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CSE 331  
Software Design & Implementation

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Testing

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# How do we ensure correctness?

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Best practice: use three techniques

## 1. **Tools**

- e.g., type checking, @Override, libraries, etc.

## 2. **Inspection**

- think through your code carefully
- have another person review your code

## 3. **Testing**

- usually >50% of the work in building software

Each removes  $\sim 2/3$  of bugs. Together >97%

# How do we ensure correctness?

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“Beware of bugs in the above code;  
I have only proved it correct, not tried it.”  
-Donald Knuth, 1977

Trying it is a surprisingly useful way to find mistakes!

No **single activity** or approach can guarantee correctness

We need tools **and** inspection **and** testing to ensure correctness

# It's hard to test your own code

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Your **psychology** is fighting against you:

- confirmation bias
  - tendency to avoid evidence that you're wrong
- operant conditioning
  - programmers get cookies when the code works
  - testers get cookies when the code breaks

You can avoid some effects of confirmation bias by

**writing most of your tests before the code**

Not much you can do about operant conditioning

# Testing Tips

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- Write tests both **before** and **after** you write the code
  - (only clear-box tests need to come afterward)
- Be systematic: think through revealing subdomains & test **each one**
- ...

# Kinds of testing

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- Testing field has terminology for different kinds of tests
  - we won't discuss all the kinds and terms
- Here are three orthogonal dimensions [so 8 varieties total]:
  - *unit* testing versus *system/integration* testing
    - one module's functionality versus pieces fitting together
  - *black-box* testing versus *clear-box* testing
    - did you look at the code before writing the test?
  - *specification* testing versus *implementation* testing
    - test only behavior guaranteed by specification or other behavior expected for the implementation

# Unit Testing

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- A unit test focuses on one class / module (or even less)
  - could write a unit test for a single method
- Tests a single unit in isolation from all others
- Integration tests verify that the modules fit together properly
  - usually don't want these until the units are well tested
    - i.e., unit tests come first

# How is testing done?

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## Write the test

- 1) Choose input / configuration
- 2) Define the expected outcome

## Run the test

- 3) Run with input and record the actual outcome
- 4) Compare *actual* outcome to *expected* outcome



# What's So Hard About Testing?

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“Just try it and see if it works...”

```
// requires:  $1 \leq x, y, z \leq 10000$   
// returns: computes some  $f(x, y, z)$   
int func1(int x, int y, int z) {...}
```

Exhaustive testing would require 1 trillion runs!

- impractical even for this trivially small problem

Key problem: choosing test suite

- Large/diverse enough to provide a useful amount of validation
- (Small enough to write/run in reasonable amount of time.)
  - less important... very few projects have too many tests

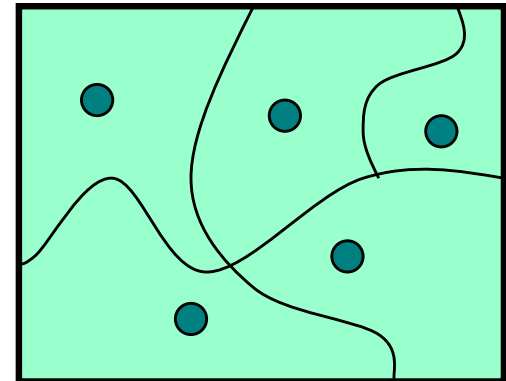
# Approach: Partition the Input Space

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## Ideal test suite:

Identify sets with “same behavior”  
(actual and expected)

Test **at least** one input from each set  
(we call this set a *subdomain*)

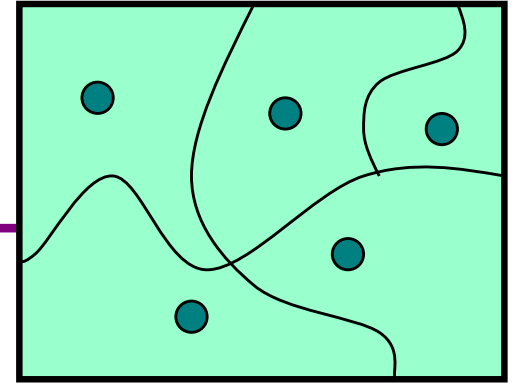


**Problem:** we don't know the behavior on all inputs

- if we did, we wouldn't need to test!

# Revealing Subdomains

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- A *subdomain* is a subset of possible inputs
- A subdomain is *revealing* for error  $E$  if either:
  - *every* input in that subdomain triggers error  $E$ , *or*
  - *no* input in that subdomain triggers error  $E$
- Need test at least one input from a revealing subdomain to find bug
  - if you test one input from every revealing subdomain for  $E$ , you are guaranteed to find the bug
- The trick is to *guess* revealing subdomains for **the errors present**
  - even though your reasoning says your code is correct, make educated guesses where the bugs might be

# Testing Heuristics

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- Testing is *essential* but difficult
  - want set of tests likely to reveal the bugs present
  - but we don't know where the bugs are
- Our approach:
  - split the input space into enough subsets (subdomains) such that inputs in each one are likely all correct or incorrect
  - can then take just one example from each subdomain
- Some heuristics are useful for choosing subdomains...

# Specification Testing

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Heuristic: Explore alternate cases in the specification

Procedure is a **black box**: specification visible, internals hidden

Example

```
// returns: a > b => returns a  
// a < b => returns b  
// a = b => returns a  
int max(int a, int b) {...}
```

3 cases lead to 3 tests

$(4, 3) \Rightarrow 4$  (*i.e. any input in the subdomain  $a > b$* )  
 $(3, 4) \Rightarrow 3$  (*i.e. any input in the subdomain  $a < b$* )  
 $(3, 3) \Rightarrow 3$  (*i.e. any input in the subdomain  $a = b$* )

# More Complex Example

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Write tests based on cases in the specification

```
// returns: the smallest i such
//           that a[i] == value
// throws:  Missing if value is not in a
int find(int[] a, int value) throws Missing
```

Two obvious tests:

```
( [4, 5, 6], 5 ) => 1
( [4, 5, 6], 7 ) => throw Missing
```

Have we captured all the cases?

```
( [4, 5, 5], 5 ) => 1
```

Must hunt for multiple cases

- Including scrutiny of effects and modifies

# Specification Testing: Advantages

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Process is not influenced by component being tested

- avoids psychological biases we discussed earlier
- can only do this for your own code if you **write tests first**

Robust with respect to changes in implementation

- test data need not be changed when code is changed

Allows others to test the code (rare nowadays)

# Heuristic: Clear (glass, white)-box testing

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*Focus* on features not described by specification

- control-flow details (e.g., conditions of “if” statements in code)
- performance optimizations
- alternate algorithms for different cases



# Clear-box Example

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There are some subdomains that black-box testing won't catch:

```
boolean[] primeTable = new boolean[CACHE_SIZE];

boolean isPrime(int x) {
    if (x > CACHE_SIZE) {
        for (int i=2; i <= x/2; i++) {
            if (x % i == 0)
                return false;
        }
        return true;
    } else {
        return primeTable[x];
    }
}
```

# Combining Clear- and Black-Box

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For buggy `abs`, what are revealing subdomains?

```
// returns:  x < 0      => returns -x
//           otherwise => returns  x

int abs(int x) {
    if (x < -2) return -x;
    else       return  x;
}
```

Example sets of subdomains:

– Which is best?

```
... {-2} {-1} {0} {1} ...
{..., -4, -3} {-2, -1} {0, 1, ...}
```

Why *not*:

```
{..., -6, -5, -4} {-3, -2, -1} {0, 1, 2, ...}
```

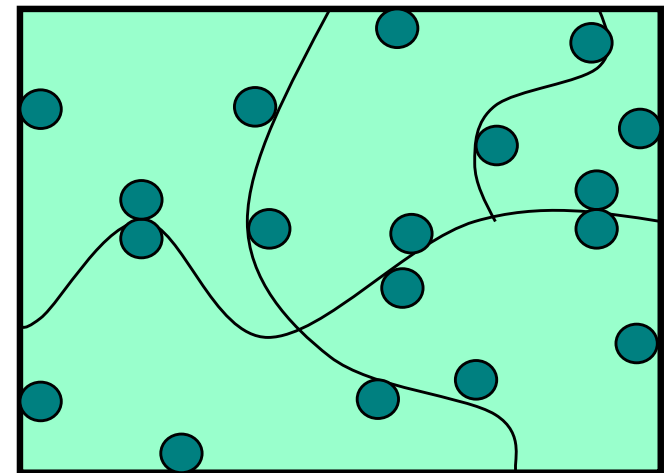
# Heuristic: Boundary & Special Cases

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Create tests at the edges of subdomains

Why?

- Off-by-one bugs
- “Empty” cases (0 elements, null, ...)
- Overflow errors in arithmetic
- Object aliasing



Small subdomains at the edges of the “main” subdomains have a high probability of revealing many common errors

- also, you might have misdrawn the boundaries

# Boundary Testing

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Point is on a boundary if either:

- there exists an adjacent point in a different subdomain
- there is no point to one side

Example: function has different behavior on  $n$  and  $n+1$

# Boundary Cases: Integers

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```
// returns: |x|  
public int abs(int x) {...}
```

What are some values or ranges of  $x$  that might be worth probing?

- $x < 0$  (flips sign) or  $x \geq 0$  (returns unchanged)
- Around  $x = 0$  (boundary condition)
- *Specific tests: say  $x = -1, 0, 1$*

# Boundary Testing

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To define the boundary, need a notion of **adjacent inputs**

Example approach:

- identify basic operations on input points
- two points are adjacent if one basic operation apart

Point is on a boundary if either:

- there exists an adjacent point in a different subdomain
- some basic operation cannot be applied to the point

Example: list of integers

- basic operations: *create*, *append*, *set*, *remove*
- adjacent points:  $\langle [2,3], [2,4] \rangle$ ,  $\langle [2,3], [2,3,3] \rangle$ ,  $\langle [2,3], [2] \rangle$
- boundary point:  $[ ]$  (can't apply *remove*)

# Heuristic: Special Cases

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## Arithmetic

- smallest/largest values
- zero

## Objects

- null
- list containing itself
  - maybe a bit too pathological
- same object passed as multiple arguments (aliasing)

All of these are common cases where bugs lurk

- you'll find more as you encounter more bugs

# Special Cases: Arithmetic Overflow

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```
// returns: |x|  
public int abs(int x) {...}
```

*How about...*

```
int x = Integer.MIN_VALUE; // x=-2147483648  
System.out.println(x<0); // true  
System.out.println(Math.abs(x)<0); // also true!
```

From Javadoc for `Math.abs`:

Note that if the argument is equal to the value of `Integer.MIN_VALUE`, the most negative representable int value, the result is that same value, which is negative



# Special Cases: Duplicates & Aliases

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```
// modifies: src, dest
// effects:  removes all elements of src and
//           appends them in reverse order to
//           the end of dest
<E> void appendList(List<E> src, List<E> dest) {
    while (src.size() > 0) {
        E elt = src.remove(src.size() - 1);
        dest.add(elt);
    }
}
```

What happens if `src` and `dest` refer to the same object?

- this is *aliasing*
- it's easy to forget!
- watch out for shared references in inputs

# sqrt example

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```
// throws: IllegalArgumentException if x<0
// returns: approximation to square root of x
public double sqrt(double x) {...}
```

What are some values or ranges of  $x$  that might be worth probing?

$x < 0$  (exception thrown)

$x \geq 0$  (returns normally)

around  $x = 0$  (boundary condition)

perfect squares ( $\text{sqrt}(x)$  an integer), non-perfect squares

$x < \text{sqrt}(x)$  and  $x > \text{sqrt}(x)$  – that's  $x < 1$  and  $x > 1$  (and  $x = 1$ )

*Specific tests: say  $x = -1, 0, 0.5, 1, 4$  (probably want more)*

# How many tests is enough?

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Common *goal* is high **code coverage**:

- ensure test suite covers (executes) all of the program
- assess quality of test suite with % *coverage*
  - tools to measure this for you

*Assumption* implicit in goal:

- if high coverage, then most mistakes discovered
- **far** from perfect but widely used

# Code coverage: statement coverage

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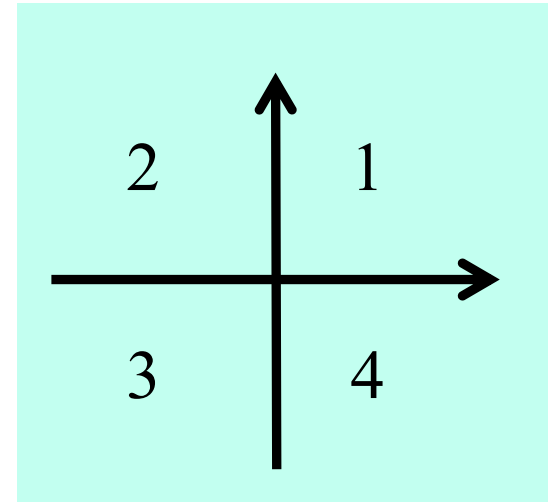
```
int min(int a, int b) {  
    int r = a;  
    if (a <= b) {  
        r = a;  
    }  
    return r;  
}
```

- Consider any test with  $a \leq b$  (e.g., `min(1, 2)`)
  - executes every instruction
  - misses the bug
- *Statement coverage* is not enough

# Code coverage: branch coverage

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```
int quadrant(int x, int y) {  
    int ans;  
    if (x >= 0)  
        ans=1;  
    else  
        ans=2;  
    if (y < 0)  
        ans=4;  
    return ans;  
}
```



- Consider two-test suite: (2,-2) and (-2,2). Misses the bug.
- *Branch coverage* (all tests “go both ways”) is not enough
  - here, *path coverage* is enough (there are 4 paths)

# Code coverage: path coverage

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```
int countPositive(int[] a) {
    int ans = 0;
    for (int x : a) {
        if (x > 0)
            ans = 1; // should be ans += 1;
    }
    return ans;
}
```

- Consider two-test suite: [0,0] and [1]. Misses the bug.
- Or consider one-test suite: [0,1,0]. Misses the bug.
- *Branch coverage* is not enough
  - here, *path coverage* is enough, but *no bound* on path-count!

# Code coverage: what is enough?

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```
int sumOfThree(int a, int b, int c) {  
    return a+b;  
}
```

- *Path coverage* is not enough
  - consider test suites where **c** is always 0
- Typically a “moot point” since path coverage is unattainable for realistic programs
  - but do not assume a tested path is correct
  - even though it is more likely correct than an untested path
- Another example: buggy **abs** method from earlier in lecture

# Varieties of coverage

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Various coverage metrics (there are more):

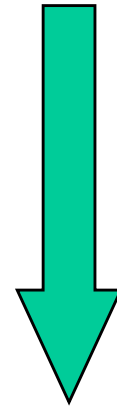
Statement coverage

Branch coverage

*Loop coverage*

*Condition/Decision coverage*

Path coverage



increasing  
number of  
test cases  
required  
(generally)

Limitations of coverage:

1. 100% coverage is not always a reasonable target
  - may be *high cost* to approach 100%
2. Coverage is *just a heuristic*
  - we really want the revealing subdomains for the errors present



# Summary of Heuristics

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- Split subdomains on boundaries appearing in the specification
- Split subdomains on boundaries appearing in the implementation
- Test boundaries that commonly lead to errors
- Test special cases like nulls, empty arrays, 0, etc.
- Tests to exercise every branch of the code
  - all paths would be even nicer (but not always possible)
- Test any cases that caused bugs before (to avoid regression)

On the other hand, don't confuse *volume* with *quality* of tests

- look for revealing subdomains
- want tests in every revealing subdomain not **just** lots of tests

# Testing Tools

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- Modern development ecosystems have built-in support for testing
- Your homework introduces you to Junit
  - standard framework for testing in Java
- Continuous integration
  - ensure tests pass **before** code is submitted
- You will see more sophisticated tools in industry
  - libraries for creating mock implementations of other modules
  - automated tools to test on every platform
  - automated tools to find severe bugs (using AI)
  - ...

# Testing Tips

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- Write tests both **before** and **after** you write the code
  - (only clear-box tests need to come afterward)
- Be systematic: think through revealing subdomains & test **each one**
- Test your tests
  - try putting a bug in to make sure the test catches it
- Test code is different from regular code
  - changeability is less important; **correctness** is more important
  - do not write **any test code** that is not obviously correct
    - otherwise, you need to test that code too!
    - unlike in regular code, it's *okay* to repeat yourself in tests