
CSE 331

Software Design & Implementation

Spring 2022

Section 5 – Graphs, Equals and Hashcode

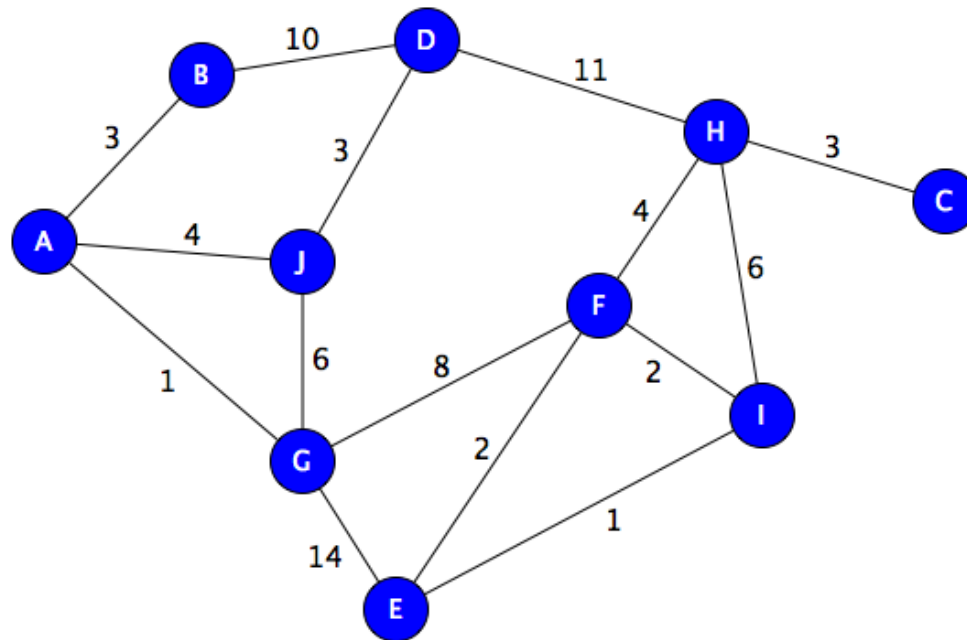
Administrivia

- HW4 due yesterday!
- HW5 out now, due next Wednesday (5/4) at 11 pm!
- Any questions?

Agenda

- Graph concepts
- HW5
- Script Testing
- Equals and Hashcode
- Extra Reasoning Practice

Graphs



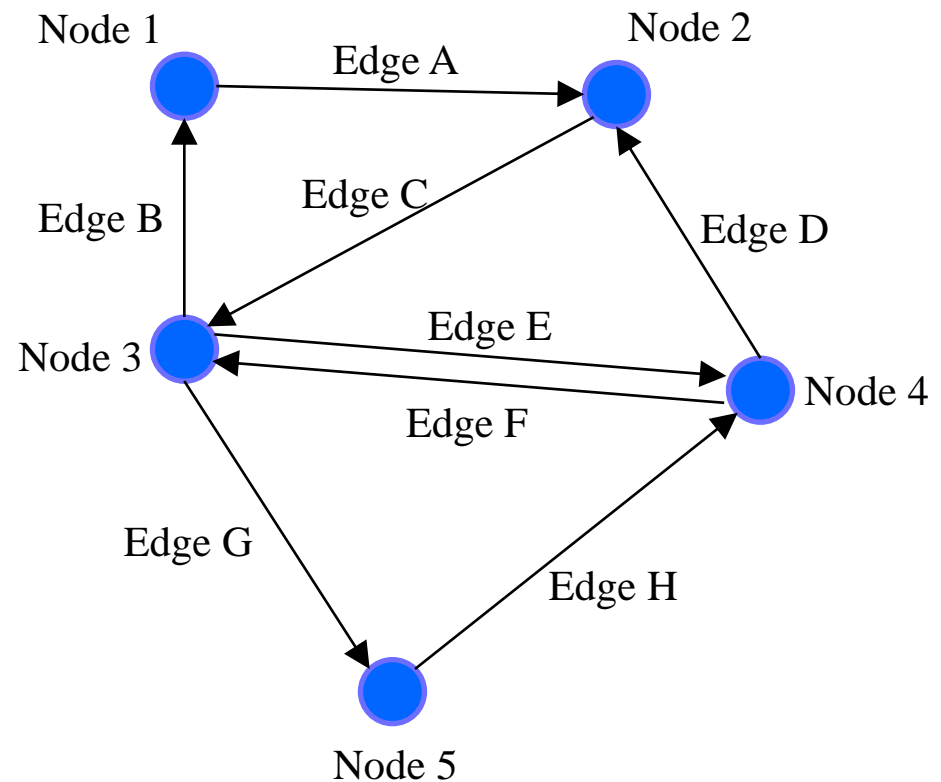
A graph represents relationships

A graph is a set of **nodes** and a set of **edges** between them.

Nodes may be **labeled**.

Edges may be **labeled**.

Edges may have a **direction**.



Example: Road Map



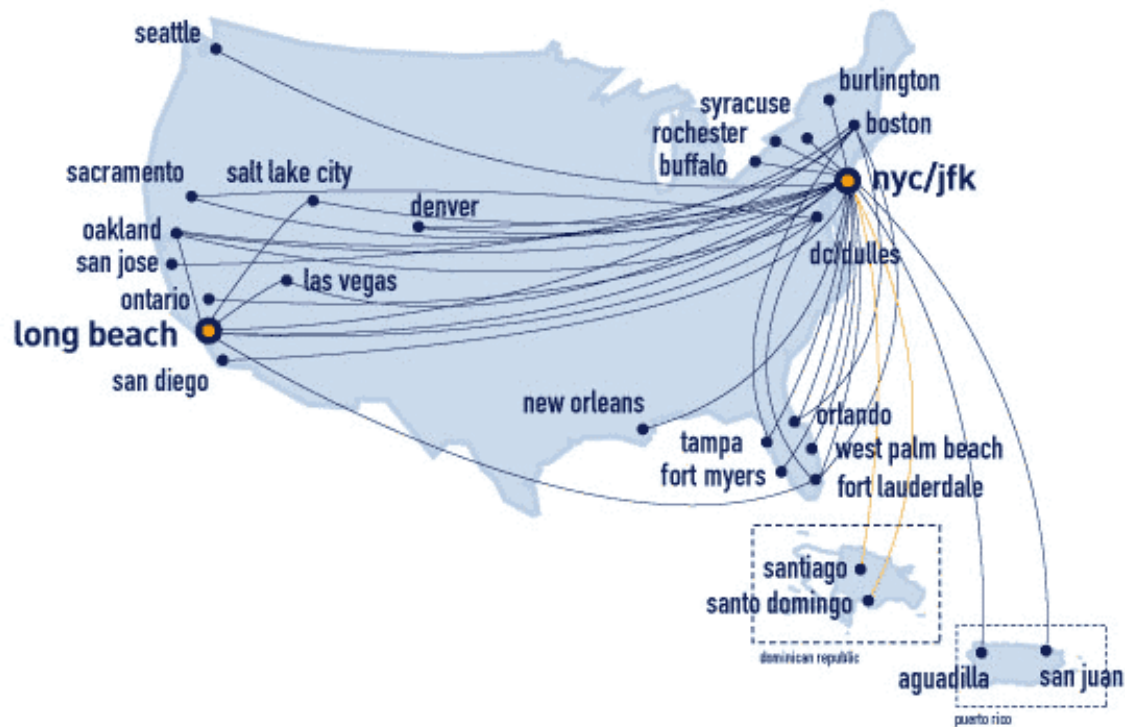
Nodes: intersections (cities)

Label: name/location

Edges: roads

Label: name/length

Example: Airline Flights



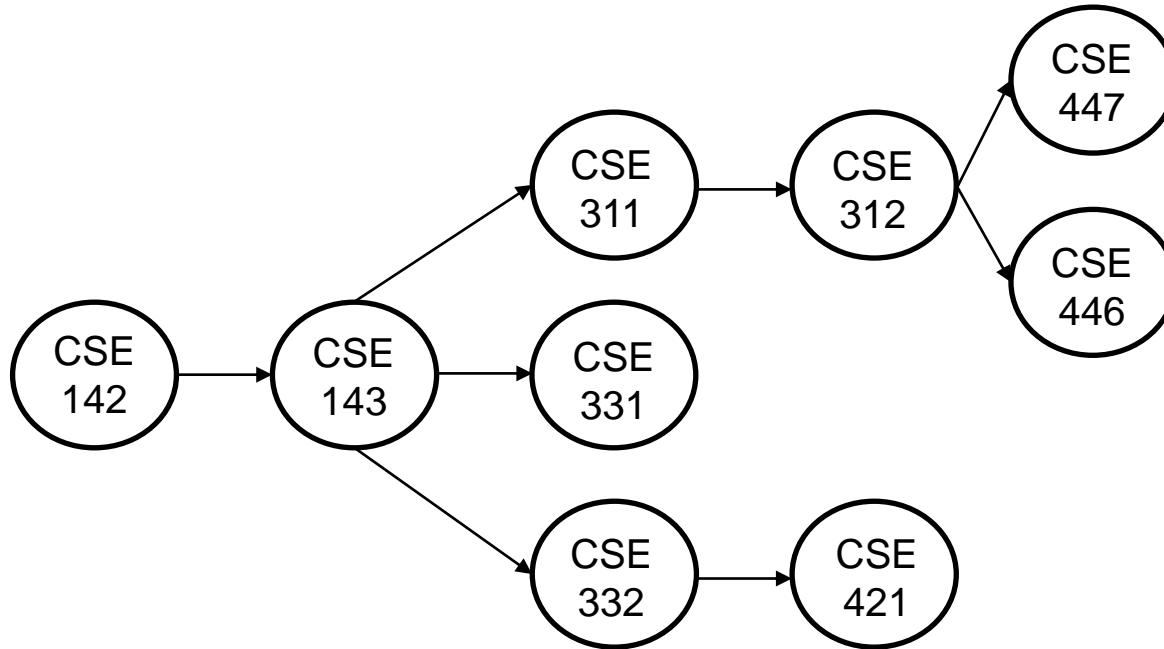
Nodes: airports

Label: airport code

Edges: flights

Label: cost/time

Example: CSE courses



Nodes: Courses

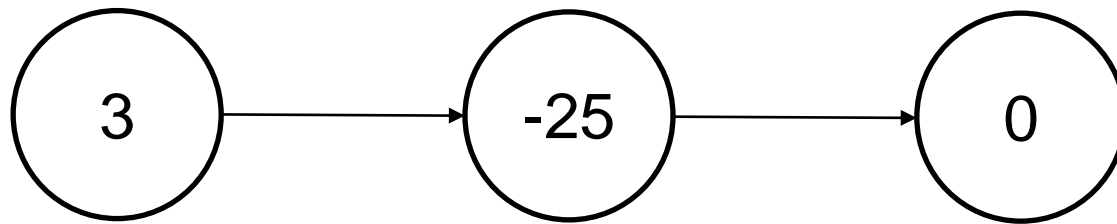
Label: Course name

Edges: pointer to next class

Label: none

You've used graphs before!

Singly linked Lists:



Nodes: Linked list node

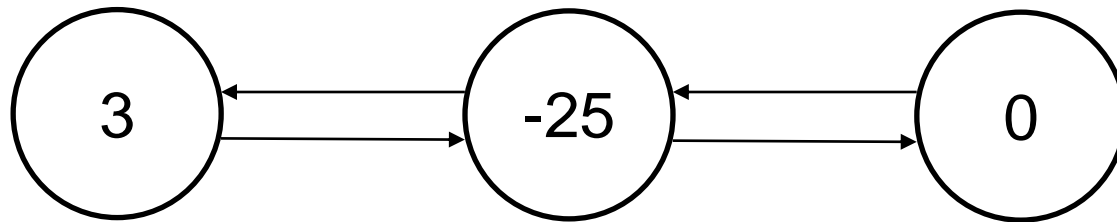
Label: integer

Edges: pointer to next node

Label: none

You've used graphs before!

Doubly linked Lists:



Nodes: Linked list node

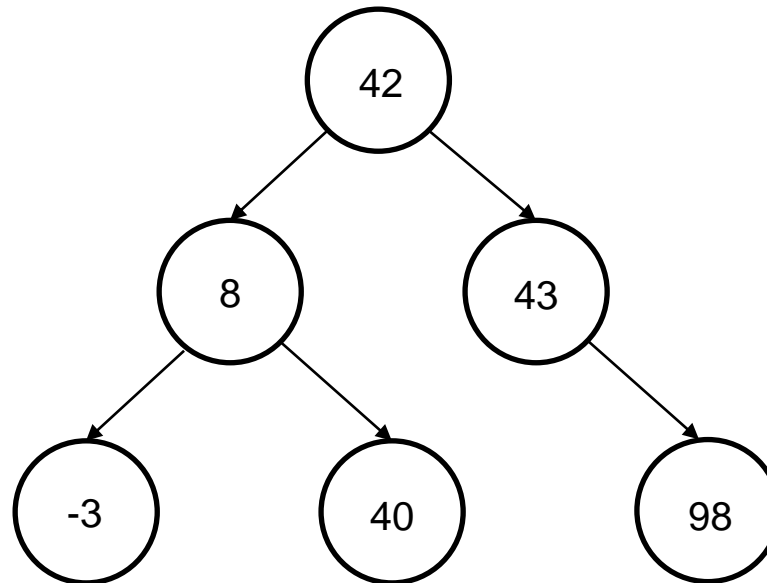
Label: integer

Edges: pointers to prev/next nodes

Label: none

You've used graphs before!

Binary trees:



Nodes: Tree node

Label: Integer

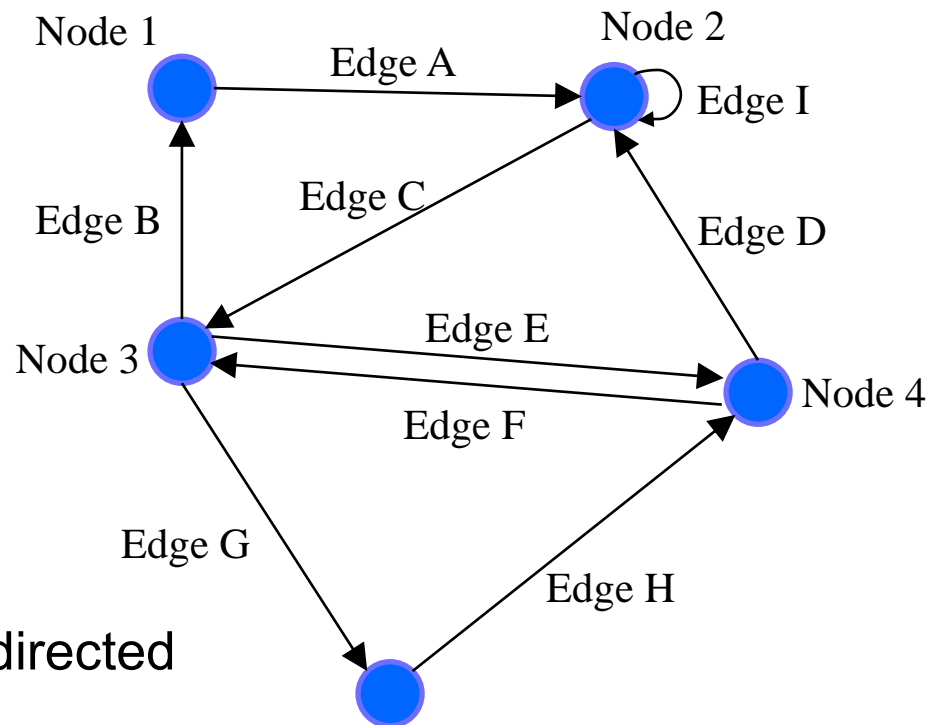
Edges: pointers to children

Label: none

An edge points from source to dest.

Each edge “points” from a **source** to a **destination**.

- **Outgoing** from **source**
- **Incoming** to **destination**



N.B.: We’re only dealing with directed graphs from here on out.

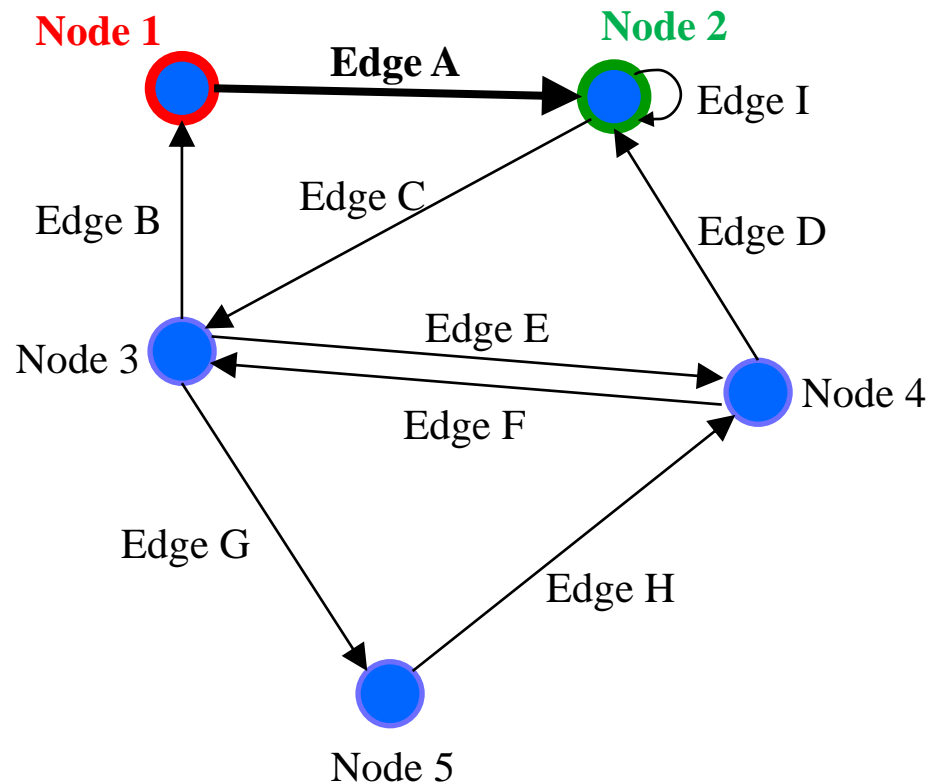
An edge points from source to dest.

Each edge “points” from a **source** to a **destination**.

- **Outgoing** from **source**
- **Incoming** to **destination**

Edge A is **Node 1** → **Node 2**.

- **Outgoing** from **Node 1**
- **Incoming** to **Node 2**



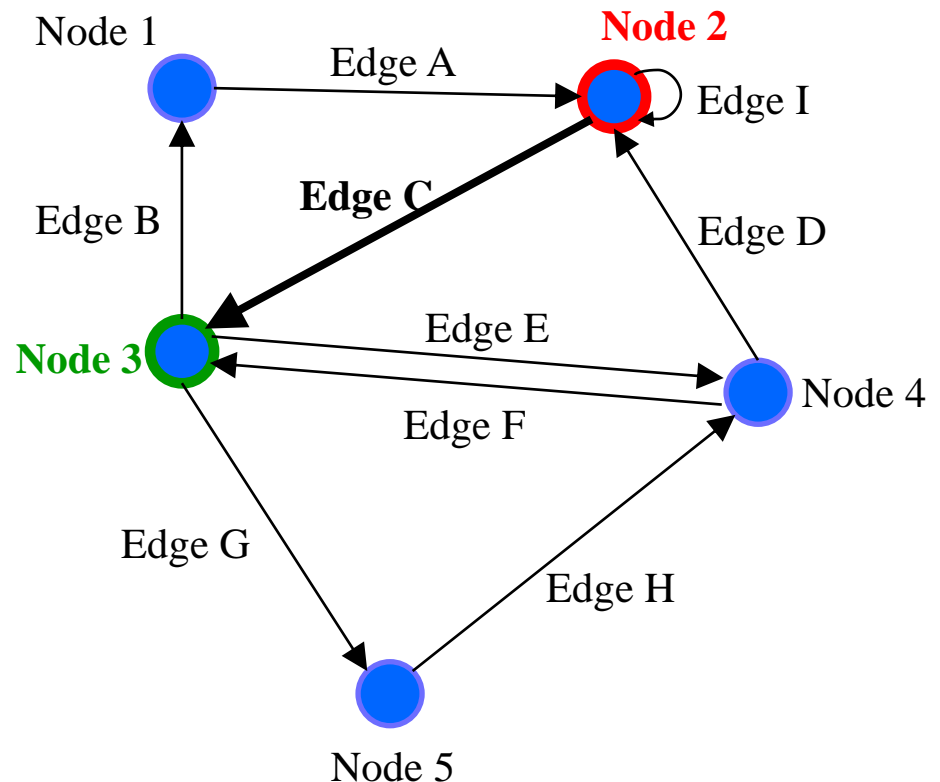
An edge points from source to dest.

Each edge “points” from a **source** to a **destination**.

- **Outgoing** from **source**
- **Incoming** to **destination**

Edge C is **Node 2** → **Node 3**.

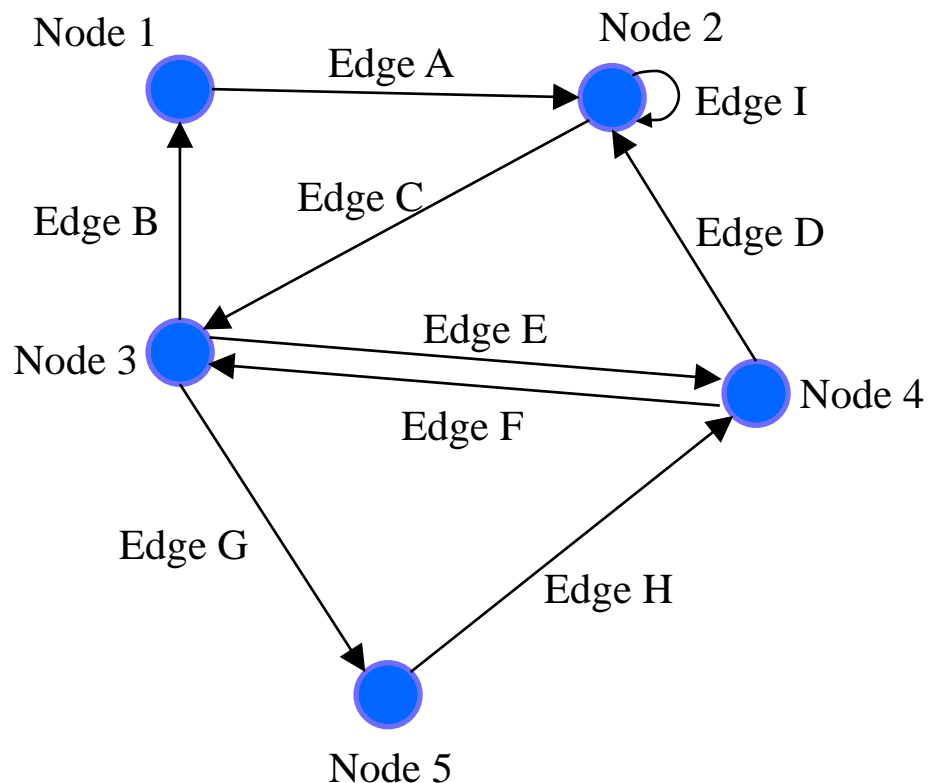
- **Outgoing** from **Node 2**
- **Incoming** to **Node 3**



A node has children

A node's outgoing edges point to its **children**.

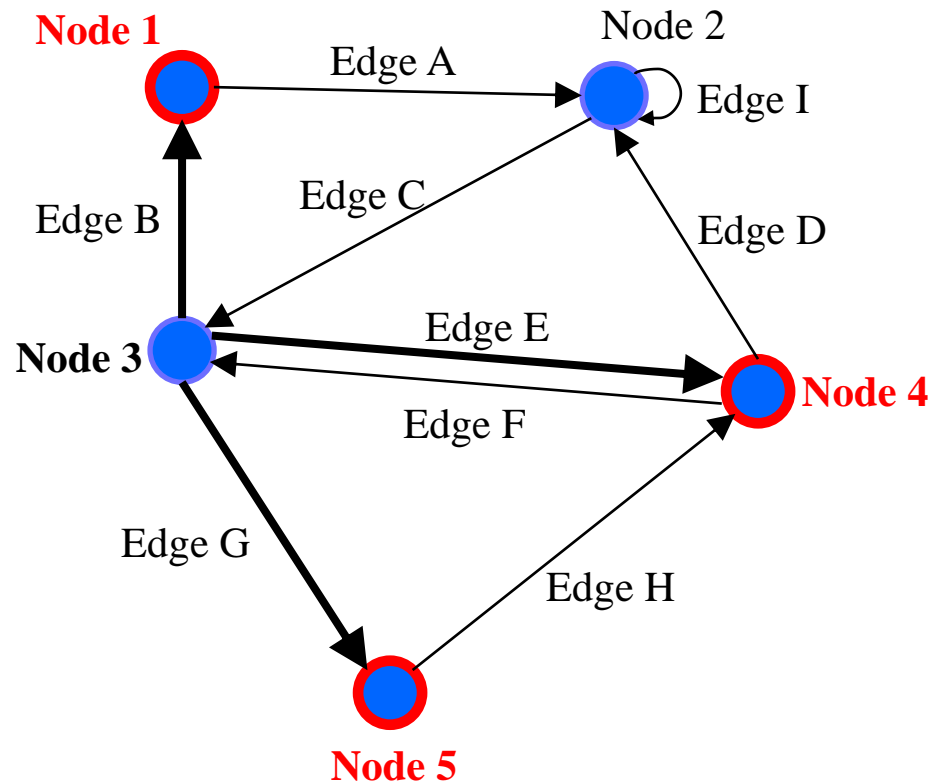
- Potentially empty set



A node has children

A node's outgoing edges point to its **children**.

- Potentially empty set



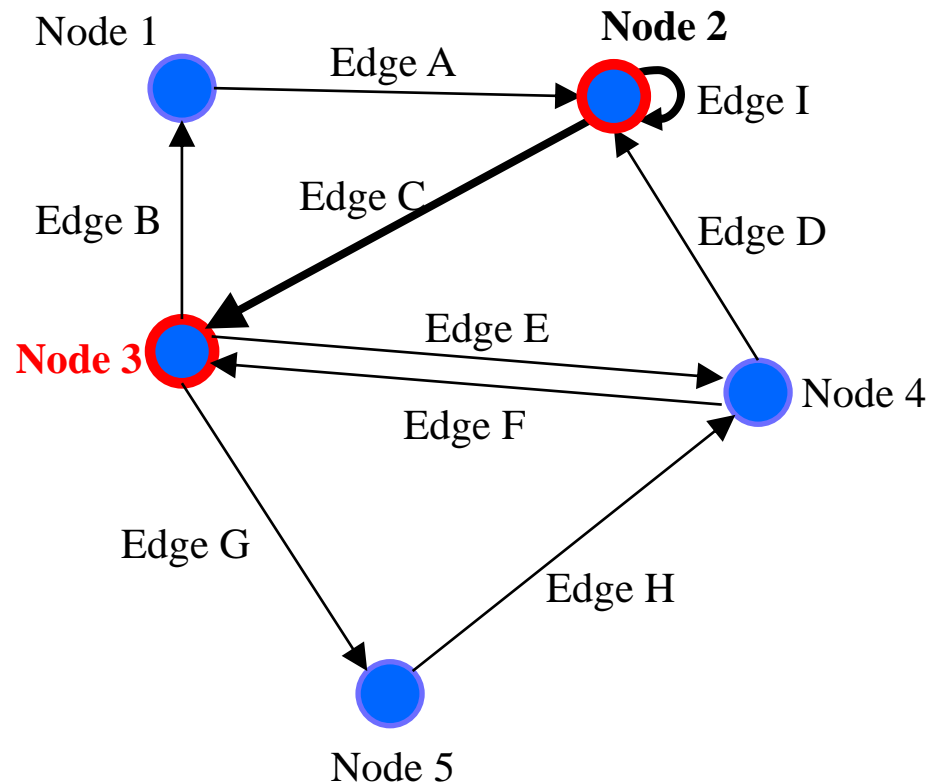
Node 3 has three children:

- Node 1
- Node 4
- Node 5

A node has children

A node's outgoing edges point to its **children**.

- Potentially empty set



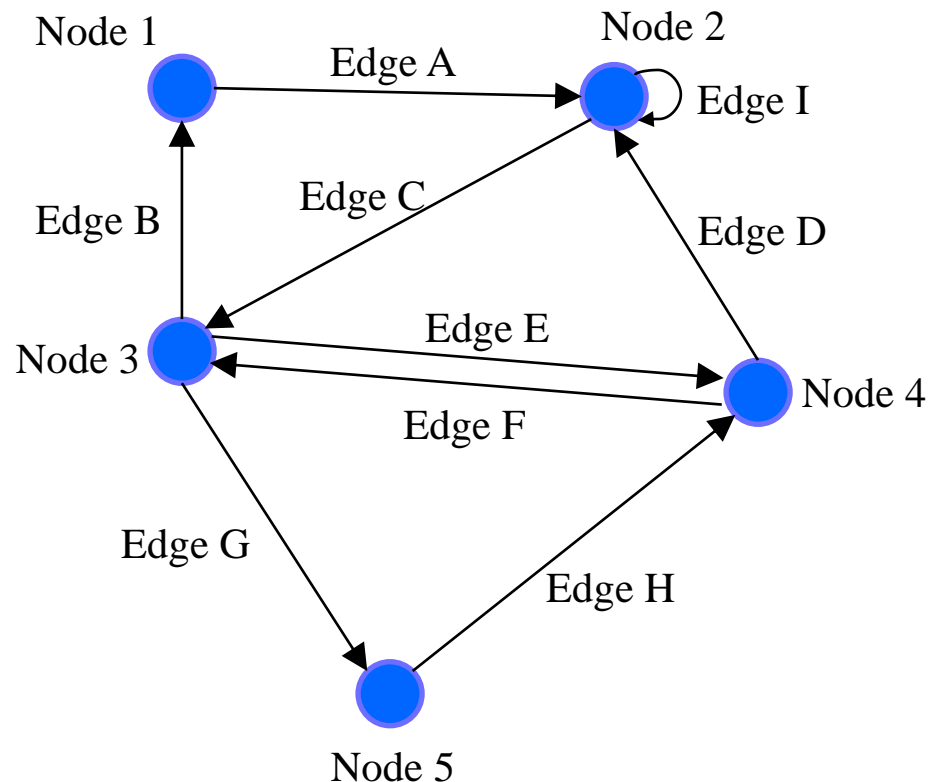
Node 2 has two children:

- Node 2
- Node 3

A node has parents

A node's incoming edges point from its **parents**.

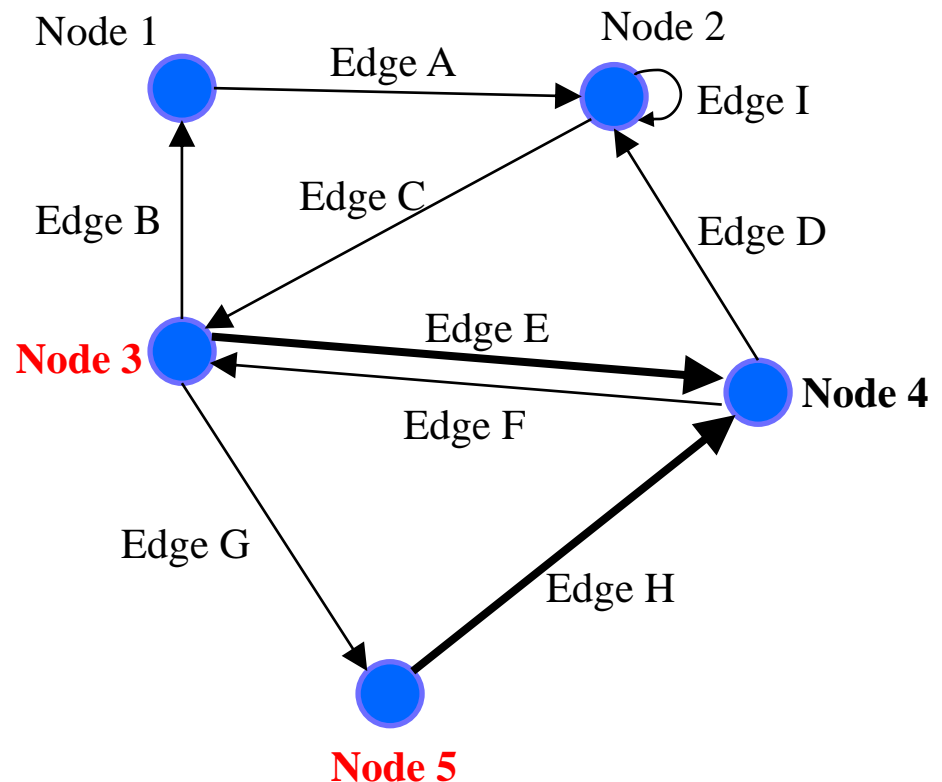
- Potentially empty set



A node has parents

A node's incoming edges point from its **parents**.

- Potentially empty set



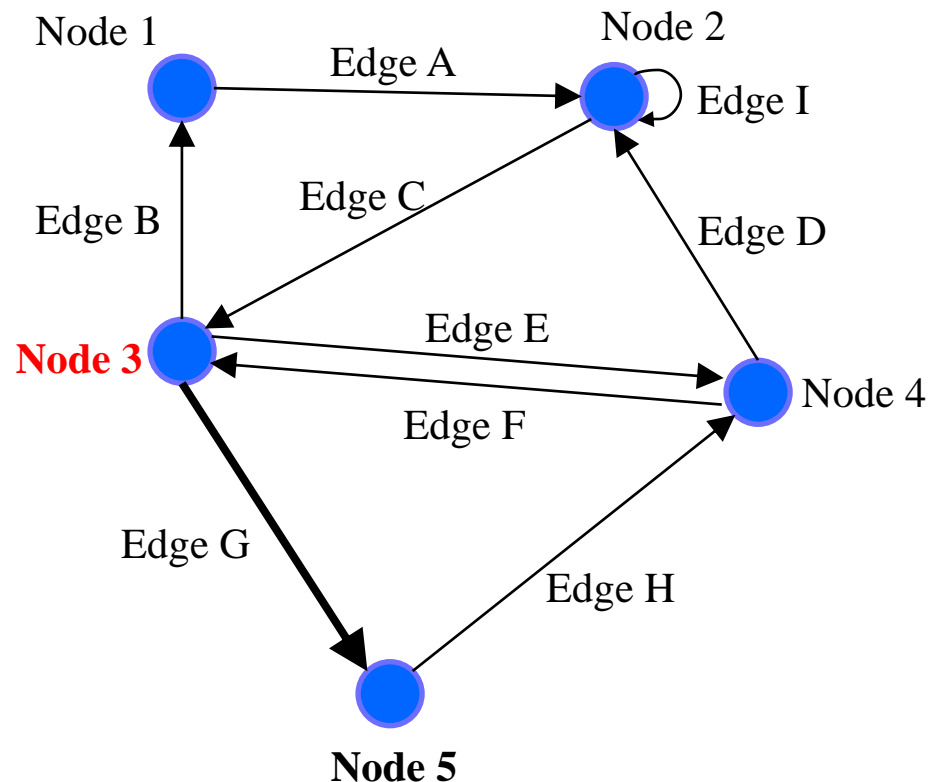
Node 4 has two parents:

- Node 3
- Node 5

A node has parents

A node's incoming edges point from its **parents**.

- Potentially empty set



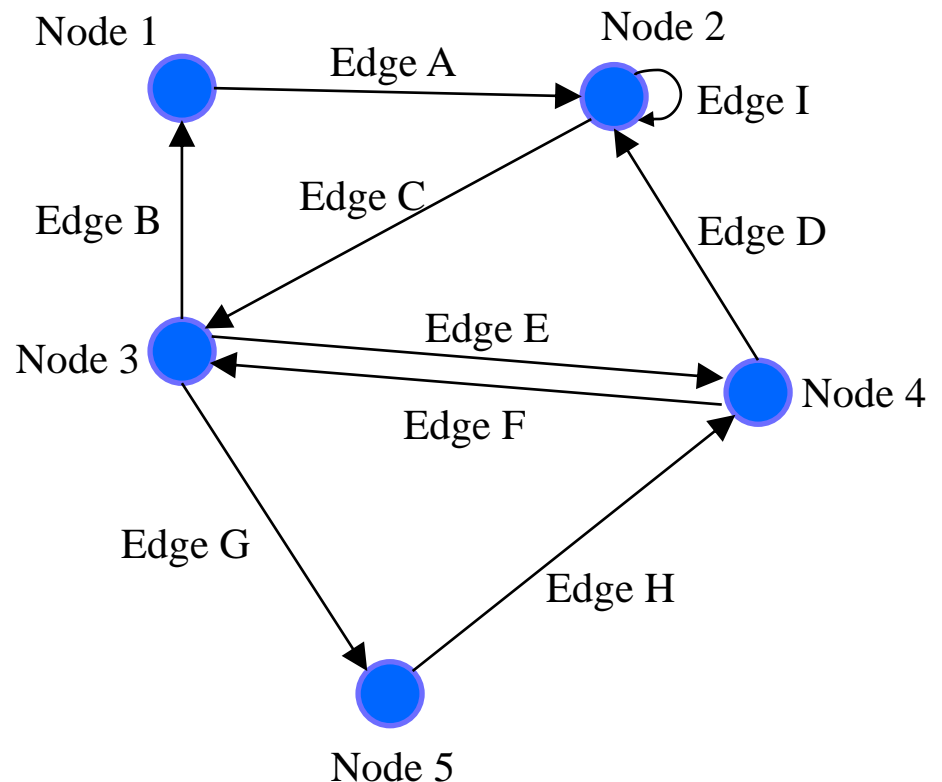
Node 5 has one parent:

- **Node 3**

A node has neighbors

A node's **neighbors** are its children plus its parents.

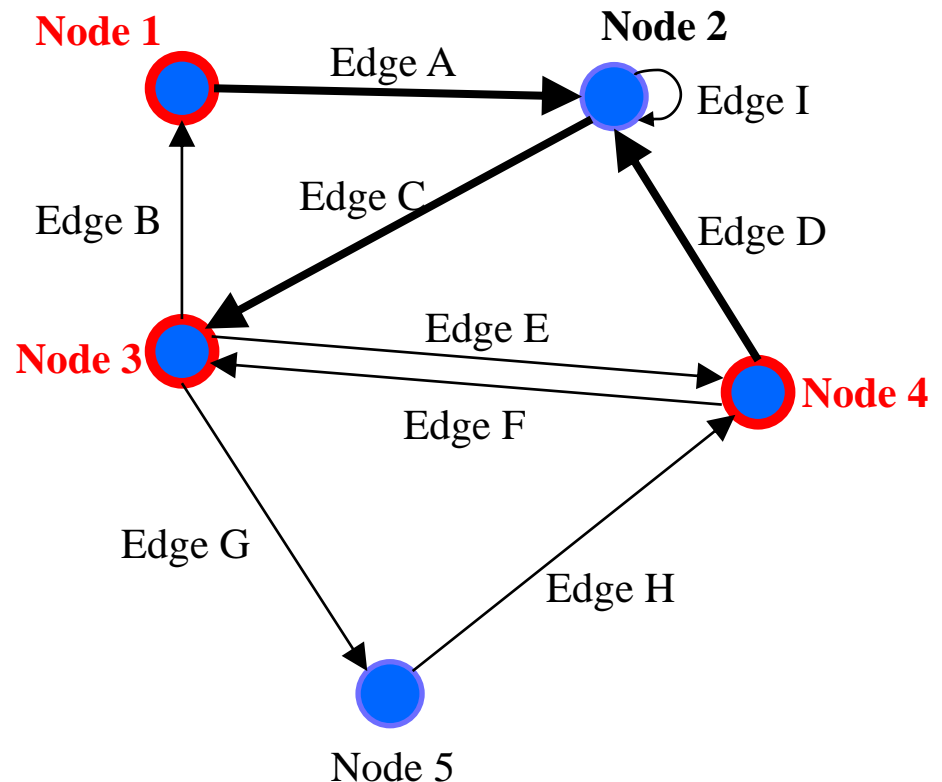
- Potentially empty set



A node has neighbors

A node's **neighbors** are its children plus its parents.

- Potentially empty set



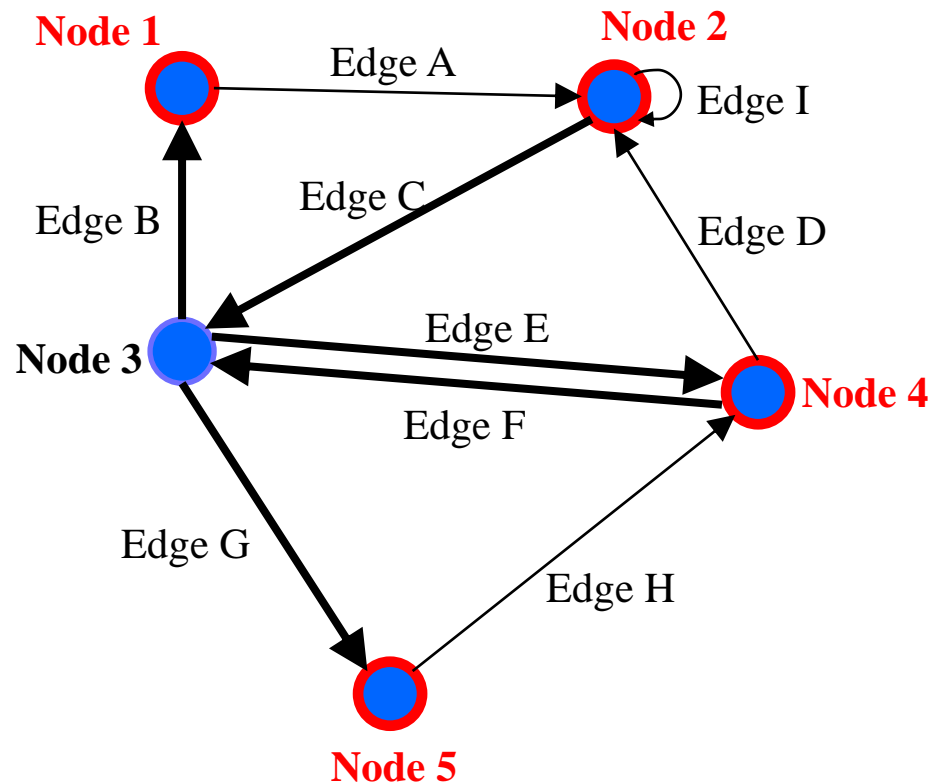
Node 2 has four neighbors:

- **Node 1** (parent)
- **Node 2** (self-pointing)
- **Node 3** (child)
- **Node 4** (parent)

A node has neighbors

A node's **neighbors** are its children plus its parents.

- Potentially empty set



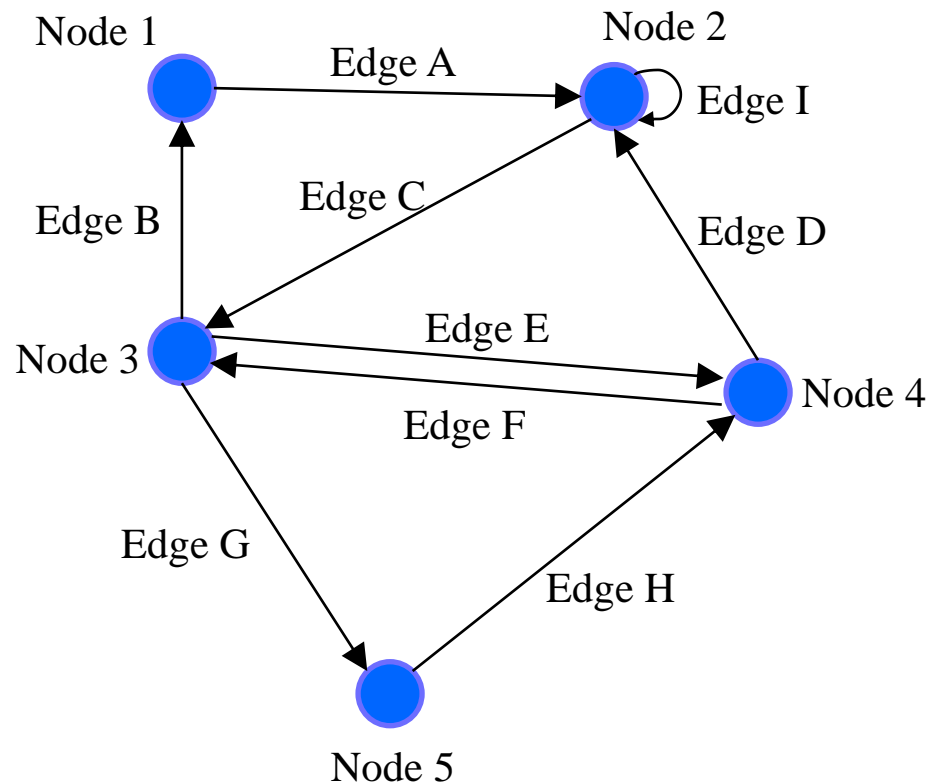
Node 3 has four neighbors:

- **Node 1** (child)
- **Node 2** (parent)
- **Node 4** (parent *and* child)
- **Node 5** (child)

Paths between nodes

A **path** is a “chain” of edges from a **source** to a **destination**.

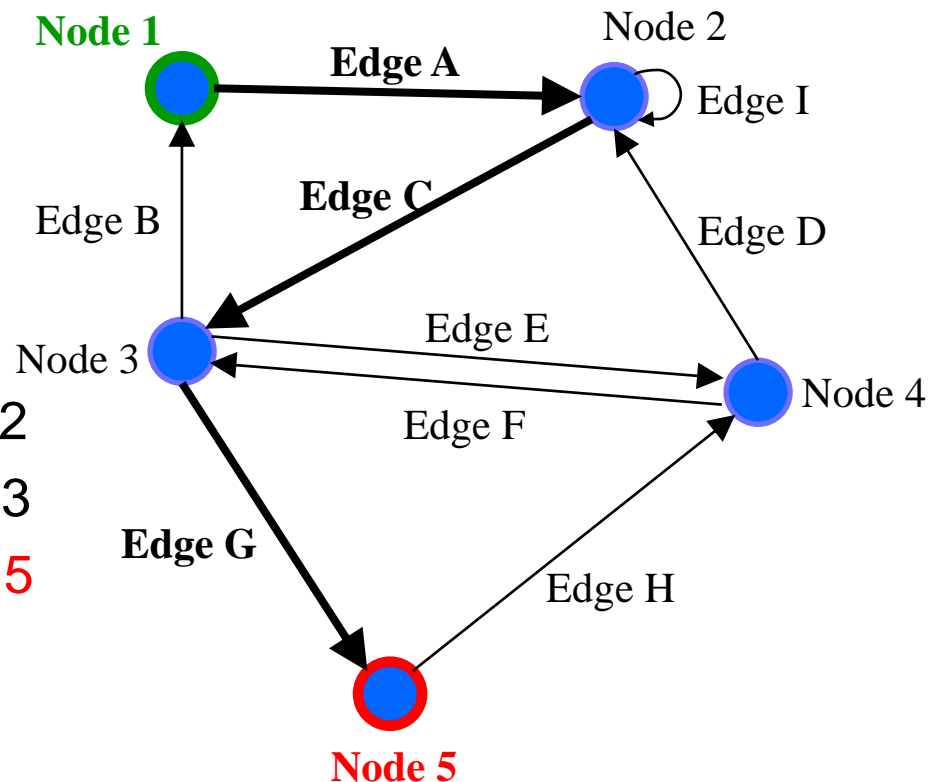
- Potentially empty sequence
- Might include a cycle
- Often want shortest



Paths between nodes

A **path** is a “chain” of edges from a **source** to a **destination**.

- Potentially empty sequence
- Might include a cycle
- Often want shortest



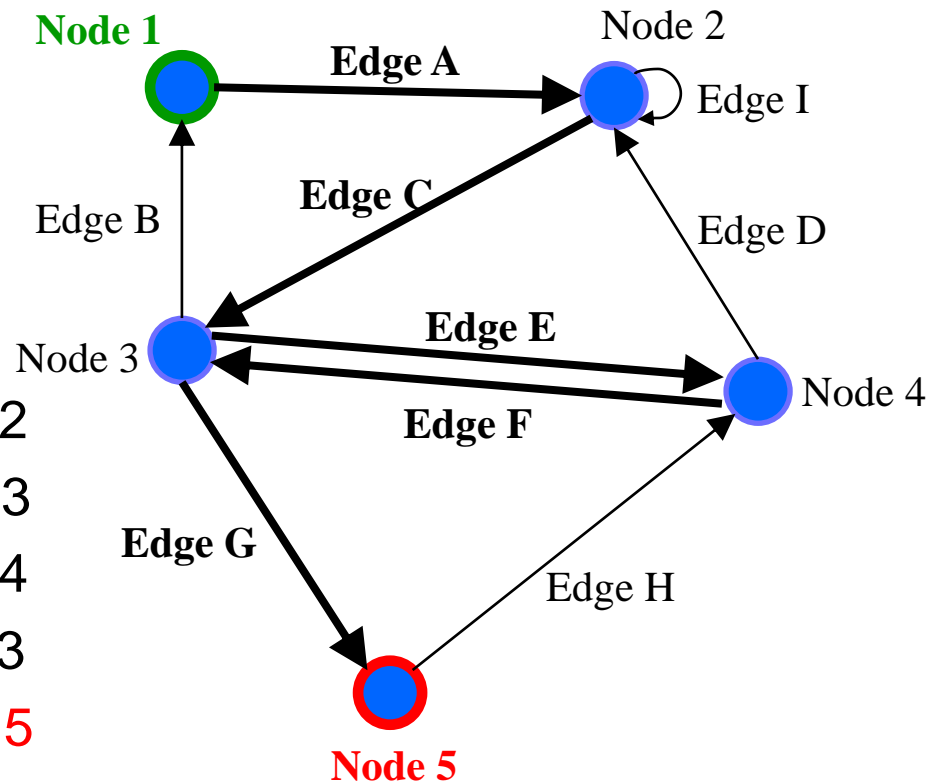
Path from **Node 1** to **Node 5**:

1. Edge A : **Node 1** → Node 2
2. Edge C : Node 2 → Node 3
3. Edge G : Node 3 → **Node 5**

Paths between nodes

A **path** is a “chain” of edges from a **source** to a **destination**.

- Potentially empty sequence
- Might include a cycle
- Often want shortest



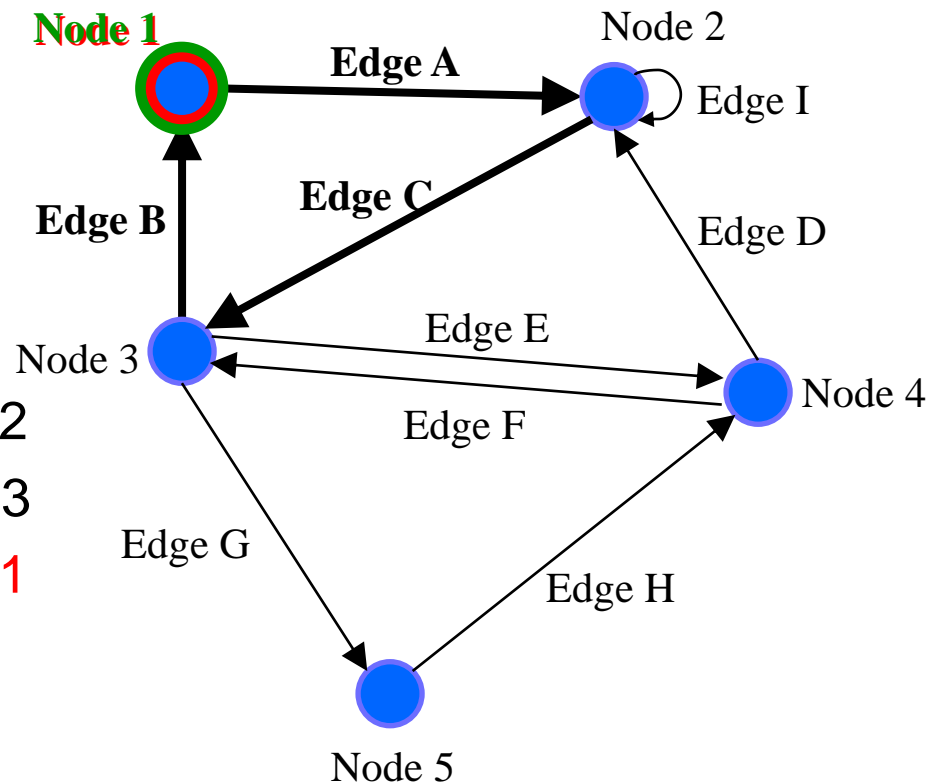
Path from **Node 1** to **Node 5**:

1. Edge A : **Node 1** → Node 2
2. Edge C : Node 2 → Node 3
3. Edge E : Node 3 → Node 4
4. Edge F : Node 4 → Node 3
5. Edge G : Node 3 → **Node 5**

Paths between nodes

A **path** is a “chain” of edges from a **source** to a **destination**.

- Potentially empty sequence
- Might include a cycle
- Often want shortest



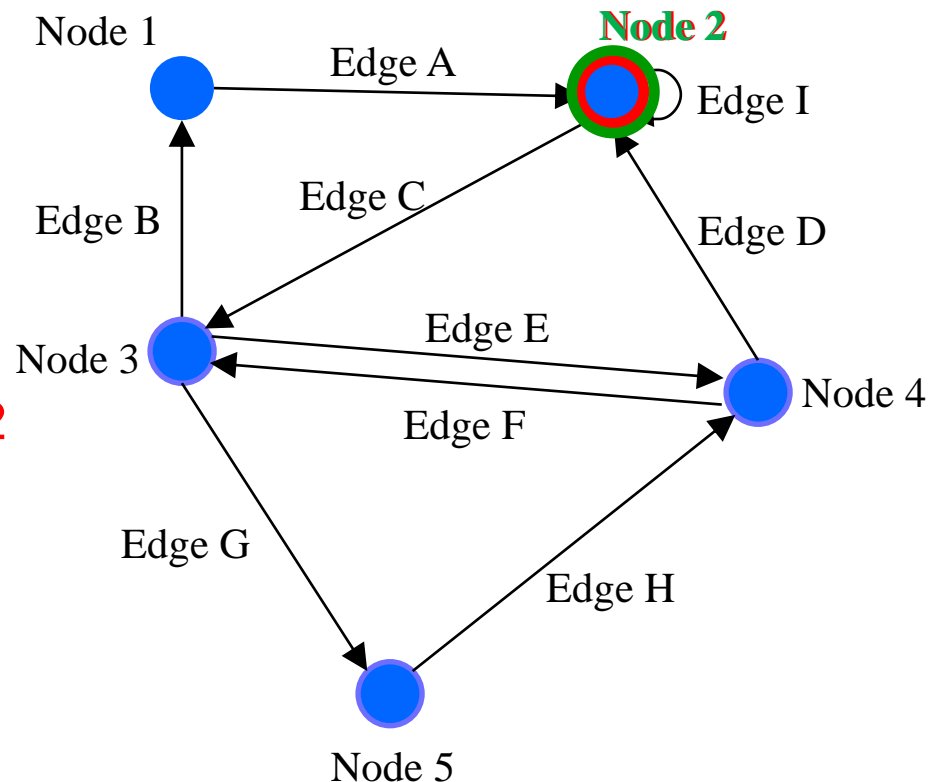
Path from **Node 1** to **Node 1**:

1. Edge A : **Node 1** → Node 2
2. Edge C : Node 2 → Node 3
3. Edge B : Node 3 → **Node 1**

Paths between nodes

A **path** is a “chain” of edges from a **source** to a **destination**.

- Potentially empty sequence
- Might include a cycle
- Often want shortest



Path from **Node 2** to **Node 2**:

1. Edge I : **Node 2** → **Node 2**

Possible graph operations

Creators

- Construct an empty graph

You might or might not want to include all of these operations in your graph ADT design.

Observers

- Look up node(s) by label, children of, parents of, neighbors of, ...
- Look up edge(s) by label, incoming to, outgoing from, ...
- Iterate through all nodes
- Iterate through all edges

Mutators

- Insert/remove a node
- Insert/remove an edge

More observers

- Find path(s) from one node to another
- Find all reachable nodes
- Count indegree, outdegree

HW5: Design before implementation

- HW5: Building an ADT for labeled, directed graphs
 - Labeled: Nodes and edges have label values (**Strings**)
 - Directed: Edges have direction
 - Edges with same source and destination will have unique labels
- The exact interface of your **Graph** class is up to you
 - So no given JUnit tests bundled with the starter code
 - Reminder: *Not a generic class.*
- HW5 is just designing and specifying the ADT
 - HW6 will be implementing it

HW5: What's Included

- Your submission for HW5 should include:
 - Java class(es) that represent your ADT
 - Each with method stubs
 - Specifications for **all** classes and methods
 - Tests for your ADT
 - JUnit and Script tests (coming soon...)
- Your submission for HW5 should **not** include:
 - Any implemented methods
 - Anything private (fields, methods, classes, etc.)
 - Including RI and AF

HW5: Specifications in JavaDoc

- Write class/method specifications in proper JavaDoc comments
 - See “Resources” → “Class and Method Specifications”
- You can generate nice HTML pages cleanly presenting all your JavaDoc specifications
 - Placed in “build/docs/javadoc/”
- This is a great way to verify the JavaDoc is formatted correctly
 - And to review/proofread your work...
- Let’s look at the JavaDoc from HW4... (demo)

JavaDoc Demo

- Run the “javadoc” gradle task (in the documentation folder)
- Locate `build/docs/javadoc/index.html`, right-click, **Open In >** a browser of your choice
 - Look for formatting errors or missing components!

HW5: Testing

- The design process includes crafting a good test suite
 - Script tests and JUnit tests
- **Script Tests** (`src/test/resources/testScripts/`)
 - Test script files `name.test` with corresponding `name.expected`
 - Validate behavior intrinsic to high-level concept (abstract meaning)
 - Tested properties should be expected of any solution to HW5
- **JUnit Tests** (`src/test/java/graph/junitTests/`)
 - JUnit test classes
 - Validate behavior that can't be tested with script tests.
- If you can validate a behavior using either test type, use a script test!

HW5: Script Tests

Each script test is expressed as text-based script `foo.test`

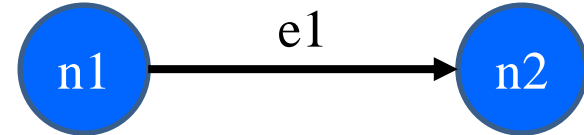
- One command per line, of the form: **Command** *arg₁* *arg₂* ...
- Script's output compared against `foo.expected`
- Precise details specified in the homework
- Match format **exactly**, including whitespace!

Command (in <code>foo.test</code>)	Output (in <code>foo.expected</code>)
<code>CreateGraph</code> <i>name</i>	<code>created graph</code> <i>name</i>
<code>AddNode</code> <i>graph label</i>	<code>added node</code> <i>label</i> <code>to graph</code>
<code>AddEdge</code> <i>graph parent child label</i>	<code>added edge</code> <i>label</i> <code>from parent to child in graph</code>
<code>ListNodes</code> <i>graph</i>	<code>graph contains:</code> <i>label</i> _{<i>node</i>} ...
<code>ListChildren</code> <i>graph parent</i>	<code>the children of parent in graph are:</code> <i>child</i> (<i>label</i> _{<i>edge</i>}) ...
<code># This is comment text ...</code>	<code># This is comment text ...</code>

HW5: example.test

```
# Create a graph  
CreateGraph graph1
```

```
# Add a pair of nodes  
AddNode graph1 n1  
AddNode graph1 n2
```



```
# Add an edge  
AddEdge graph1 n1 n2 e1
```

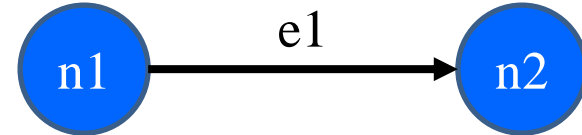
```
# Print all nodes in the graph  
ListNodes graph1
```

```
# Print all child nodes of n1 with outgoing edge  
ListChildren graph1 n1
```

HW5: example.expected

```
# Create a graph  
created graph graph1
```

```
# Add a pair of nodes  
added node n1 to graph1  
added node n2 to graph1
```



```
# Add an edge  
added edge e1 from n1 to n2 in graph1
```

```
# Print all nodes in the graph  
graph1 contains: n1 n2
```

```
# Print all child nodes of n1 with outgoing edge  
the children of n1 in graph1 are: n2(e1)
```

HW5: Why Script Tests?

- Everyone's implementation could (will!) be different, so we (staff) cannot write JUnit tests for everyone to use or to use for checking everyone's code.
- We still need a way to test that you specify and implement the proper behavior, so we use script tests that work regardless of the implementation.
- They test what the methods are doing, they don't care how the methods are doing it.

HW5: Creating a script test

1. Write test steps as script commands in a file `foo.test`
2. Write expected (“correct”) output in a file `foo.expected`
 - ...taking care to match the output format *exactly*
3. Place both files under `src/test/resources/testScripts/`
4. Run all such tests via the Gradle task `scriptTests`
 - After class implemented and **GraphTestDriver** stubs filled

HW5: Test Commands vs Methods

- Your graph should not have the exact same interface as the script test commands
 - e.g. you should not have a method called **AddNode()** that adds a node to the graph and prints out/returns the string “added node n1 to graph1”
 - This wouldn’t make much sense for other graph clients!
- But you will need the ability to add a node!
- Later, we will need some way to map script test commands (**AddNode graph1 n1**) to some Java code that uses the methods of your graph class
 - This is part of HW6; do not worry about for now

HW5: Script tests vs. JUnit Tests

- Script tests will not cover every case for your graph:
 - What if you have additional methods that can't be tested by our script test commands?
 - What about “bad” input for your graph?
 - What happens when you try to add the same node twice?
 - ...
- We need some way to test cases that cannot be covered by our script tests
- For this, we use JUnit tests.

HW5: Creating JUnit tests

1. Create JUnit test class in `src/test/java/graph/junitTests/`
2. Write a test method for each unit test
3. Run all such tests via the Gradle task `junitTests`

```
import org.junit.*;
import static org.junit.Assert.*;

/** Document class... */
public class FooTests {
    /** Document method... */
    @Test
    public void testBar() { ... /* JUnit assertions */ }
}
```

HW5: Creating JUnit tests

- Note: Your JUnit tests will fail in HW5, because you have not implemented the actual methods yet
 - The same goes for your script tests
- You will get them passing in HW6

Equals and Hashcode

The equals method (review)

- Specification mandates several properties:
 - *Reflexive*: `x.equals(x)` is `true`
 - *Symmetric*: `x.equals(y) ⇔ y.equals(x)`
 - *Transitive*: `x.equals(y) ∧ y.equals(z) ⇒ x.equals(z)`
 - *Consistent*: `x.equals(y)` shouldn't change, unless perhaps `x` or `y` did
 - *Null uniqueness*: `x.equals(null)` is `false`
- Several notions of equality:
 - *Referential*: literally the same object in memory
 - *Behavioral*: no sequence of operations could tell apart (excluding `==`)
 - *Observational*: no sequence of observer operations could tell apart (excluding `==`)

The hashCode method (review)

- Specification mandates several properties:
 - *Self-consistent*: `x.hashCode ()` shouldn't change, unless `x` did
 - *Equality-consistent*: `x.equals (y) ⇒ x.hashCode () == y.hashCode ()`
- Equal objects *must* have the same hash code.
 - Implementations of `equals` and `hashCode` work together for this
 - If you override `equals`, you **must** override `hashCode` as well
- Ideally a good `hashCode` method returns different values for unequal objects, but the contract does not require this.

Overriding `equals` and `hashCode`

- A subclass method overrides a superclass method, when...
 - They have the exact same name
 - They have the exact same argument types
- An overriding method should satisfy the overridden method's spec.
- Always use `@override` tag when overriding `equals` and `hashCode` (or any other overridden method)
- Note: Method overloading is not the same as overriding
 - Same name but distinguished by different argument types
- Keep these details in mind if you override `equals` and `hashCode`.

`equals` and `hashCode` worksheet

- Let's practice...

More Reasoning Practice

intToString()

Fill in the implementation of a method that converts a **positive integer** to its **string representation in decimal** (invariant given on next slide).

```
{ { P: x > 0 } }
```

```
String intToString(int x)
```

Useful facts to recall:

1. Convert **char** **ch** that is one of `'0'`, `'1'`, ..., `'9'` to a corresponding **int** by doing `ch - '0'`
2. Convert **int** **x** that is one of `0`, `1`, ..., `9` to a corresponding **char** by doing `(char) (x + '0')`

intToString()

```
{ { P: x > 0 } }
```

```
String intToString(int x) {
```

```
    StringBuilder buf =
```

```
    int k = , y = ;
```

```
    { { Inv: P and buf stores the lowest k digits of x  
        in reverse order and  $y = x / 10^k$  } }
```

```
    while (y != 0) {
```

```
        k = k + 1;
```

```
    }
```

```
    return buf.reverse().toString();
```

```
}
```

How do we get the invariant to hold initially?

intToString()

```
{ { P: x > 0 } }  
String intToString(int x) {  
    StringBuilder buf = new StringBuilder();  
    int k = 0, y = x;  
    { { Inv: P and buf stores the lowest k digits of x  
        in reverse order and y = x / 10^k } }  
    while (y != 0) {  
  
        k = k + 1;  
    }  
  
    return buf.reverse().toString();  
}
```

How do we fill out the loop body?

intToString()

```
{ { P: x > 0 } }
String intToString(int x) {
    StringBuilder buf = new StringBuilder();
    int k = 0, y = x;
    { { Inv: P and buf stores the lowest k digits of x
        in reverse order and y = x / 10^k } }
    while (y != 0) {

        k = k + 1;
    }

    return buf.reverse().toString();
}
```

Inv changes k to $k+1$, so

- y becomes $x / 10^{k+1}$
- $y_{\text{post}} = x / 10^{k+1} = y_{\text{pre}} / 10$

intToString()

```
{ { P: x > 0 } }  
String intToString(int x) {  
    StringBuilder buf = new StringBuilder();  
    int k = 0, y = x;  
    { { Inv: P and buf stores the lowest k digits of x  
        in reverse order and y = x / 10^k } }  
    while (y != 0) {  
  
        y = y / 10;  
        k = k + 1;  
    }  
  
    return buf.reverse().toString();  
}
```

Inv changes k to k+1, so

- y becomes $x / 10^{k+1}$
- $y_{\text{post}} = x / 10^{k+1} = y_{\text{pre}} / 10$

intToString()

```
{ { P: x > 0 } }  
String intToString(int x) {  
    StringBuilder buf = new StringBuilder();  
    int k = 0, y = x;  
    { { Inv: P and buf stores the lowest k digits of x  
        in reverse order and y = x / 10^k } }  
    while (y != 0) {  
  
        y = y / 10;  
        k = k + 1;  
    }  
  
    return buf.reverse().toString();  
}
```

- Inv changes k to $k+1$, so
- buf stores lowest $k+1$ digits

intToString()

```
{ { P: x > 0 } }  
String intToString(int x) {  
    StringBuilder buf = new StringBuilder();  
    int k = 0, y = x;  
    { { Inv: P and buf stores the lowest k digits of x  
        in reverse order and y = x / 10^k } }  
    while (y != 0) {  
  
        y = y / 10;  
        k = k + 1;  
    }  
  
    return buf.reverse().toString();  
}
```

Inv changes k to $k+1$, so

- buf stores lowest $k+1$ digits

$(k+1)$ -st lowest digit goes at end
since buf stores them reversed

intToString()

```
{ { P: x > 0 } }
String intToString(int x) {
    StringBuilder buf = new StringBuilder();
    int k = 0, y = x;
    { { Inv: P and buf stores the lowest k digits of x
        in reverse order and y = x / 10^k } }
    while (y != 0) {
        char ch = ?
        buf.append(ch);
        y = y / 10;
        k = k + 1;
    }

    return buf.reverse().toString();
}
```

How can we get the (k+1)-st lowest digit of x? And make it a char?

intToString()

```
{ { P: x > 0 } }  
String intToString(int x) {  
    StringBuilder buf = new StringBuilder();  
    int k = 0, y = x;  
    { { Inv: P and buf stores the lowest k digits of x  
        in reverse order and y = x / 10^k } }  
    while (y != 0) {  
        char ch = (char) (y % 10 + '0');  
        buf.append(ch);  
        y = y / 10;  
        k = k + 1;  
    }  
  
    return buf.reverse().toString();  
}
```

intToString() solution

```
{ { P: x > 0 } }
String intToString(int x) {
    StringBuilder buf = new StringBuilder();
    int k = 0, y = x;
    { { Inv: P and buf stores the lowest k digits of x
        in reverse order and y = x / 10^k } }
    while (y != 0) {
        char ch = (char) (y % 10 + '0');
        buf.append(ch);
        y = y / 10;
        k = k + 1;
    }
    { { buf stores the digits of x in reverse order } }
    return buf.reverse().toString();
}
```

Why does this hold?

intToString() solution

```
{ { P: x > 0 } }
String intToString(int x) {
    StringBuilder buf = new StringBuilder();
    int k = 0, y = x;
    { { Inv: P and buf stores the lowest k digits of x
        in reverse order and y = x / 10^k } }
    while (y != 0) {
        char ch = (char) (y % 10 + '0');
        buf.append(ch);
        y = y / 10;
        k = k + 1;
    }
    { { buf stores the digits of x in reverse order } }
    return buf.reverse().toString();
}
```

Why does this hold?

$y = 0 \Rightarrow x < 10^k$ so x only has k digits