, a **subtype** can be thought of as a **subset**
 - e.g., the even integers are a subtype of $\ensuremath{\mathbb{Z}}$
 - e.g., the numbers $\{1, 2, 3, 4, 5, 6\}$ are a subtype of \mathbb{Z}
 - likewise, a **superset** would be a **supertype**
- Any even integer "is an" integer

- "is a" is often (but not always) good intuition for subtypes

Recall: Subtypes of Abstract Types

- Subtypes are **substitutable** for supertype
 - this is the "Liskov substitution principle"
 - due to Barbra Liskov
- For ADTs, we use this as our definition of subtype
- When is ADT B substitutable for A?
 - **1.** B must provide all the methods of A

If A has a method "f", then B must have a method called "f"

2. B's corresponding method spec must be stronger than A's must accept all the inputs that A's does must also promise everything in A's postcondition

```
// Represents an amount of time measured in seconds
class Duration {
    // RI: 0 <= sec < 60
    // AF: obj = 60 * this.min + this.sec
    readonly min: number;
    readonly sec: number;
    equal = (d: Duration): boolean => {
        return this.min === d.min && this.sec === d.sec;
    };
    ...
```

- defines Duration as an ADT instead

getMinutes and getSeconds methods not shown
equal still makes sense, just as before

Suppose a subclass also measures nanoseconds

```
class NanoDuration extends Duration {
   // min: number (inherited)
   // sec: number (inherited)
   readonly nano: number;
```

How should we define equal?

...

– remember that it takes an argument of type Duration

```
we cannot accept fewer arguments
```

```
class NanoDuration extends Duration {
  // min: number (inherited)
  // sec: number (inherited)
                                         Must take Duration
                                       argument to be a subtype
  readonly nano: number;
  equal = (d: Duration): boolean => {
    if (d instanceof NanoDuration) {
      return this.min === d.min &&
              this.sec === d.sec &&
              this.nano === d.nano;
    } else {
      return false;
    }
                                       No! It lacks symmetry
  };
```

- does this have the three required properties?

Example: NanoDuration

```
const d = new Duration(2, 10);
const n = new NanoDuration(2, 10, 300);
console.log(n.equal(d)); // false
console.log(d.equal(n)); // true!
```

- NanoDuration is only equal to other NanoDurations
- Duration can be equal to a NanoDuration if they have the same minutes and seconds

```
class NanoDuration extends Duration {
  // min (inherited)
  // sec (inherited)
  readonly nano: number;
  equal = (d: Duration): boolean => {
    if (d instanceof NanoDuration) {
      return this.min === d.min &&
             this.sec === d.sec &&
              this.nano === d.nano;
    } else {
      return this.min == d.min && this.sec == d.sec;
    }
  };
                                     No! It lacks transitivity
```

– fixes symmetry! all good now?

```
const n1 = new NanoDuration(2, 10, 300);
const d = new Duration(2, 10);
const n2 = new NanoDuration(2, 10, 400);
```

console.log(n1.equal(d)); // true
console.log(d.equal(n2)); // true
console.log(n1.equal(n2)); // false!

- transitivity requires n1 to equal n2 (but it doesn't)

Subclasses and Equals Don't Always Mix

- No good solution to this problem!
 - inherent tension between subtyping and equality
 subtyping wants subclasses to behave the same
 equality wants to treat them differently (using extra information)
- This is a general problem for "binary operations"
 - equality is just one example
- Real issue may be that NanoDuration isn't a subtype
 - subclass does not mean subtype
 - (would have seen this if we documented the ADT properly)

Suppose a subclass also measures nanoseconds

- Abstract states of the two types are different
 - time in seconds vs nanoseconds
 - abstract states of subtypes would need to be subtypes

Constructors

- Most Java classes have public constructors
 - e.g., create an ArrayList with "new ArrayList<String>()"
- For our ADTs, we didn't do this
 - class was hidden (not exported)
 - we exported a "factory function" that used the constructor
 e.g., makeSortedNumberSet
 - this was not accidental...
- Constructors have undesirable properties
 - surprisingly error-prone
 - several important limitations

Recall: Tight Coupling (Example 3)

```
class WorkList {
    // RI: len(names) = len(times) and total = sum(times)
    protected ArrayList<String> names;
    protected ArrayList<Integer> times;
    protected int total;

    public addWork(Job job) {
        int time = job.getTime(); // just one call
        total += time;
        addToLists(job.getName(), time);
    }
}
```

RI is not true in method call!

Method Calls from Constructors

- Any method call from a constructor is dangerous!
- Almost always calling with RI false
 - usually, the RI does not hold until all fields are assigned typically, that is the last line of the constructor
 - hence, any methods are called with the RI still false
- Asking for trouble!
 - method needs to know that some parts of RI may be false
 - eventually, someone changing code will mess this up
 - better to avoid method calls in the constructor

- Constructor is called *after* the object is created
 - can't decide, in the constructor, not to create it
- Limitations of constructors
 - **1.** Cannot return an existing object
 - 2. Cannot return a different class
 - 3. Does not have a name!

- Factory functions <u>can</u> return an existing object
- Common case: there is only one instance!
 - factory function can avoid creating new objects each time
 - called the "singleton" design pattern
- Example from HW5...

// @returns ColorList containing all known colors
export const makeSimpleColorList = (): ColorList => {
 return new SimpleColorList(COLORS);
}

- every object returned is the same
- no need to make more than one

```
const simpleColorList = new SimpleColorList(COLORS);
// @returns ColorList containing all known colors
export const makeSimpleColorList = (): ColorList => {
   return simpleColorList;
}
```

Note: only allowed because SimpleColorList is immutable

Returning a Subtype

- Factory functions <u>can</u> return a subtype
 - declared to return A but returns subtype B instead
 - allowed since every B is an A

• Example:

```
// @returns an empty NumberSet that can be used to
// store numbers between min and max (inclusive)
const makeNumberSet = (min: number, max: number): NumberSet => {
    if (0 <= min && max <= 100) {
        return makeArrayNumberSet(); // only supports small sets
    } else {
        return makeSortedNumberSet(); // use a tree instead
    }
}</pre>
```

Java classes allow multiple constructors

```
class HashMap {
  public HashMap() { ... } // initial capacity of 16
  public HashMap(int initialCapacity) { ... }
}
```

• TypeScript classes do not, but you can fake it with *optional* arguments

```
class HashMap {
  constructor(initialCapacity?: number) { ... }
}
```

Constructors Have No Name

- Do not get to name constructors
 - in Java, same name as the class
 - in TypeScript, called "constructor"
- Names are useful
 - 1. Let you <u>distinguish</u> between different cases
 - use names to distinguish cases that otherwise look the same
 - 2. Let you explain what it does
 - the only thing you know the client will read!

Example: Distinguishing Constructors

JavaScript's Array has multiple constructors

new Array() // creates []
new Array(a1, ..., aN) // creates [a1, ..., aN]
new Array(2) // creates [undefined, undefined]

- what does "new Array(a1)" return when a1 is a number?
- how to make a 1-element array containing just a1

```
const A = new Array(1);
A[0] = a1;
```

- don't have a name to distinguish these cases!

Example: Distinguishing Constructors

- Factory Functions have names
 - allow us to distinguish these cases

```
// @returns []
const makeEmptyArray = (): Array => { ... };
// @returns A with A.length = len and
// A[j] = undefined for any 0 <= j < len
const makeArray = (len: number): Array => { ... };
```

// @returns [args[0], ..., args[N-1]]
const makeArrayContaining = (...): Array => { ... };

Example: Distinguishing Constructors

- Factory Functions have names
 - allow us to distinguish these cases

```
// @returns []
const makeEmptyArray = (): Array => { ... };
// @returns A with A.length = len and
// A[j] = undefined for any 0 <= j < len
const makeArray = (len: number): Array => { ... };
// @returns A with A.length = len and
// A[j] = val for any 0 \le j \le len
const makeFilledArray =
    (len: number, val: number): Array => { ... };
          Be very, very careful...
```

Type checker won't notice if client mixes these up!

- Some famous bugs due to mixing up argument order!
- If you program long enough, you will see this one
 - ... and just about every other bug



Junior dev: "I f dev up bad, I'm so fired"

Senior dev: "I have 3 production outages named after me lol"

6:48 PM · Jan 12, 2022

Use Records to Force Call-By-Name

Can use a record to make clients type names

// @returns A with A.length = len and // A[j] = val for any 0 <= j < len const makeFilledArray = (desc: {len: number, value: number}): Array

- takes one argument, not two
- client writes "makeFilledArray({len: 3, value: 0})"
- Think about mistakes clients might make
 - be paranoid when debugging will be painful