CSE 331 Software Design & Implementation

Hal Perkins Winter 2018 Abstraction Functions

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Connecting implementations to specs

Representation Invariant: maps Object → boolean

- Indicates if an instance is *well-formed*
- Defines the set of valid concrete values
- Only values in the valid set make sense as implementations of an abstract value
- For implementors/debuggers/maintainers of the abstraction: no object should ever violate the rep invariant
 - Such an object has no useful meaning

Abstraction Function: maps Object \rightarrow abstract value

- What the data structure *means* as an abstract value
- How the data structure is to be interpreted
- Only defined on objects meeting the rep invariant
- For implementors/debuggers/maintainers of the abstraction: Each procedure should meet its spec (abstract values) by "doing the right thing" with the concrete representation

Rep inv. constrains structure, not meaning

```
An implementation of insert that preserves the rep invariant:
    public void insert(Character c) {
        Character cc = new Character(encrypt(c));
        if (!elts.contains(cc))
            elts.addElement(cc);
    }
    public boolean member(Char
        return elts.contains(c)
    }
    ...
}
CharSet s = new CharSet();
```

Program is still wrong

- Clients observe incorrect behavior
- What client code exposes the error?
- Where is the error?
- We must consider the *meaning*
- The *abstraction function* helps us

Abstraction function: rep→abstract value

The abstraction function maps the concrete representation to the abstract value it represents
AF: Object → abstract value
AF(CharSet this) = { c | c is contained in this.elts }
"set of Characters contained in this.elts"

Not executable because abstract values are "just" conceptual

The abstraction function lets us reason about what [concrete] methods do in terms of the clients' [abstract] view

Abstraction function and insert

Goal is to satisfy the specification of insert:

// modifies: this
// effects: this_{post} = this_{pre} U {c}
public void insert (Character c) {...}

The AF tells us what the rep means, which lets us place the blame

AF(CharSet this) = { c | c is contained in this.elts } Consider a call to insert:

On *entry*, meaning is AF(this_{pre}) = elts_{pre} On *exit*, meaning is AF(this_{post}) = AF(this_{pre}) U {encrypt('a')}

What if we used this abstraction function instead? AF(this) = { c | encrypt(c) is contained in this.elts } = { decrypt(c) | c is contained in this.elts } UW CSE 331 Winter 2018

The abstraction function is a function

Why do we map concrete to abstract and not vice versa?

- It's not a function in the other direction
 - Example: lists [a,b] and [b,a] might each represent the set {a,b}
- It's not as useful in the other direction
 - Purpose is to reason about whether our methods are manipulating concrete representations correctly in terms of the abstract specifications

Stack AF example

Abstract stack with array and "top" index implementation



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Benevolent side effects



- Move-to-front speeds up repeated membership tests
- Mutates rep, but does not change abstract value
 - AF maps both reps to the same abstract value
 - Precise reasoning/explanation for "clients can't tell"

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For any correct operation...



Writing an abstraction function

Domain: all representations that satisfy the rep invariant Range: can be tricky to denote

- For mathematical entities like sets: easy
- For more complex abstractions: give names to specification
- AF defines the value of each "specification field"
 - (Course notes have examples of complex AFs with many spec. fields, but it's possible to be too complex – go for simple, correct, understandable whenever possible)

Overview section of the specification should provide a notation for writing abstract values

- Could implement a method for printing in this notation
 - Useful for debugging
 - Often a good choice for toString

Data Abstraction: Summary

Rep invariant

- Which concrete values represent abstract values

Abstraction function

- For each concrete value, which abstract value it represents

Together, they modularize the implementation

- Neither one is part of the ADT's specification
- Both are needed to reason that an implementation satisfies the specification

In practice, representation invariants are documented more often and more carefully than abstraction functions

A more widely understood and appreciated concept