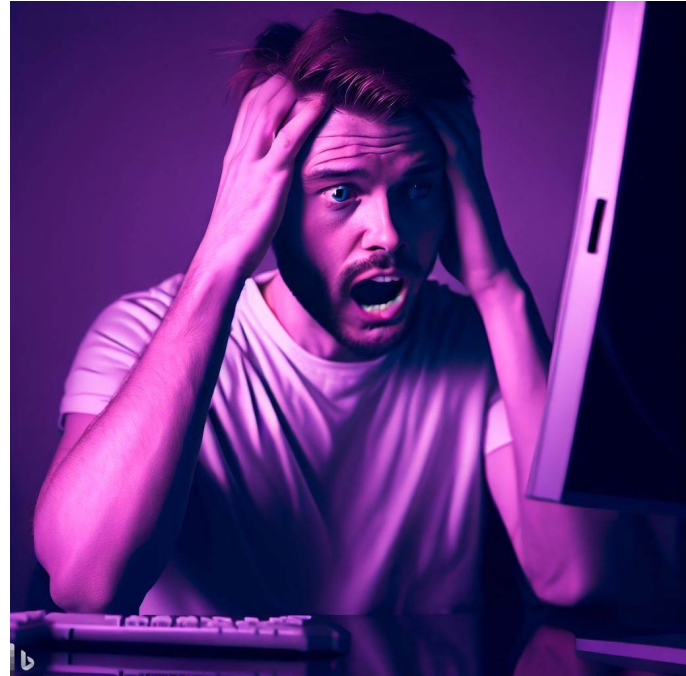


CSE 331

Aliasing

Kevin Zatloukal



HW9 Reminders

- **HW9 released last night**
 - another debugging assignment
 - make sure you **understand** all the pieces
- **HW9 is individual (not group) work**
 - will compare solutions for similarity
 - only person you can copy from is me (e.g., Auctions)
- **Tests your knowledge of lecture content**
 - not knowledge of libraries
 - **linter** to updated to further exclude non-331 code

Revisiting HW5

- In HW5, color information in a `ColorInfo` record
 - we used a triple, but a record also works

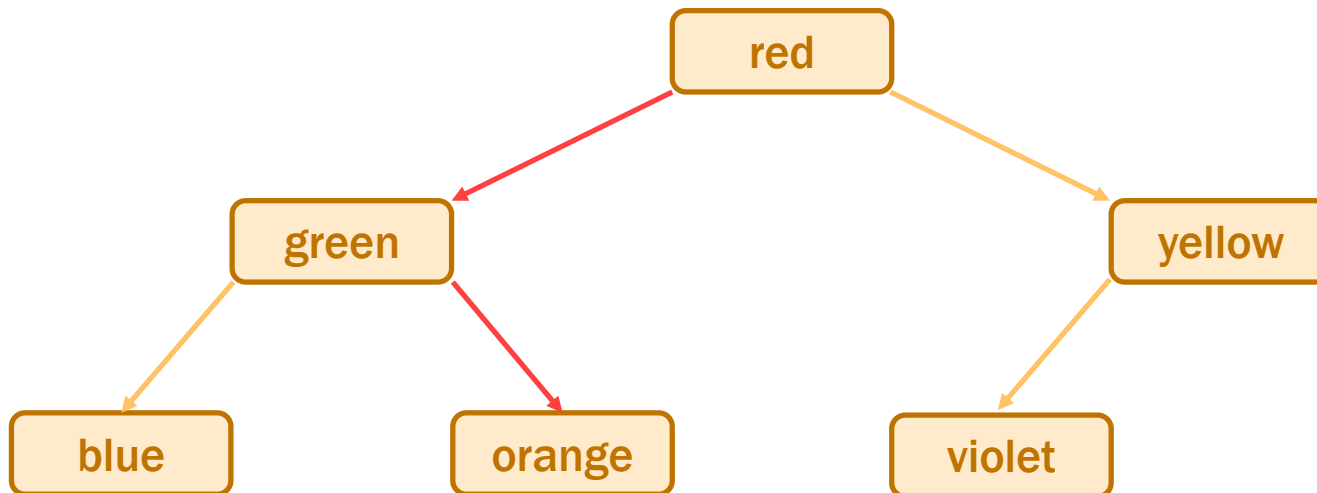
```
type ColorInfo = {  
    name: string, cssColor: string, dark: boolean};
```

- Could also write functions that mutate them:

```
const makeFavColor = (c: ColorInfo): ColorInfo => {  
    c.name = "pink";  
    c.cssColor = "#FFC0CB";  
    c.dark = false;  
    return c;  
};
```

Revisiting HW5

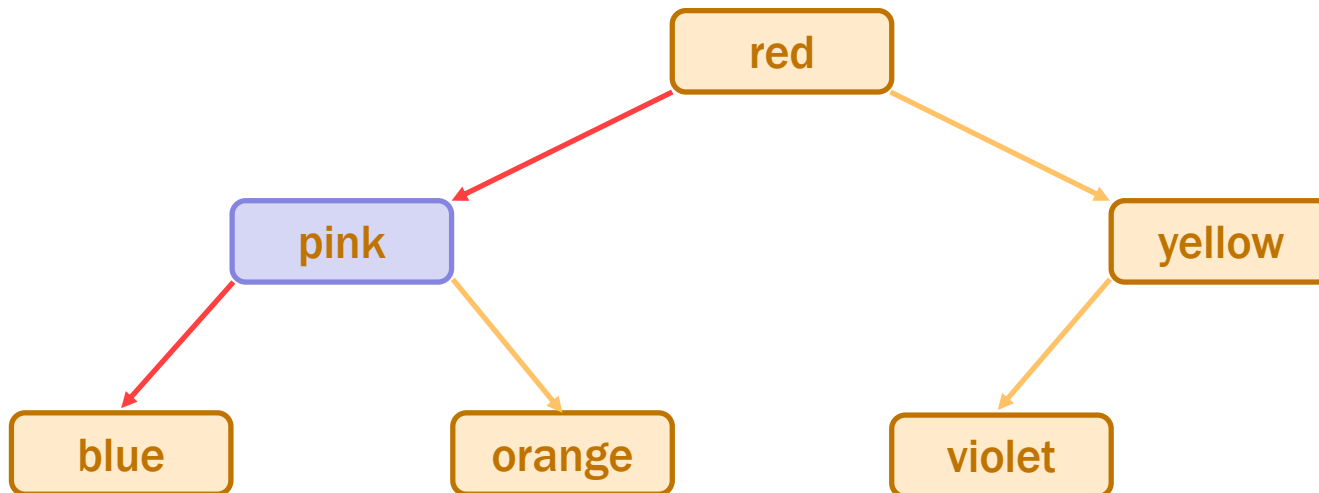
- In HW5, we had a **BST of ColorInfo records**
 - faster way to look up color information
 - e.g., find orange like this



- Suppose we called `makeFavColor` on the green record...

Revisiting HW5

- **Suppose we called `makeFavColor` on green record...**
 - it is mutated into pink
 - now this happens when we look for orange:



- **it can no longer be found!**
we violated the BST invariant

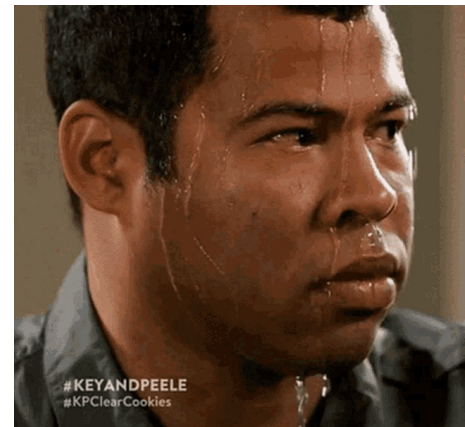
Revisiting HW5

- In HW5, color information in a `ColorInfo` record
 - we used a triple, but a record also works

```
type ColorInfo = {  
    name: string, cssColor: string, dark: boolean};
```

- Could also write functions that mutate them:

```
const makeFavColor = (c: ColorInfo): ColorInfo => {  
    c.name = "pink";  
    c.cssColor = "#FFC0CB";  
    c.dark = false;  
    return c;  
};
```



Scary Bugs

- **Do not fear crashes**
 - those are easy to spot and fix
 - get a stack trace that tells you exactly where it went wrong
- **Do fear unexpected mutation**
 - failure will give you no clue what went wrong
 - will take a long time to realize the BST invariant was violated by mutation
 - bug could be almost anywhere in the code
 - anyone who mutates a `ColorInfo` could have caused it
 - could take *weeks* to track it down

Recall: Correctness Levels

Level	Description	Testing	Tools	Reasoning
-1	small # of inputs	exhaustive		
0	straight from spec	heuristics	type checking	code reviews
1	no mutation	“	libraries	calculation induction
2	local variable mutation	“	“	Floyd logic
3	array / object mutation	“	“	rep invariants

Level 3: Mutable Heap State

- “With great power, comes great responsibility”
- **With arrays:**
 - gain the ability to easily access any element
 - must keep track of information about the whole array
- **Additional references to the same object are “aliases”**
- **With mutable heap state:**
 - gain efficiency in some cases
 - must keep track of every alias that could mutate that state
 - any alias, anywhere in the *entire* program could cause a bug

Easy Ways to Stay Safe

1. Do not use mutable state

- don't need to think about aliasing at all
- any number of aliases is fine

2. a) Do not hand out aliases

- never give anyone else an alias
- create the state in your constructor and don't share it:

```
class MyClass {  
    vals: Array<string>;  
  
    constructor() {  
        this.vals = new Array(0); // only alias  
    }  
    ...  
}
```

Easy Ways to Stay Safe

1. Do not use mutable state

- don't need to think about aliasing at all
- any number of aliases is fine

2. a) Do not hand out aliases

only one reference to an object
(no aliases)

- never give anyone else an alias
- create the state in your constructor and don't share it

b) Make a copy of anything you want to keep

- you have the only reference to the newly created copy
- does not matter if the caller later mutates the original

An Advanced (Two-Stage) Approach

- **Mutable object has only one reference (**owner**)**
 - one reference that is allowed to use & mutate it
- **Must track ownership of each mutable object**
 - can be passed in a function call
 - passed permanently or just “borrowed”
 - borrowing returns ownership back when the call ends
 - Rust programming language has built-in support for this type system ensures that there is only one owner
- **Object can be “frozen”, making it immutable**
 - no longer necessary to track ownership

Mutable ADTs

ADTs

- **Main place we have heap state is in an ADT**
- **Previously:**
 - **state was immutable**
 - **set in the constructor and then never changed**
 - only need to confirm RI holds at the end of the constructor
 - if RI holds there, then it holds forever
- **Now:**
 - **allow state to be changed by methods**

ADTs

- **Main place we have heap state is in an ADT**
- **New Power:**
 - allow state to be changed by methods
- **New Responsibilities:**
 - **more complex specifications**
add `@effects` and `@modifies`
 - **must check the RI holds after any method that mutates**
often a good idea to write code to check this at runtime
 - **must avoid aliasing of anything mutable**
we call this “representation exposure”

Recall: List ADT with a Fast getLast

```
// Represents an (immutable) list of numbers.
interface FastList {

    // @returns cons(x, obj)
    cons: (x: number) => FastList;

    // @returns last(obj)
    getLast: () => number | undefined;

    // @returns obj
    toList: () => List<number>;
};

const makeFastList = (): FastList => {
    return new FastListImpl(nil);
};
```

producer method

Mutable List ADT with a Fast `getLast`

```
// Represents a mutable list of numbers.
interface MutableFastList {

    // @modifies obj
    // @effects obj = cons(x, obj_0)          mutator method
    cons: (x: number) => void;
    ...
}
```

- **Method `cons` changes the list, putting `x` in front**
 - now returns `void`
 - mutation explained in `@modifies` and `@effects`
abstract state is the old abstract state with `x` put in front

Mutable List ADT with a Fast `getLast`

```
// Represents a mutable list of numbers.
interface MutableFastList {

    // @modifies obj
    // @effects obj = cons(x, obj_0)          mutator method
    cons: (x: number) => void;
    ...
}
```

- **Method `cons` changes the list, putting `x` in front**
 - **now a mutable data type**
 - clients need to worry about aliasing
 - **don't make a tree of these!**
 - some languages (e.g., Python) don't allow this

Recall: One Concrete Rep for FastList

```
class FastListImpl implements FastList {
  // RI: this.last = last(this.list)
  // AF: obj = this.list
  readonly last: number | undefined;
  readonly list: List<number>;

  constructor(list: List<number>) {
    this.list = list;
    this.last = last(this.list);
  }
}
```

- We can use the same rep for a mutable version

Mutable List ADT with a Fast getLast

```
class MutableFastListImpl implements MutableFastList {
  // RI: this.last = last(this.list)
  // AF: obj = this.list
  last: number | undefined;
  list: List<number>;

  // @modifies obj
  // @effects obj = cons(x, obj_0)
  cons = (x: number): void => {
    this.list = cons(x, this.list);
  };
}
```

- Let's check correctness...

Mutable List ADT with a Fast getLast

```
class MutableFastListImpl implements MutableFastList {
  // RI: this.last = last(this.list)
  // AF: obj = this.list
  last: number | undefined;
  list: List<number>;

  // @modifies obj
  // @effects obj = cons(x, obj_0)
  cons = (x: number): void => {
    ↓ this.list = cons(x, this.list);
    {{ this.list = cons(x, this.list0) }}
    ↑ {{ Post: obj = cons(x, obj0) }}
  };
}
```

Mutable List ADT with a Fast getLast

```
class MutableFastListImpl implements MutableFastList {
  // RI: this.last = last(this.list)
  // AF: obj = this.list
  last: number | undefined;
  list: List<number>;

  // @modifies obj
  // @effects obj = cons(x, obj_0)
  cons = (x: number): void => {
    this.list = cons(x, this.list);
    {{ this.list = cons(x, this.list0) }}
    {{ Post: obj = cons(x, obj0) }}
  };
```

What is missing?

Also, need the RI to hold!

obj = this.list
= cons(x, this.list₀)
= cons(x, obj₀)

by AF
since this.list = cons(x, this.list₀)
by AF

Mutable List ADT with a Fast getLast

```
class MutableFastListImpl implements MutableFastList {
  // RI: this.last = last(this.list)
  // AF: obj = this.list
  last: number | undefined;
  list: List<number>;

  // @modifies obj
  // @effects obj = cons(x, obj_0)
  cons = (x: number): void => {
    this.list = cons(x, this.list);
    {{ this.list = cons(x, this.list_0) }}
    {{ Post: obj = cons(x, obj_0) and
      this.last = last(this.list) }}
  };
```

Also, need the RI to hold!

Does it? No!

- Postcondition is @returns, @effects, and RI

Mutable List ADT with a Fast getLast

```
class MutableFastListImpl implements MutableFastList {
    // RI: this.last = last(this.list)
    // AF: obj = this.list
    last: number | undefined;
    list: List<number>;

    // @modifies obj
    // @effects obj = cons(x, obj_0)
    cons = (x: number): void => {
        this.list = cons(x, this.list);
        this.last = last(this.list);
        {{ this.list = cons(x, this.list0) and this.last = last(this.list) }}
        {{ Post: obj = cons(x, obj0) and this.last = last(this.list) }}
    };
}
```

Rep Invariant now holds

Mutable List ADT with a Fast getLast

```
class MutableFastListImpl implements MutableFastList {
  // RI: this.last = last(this.list)
  // AF: obj = this.list
  last: number | undefined;
  list: List<number>;

  // @modifies obj
  // @effects obj = cons(x, obj_0)
  cons = (x: number): void => {
    this.last = last(this.list);
    {{ this.last = last(this.list) }}
    this.list = cons(x, this.list);
    {{ this.list = cons(x, this.list0) and this.last = last(this.list0) }}
    {{ Post: obj = cons(x, obj0) and this.last = last(this.list) }}
  };
}
```

Rep Invariant would not hold if we switched the order

Mutable List ADT with a Fast `getLast`

```
class MutableFastListImpl implements MutableFastList {
    // RI: this.last = last(this.list)
    // AF: obj = this.list
    last: number | undefined;
    list: List<number>;

    // @modifies obj
    // @effects obj = cons(x, obj_0)
    cons = (x: number): void => {
        this.list = cons(x, this.list);
        this.last = last(this.list);
        {{ this.list = cons(x, this.list0) and this.last = last(this.list) }}
        {{ Post: obj = cons(x, obj0) and this.last = last(this.list) }}
    };
}
```

This version is obviously correct, but $O(n)$.

Can we do it faster?

Mutable List ADT with a Fast getLast

```
class MutableFastListImpl implements MutableFastList {
  // RI: this.last = last(this.list)
  // AF: obj = this.list
  last: number | undefined;
  list: List<number>;

  // @modifies obj
  // @effects obj = cons(x, obj_0)
  cons = (x: number): void => {
    if (this.list === nil)
      this.last = x;
    this.list = cons(x, this.list);
    {{ _____ }}
    {{ Post: obj = cons(x, obj_0) and this.last = last(this.list) }}
  };
}
```

O(1) version, but more complex reasoning (two branches)

Mutable List ADT with a Fast `getLast`

```
class MutableFastListImpl implements MutableFastList {  
    cons = (x: number): void => {  
        if (this.list === nil)  
            this.last = x;  
        this.list = cons(x, this.list);  
        {{ this.list = cons(x, this.list0) and this.list0 = nil and this.last = x }}  
        {{ Post: obj = cons(x, obj0) and this.last = last(this.list) }}  
    };  
}
```

Case “then”:

$\text{last}(\text{this.list}) = \text{last}(\text{cons}(x, \text{this.list}_0))$
 $= \text{last}(\text{cons}(x, \text{nil}))$
 $= x$
 $= \text{this.last}$

since $\text{this.list} = \text{cons}(x, \dots)$
since $\text{this.list}_0 = \text{nil}$
def of last
since $x = \text{this.last}$

Mutable List ADT with a Fast `getLast`

```
class MutableFastListImpl implements MutableFastList {  
  cons = (x: number): void => {  
    if (this.list === nil)  
      this.last = x;  
    this.list = cons(x, this.list);  
    {{ this.list = cons(x, this.list0) and this.list0 ≠ nil and this.last = this.last0 }}  
    {{ Post: obj = cons(x, obj0) and this.last = last(this.list) }}  
  };  
}
```

Case “else”:

$\text{last}(\text{this.list}) = \text{last}(\text{cons}(x, \text{this.list}_0))$	since $\text{this.list} = \text{cons}(x, \dots)$
$= \text{last}(\text{this.list}_0)$	since $\text{this.list}_0 \neq \text{nil}$
$= \text{this.last}_0$	by RI
$= \text{this.last}$	since $\text{this.last} = \text{this.last}_0$

Moral of the Story for Level 3

- **More mutation gave us better efficiency**
 - saved memory
 - immutable version could be just as fast (level 1)
- **More mutation means more complex reasoning**
 - more facts to keep track of
 - more ways to make mistakes
 - more work to make sure we did it right

Recall: Immutable Queue ADT

- A queue is a list that can *only* be changed two ways:
 - add elements to the front
 - remove elements from the back

```
// List that only supports adding to the front and
// removing from the end
interface NumberQueue {
  // @returns len(obj)
observer    size: () => number;

  // @returns cons(x, obj)
producer    enqueue: (x: number) => NumberQueue;

  // @requires len(obj) > 0
producer    dequeue: () => [number, NumberQueue];
}
```

Mutable Queue ADT

- Mutable versions has mutators instead of producers

```
// Mutable array that only supports adding to the front
// and removing from the end.
interface MutableNumberQueue {

    // @returns obj
observer    elements(): number[];

    // @modifies obj
mutator     // @effects obj = [x] ++ obj_0
            enqueue(x: number): void;

    // @requires len(obj) > 0
mutator     // @modifies obj
            // @effects obj_0 = obj ++ [x]
            // @returns x
            dequeue(): number;
}
```


Recall: Implementing a Queue with Two Lists

```
// Implements a queue using two lists.
class ListPairQueue implements NumberQueue {

    // AF: obj = concat(this.front, rev(this.back))
    // RI: if this.back = nil, then this.front = nil
    readonly front: List;
    readonly back: List;

    // makes obj = concat(front, rev(back))
    constructor(front: List, back: List) {
        ...
    }
}
```

- Queue was in two parts, front and back
 - back stored in reverse order
 - full list was `concat(this.front, rev(this.back))`

Implementing Mutable Queue with Two Arrays

```
// Implements a mutable queue using two arrays.
class ArrayPairQueue implements MutableNumberQueue {

    // AF: obj = rev(this.front) ++ this.back
    front: number[];
    back: number[];

    // makes obj = vals
    constructor(vals: number[]) {
        this.front = [];
        this.back = vals;
    }
}
```

We should check this...

Implementing Mutable Queue with Two Arrays

```
// Implements a mutable queue using two arrays.
class ArrayPairQueue implements MutableNumberQueue {

    // AF: obj = rev(this.front) ++ this.back
    front: number[];
    back: number[];

    // makes obj = vals
    constructor(vals: number[]) {
        this.front = [];
        this.back = vals;
        {{ this.front = [] and this.back = vals }}
        {{ Post: obj = vals }}
    }
}
```

Implementing Mutable Queue with Two Arrays

```
// Implements a mutable queue using two arrays.
class ArrayPairQueue implements MutableNumberQueue {

  // AF: obj = rev(this.front) ++ this.back
  front: number[];
  back: number[];

  // makes obj = vals
  constructor(vals: number[]) {
    this.front = [];
    this.back = vals;
    {{ this.front = [] and this.back = vals }}
    {{ Post: obj = vals }}
  }
}
```

Is this really correct?

No way to say!

obj = rev(this.front) # this.back
= rev([]) # this.back
= [] # this.back
= this.back = vals

by AF
since this.front = []
def of rev
since this.back = vals

Implementing Mutable Queue with Two Arrays

```
// Implements a mutable queue using two arrays.
class ArrayPairQueue implements MutableNumberQueue {

    // AF: obj = rev(this.front) ++ this.back
    front: number[];
    back: number[];

    // makes obj = vals
    constructor(vals: number[]) {
        this.front = [];
        this.back = vals.slice(0, vals.length);
    }
}
```

- **Must make a copy of the array!**
 - then, we have the only reference to it (no aliases)

Implementing Mutable Queue with Two Arrays

```
// Implements a mutable queue using two arrays.
class ArrayPairQueue implements MutableNumberQueue {

    // AF: obj = rev(this.front) ++ this.back
    front: number[];
    back: number[];

    // @returns obj
    elements = (): number[] => {
        let revFront: number[] =
            this.front.slice(0, this.front.length);
        revFront.reverse();
        return revFront.concat(this.back);
    };
};
```

This is $O(n)$...

We can optimize it if front = [].

rev([]) # this.back = [] # this.back = this.back

Implementing Mutable Queue with Two Arrays

```
// Implements a mutable queue using two arrays.
class ArrayPairQueue implements MutableNumberQueue {

    // AF: obj = rev(this.front) ++ this.back
    front: number[];
    back: number[];

    // @returns obj
    elements = (): number[] => {
        if (this.front.length === 0) {
            return this.back;    // O(1) when this.front = []
        } else {
            let revFront: number[] =
                this.front.slice(0, this.front.length);
            revFront.reverse();
            return revFront.concat(this.back);
        }
    };
};
```

Is this correct?

No way to say!

Implementing Mutable Queue with Two Arrays

```
// Implements a mutable queue using two arrays.
class ArrayPairQueue implements MutableNumberQueue {

    // AF: obj = rev(this.front) ++ this.back
    front: number[];
    back: number[];

    // @returns obj
    elements = (): number[] => {
        let revFront: number[] = this.front.slice(0);
        revFront.reverse();
        return revFront.concat(this.back);
    };
};
```

- Cannot return an alias to `this.back`
 - must make a copy in all cases

Avoiding Representation Exposure

- **Prevent aliasing of mutable state**
 - otherwise, code outside your class can break it
- **Options for avoiding representation exposure:**
 - 1. Use immutable types**
 - lists are immutable, so you can freely accept and return them
 - 2. Copy In, Copy Out**
 - store copies of mutable values passed to you
 - return copies of not aliases to mutable state
 - don't take their word that they haven't kept an alias
- **Professionals are untrusting about aliases**