

CSE 331

Software Design and Implementation

# Lecture 5

## *Representation Invariants*

Leah Perlmutter / Summer 2018

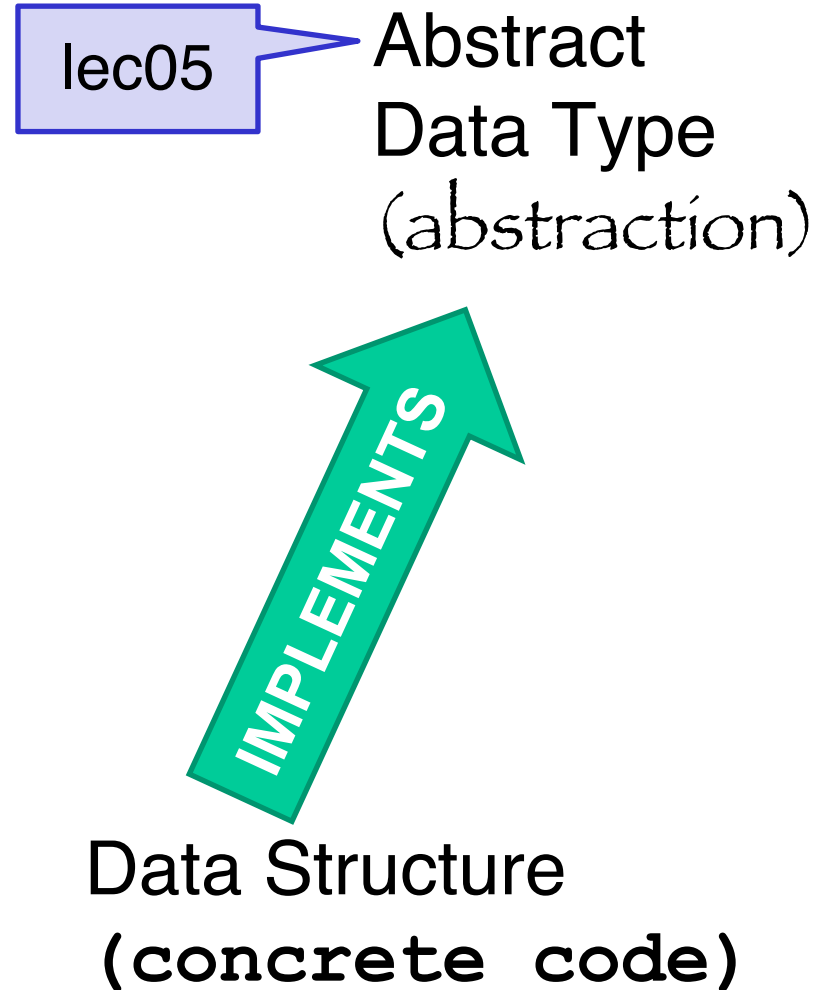
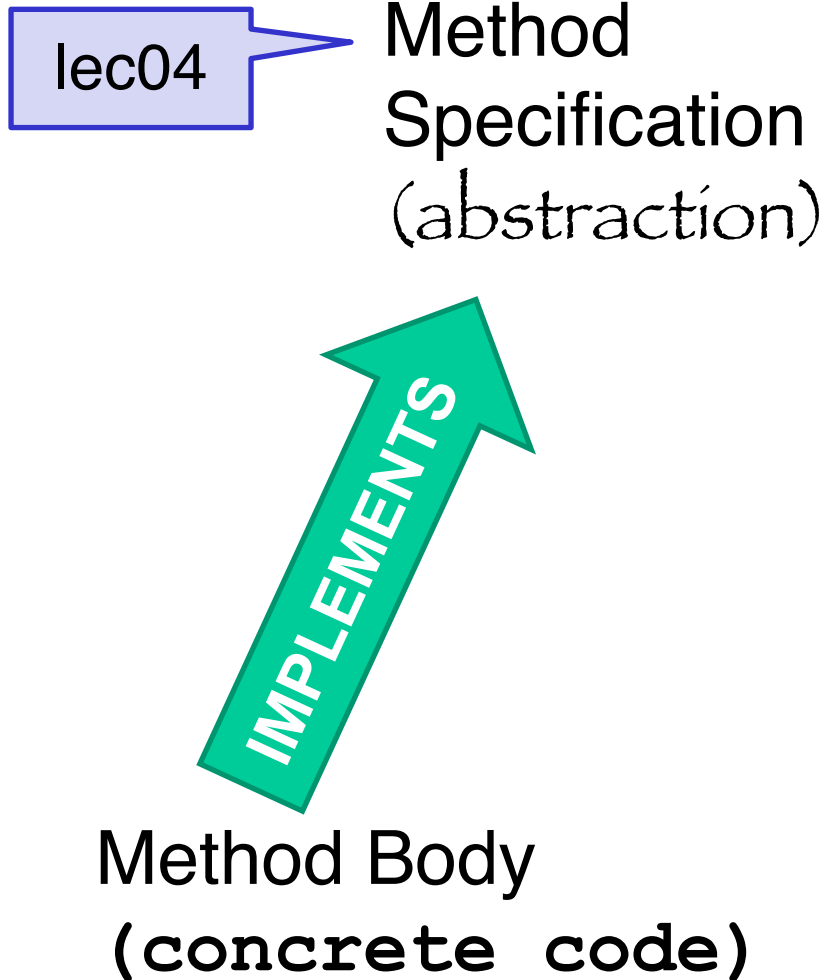
# Announcements

# Announcements

- Happy Friday!
  - My t-shirt
- Next week
  - HW2 due Monday, July 4 at 10pm
    - It's harder than HW1
    - Please take advantage of today's office hours!
  - July 4 holiday on Wednesday -- no class!
    - TAs will announce OH changes
  - HW3 due Thursday

# Motivation

# Review



# An ADT is a specification

**Abstract state** + collection of **procedural abstractions** (aka method specs)

- Not a collection of procedures

Together, these procedural abstractions provide some **set of values**

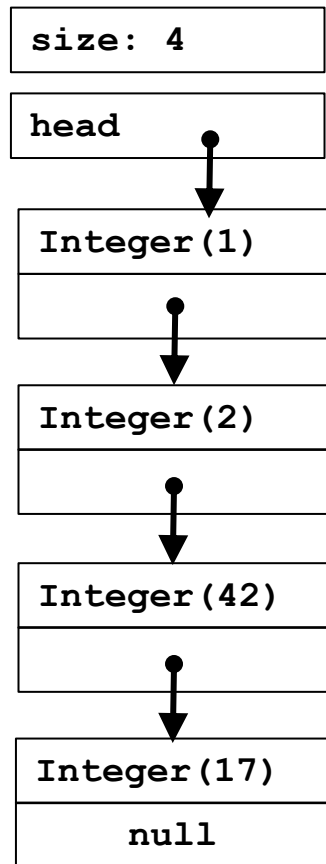
**All** the ways of directly using that set of values

- Creating
- Manipulating
- Observing

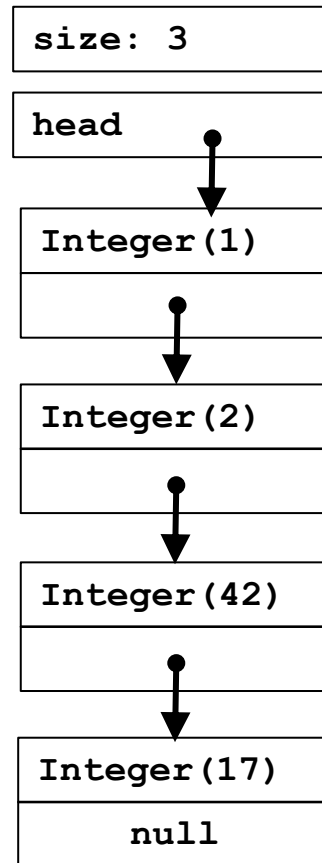
- Creators and producers: make new values
- Mutators: change the value
- Observers: allow one to distinguish different values

# An ADT has an abstract value

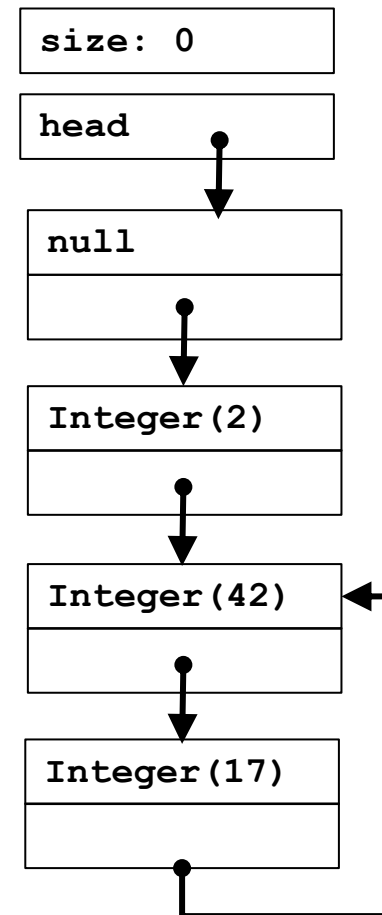
Abstract Value: An Int List is a finite sequence of integer values



1, 2, 42, 17

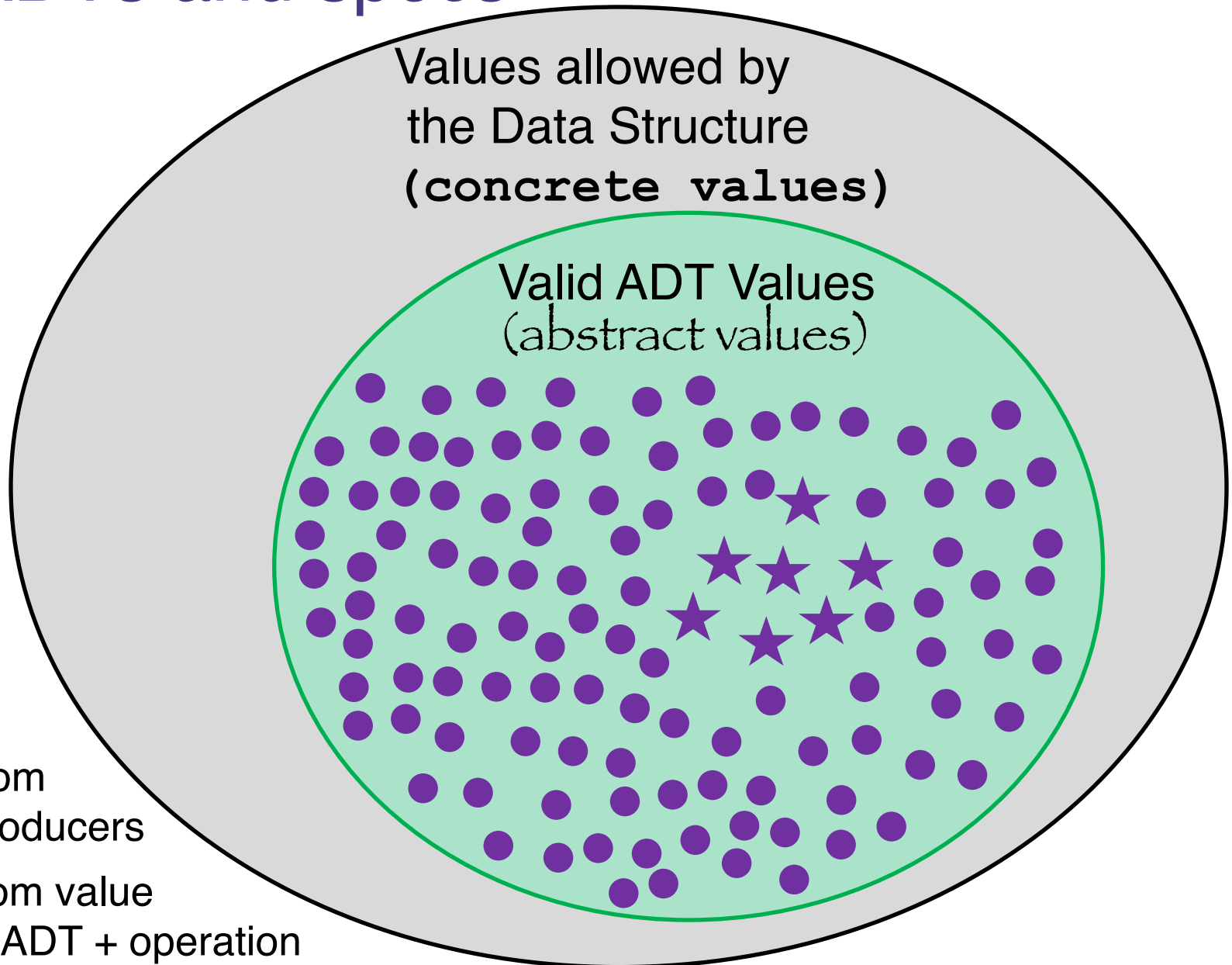


?



?????

# ADTs and specs





# ADTs and specifications

So far, we have only specified ADTs



lec05

- Specification makes no reference to the implementation

Of course, we need [*guidelines for how*] to implement ADTs

- **Data Structure** implements an ADT

Of course, we need [*guidelines for how*] to ensure our implementations satisfy our specifications

Two intellectual tools are really helpful...

# Connecting implementations to specs

**Representation Invariant:** maps Object  $\rightarrow$  boolean

lec06  
(today)

- Indicates if an instance is *well-formed*
- Defines the set of valid concrete values
- Only values in the valid set make sense as implementations of an abstract value
- **For implementors/debuggers/maintainers of the abstraction: no object should *ever* violate the rep invariant**
  - Such an object has no useful meaning

**Abstraction Function:** maps Object  $\rightarrow$  abstract value

lec07

- What the data structure *means* as an abstract value
- How the data structure is to be interpreted
- Only defined on objects meeting the rep invariant
- **For implementors/debuggers/maintainers of the abstraction:** Each procedure should meet its spec (abstract values) by “doing the right thing” with the concrete representation

# Representation Invariants

# Implementing a Data Abstraction (ADT)

To implement a data abstraction:

- Select the representation of instances, “*the rep*”
  - In Java, typically instances of some class you define
- Implement operations in terms of that rep

Choose a representation so that:

- It is possible to implement required operations
- The most frequently used operations are efficient
  - But which will these be?
  - Abstraction allows the rep to change later

# Example: CharSet Abstraction

// Overview: A CharSet is a finite mutable set of Characters

// @effects: creates a fresh, empty CharSet

public CharSet() {...}

set – see Wolfram  
Alpha definition

// @modifies: this

// @effects:  $\text{this}_{\text{post}} = \text{this}_{\text{pre}} + \{c\}$

public void insert(Character c) {...}

set union

// @modifies: this

// @effects:  $\text{this}_{\text{post}} = \text{this}_{\text{pre}} - \{c\}$

public void delete(Character c) {...}

set difference

// @return: ( $c \in \text{this}$ )

public boolean member(Character c) {...}

// @return: cardinality of this

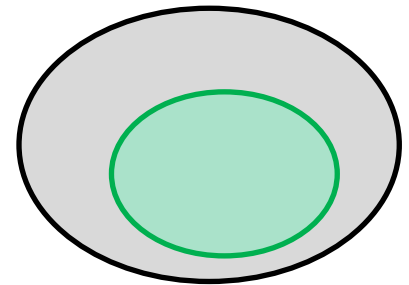
public int size() {...}

Informal notation warning

# An implementation: Is it right?

```
class CharSet {  
    private List<Character> elts =  
        new ArrayList<Character>();  
    public void insert(Character c) {  
        elts.add(c);  
    }  
    public void delete(Character c) {  
        elts.remove(c);  
    }  
    public boolean member(Character c) {  
        return elts.contains(c);  
    }  
    public int size() {  
        return elts.size();  
    }  
}
```

the rep



Does this implementation prevent poorly formed values?

# An implementation: Is it right?

```
class CharSet {  
    private List<Character> elts =  
        new ArrayList<Character>();  
  
    public void insert(  
        elts.add(c);  
    }  
    public void delete(  
        elts.remove(c);  
    }  
    public boolean member(  
        return elts.contains(c);  
    }  
    public int size() {  
        return elts.size();  
    }  
}
```

```
CharSet s = new CharSet();  
Character a = new Character('a');  
s.insert(a);  
s.insert(a);  
s.delete(a);  
if (s.member(a))  
    System.out.print("wrong");  
else  
    System.out.print("right");
```

# An implementation: Is it right?

```
class CharSet {  
    private List<Character> elts =  
        new ArrayList<Character>();  
    public void insert(Character c) {  
        elts.add(c);  
    }  
    public void delete(Character c) {  
        elts.remove(c);  
    }  
    public boolean member(Character c) {  
        return elts.contains(c);  
    }  
    public int size() {  
        return elts.size();  
    }  
}
```

*Where* is the error?



# Where Is the Error?

If you can answer this, then you know what to fix

*Perhaps **delete** is wrong*

- Should remove all occurrences?

*Perhaps **insert** is wrong*

- Should not insert a character that is already there?

How can we know?

- The **representation invariant** tells us
- If it's “our code”, this is how we document our choice for “the right answer”

# The representation invariant

- Defines data structure well-formedness
- Must hold before and after every `CharSet` operation
- Operations (methods) may depend on it
- Write it like this:

```
class CharSet {  
    // Rep invariant:  
    //    this.elts has no nulls and no duplicates  
    private List<Character> elts = ...  
    ...  
}
```

Or, more formally (if you prefer):

$\forall$  indices  $i$  of `this.elts` , `this.elts.elementAt(i)  $\neq$  null`

$\forall$  indices  $i, j$  of `this.elts` ,

`this.elts.elementAt(i).equals(this.elts.elementAt(j))  $\Rightarrow$   $i = j$`

$\forall$  = "for all"

$\Rightarrow$  = logical implication

# The representation invariant

```
class CharSet {  
    // Rep invariant:  
    //    this.elts has no nulls and no duplicates  
    private List<Character> elts = ...  
    ...  
}
```

- Written in terms of the representation (`this.elts`)
- Internal comment (not javadoc)
  - located just inside of the class definition at the very beginning

# The representation invariant

```
class CharSet {  
    // Rep Invariant:  
    // for all indices i of this.elts ,  
    //      this.elts.elementAt(i) is not null  
    // for all indices i, j of this.elts ,  
    //      this.elts.elementAt(i) .  
    //          equals(this.elts.elementAt(j))  
    //          implies that i = j  
    private List<Character> elts = ...  
    ...  
}
```


- Written in terms of the representation (`this.elts`)
- Internal comment (not javadoc)
  - located just inside of the class definition at the very beginning

# Now we can locate the error

```
// Rep invariant:  
//   elts has no nulls and no duplicates  
  
public void insert(Character c) {  
    elts.add(c);  
}  
  
public void delete(Character c) {  
    elts.remove(c);  
}
```

# Another example

```
class Account {  
    private int balance;  
    // history of all transactions  
    private List<Transaction> transactions;  
    ...  
}
```



Real-world constraints:

- Balance  $\geq 0$
- Balance =  $\sum_i \text{transactions.get}(i).\text{amount}$

$\sum_i \dots$  = the sum, over  
all values of  $i$ , of ...

Implementation-related constraints:

- Transactions  $\neq$  null
- No nulls in transactions

# Checking rep invariants

**Should code check that the rep invariant holds?**

– **Short answer: YES!!!!**

More considerations

- Development vs. Production
  - Always yes in development [even when it's expensive]
  - Production... usually yes
    - (See Pragmatic Programmer: Assertive Programming)
- computational cost [depends on the invariant]
  - sometimes no for expensive checks, in production
- Some private methods need not check (Why?)

**A great debugging technique:**

**Design your code to catch bugs early by implementing and using rep-invariant checking**

# Checking the rep invariant

Rule of thumb: check on entry *and* on exit (why?)

```
/** Verify elts has no nulls or duplicates and... */
private void checkRep() {
    for (int i = 0; i < elts.size(); i++) {
        assert elts.elementAt(i) != null;
        assert elts.indexOf(elts.elementAt(i)) == i;
    }
    ... // more checks
}

public void delete(Character c) {
    checkRep();
    elts.remove(c);
    // Is this guaranteed to get called?
    // (could guarantee it with a finally block)
    checkRep();
}
```

What does  
assert mean?



# Practice *defensive programming*

Assume that you will make mistakes

Write and incorporate code designed to catch them

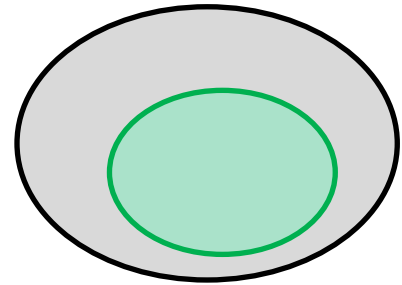
- On entry:
  - Check rep invariant
  - Check preconditions
- On exit:
  - Check rep invariant
  - Check postconditions

Checking the rep invariant helps you *discover* errors

Reasoning about the rep invariant helps you *avoid* errors

# Summary so far...

- We implement an **Abstract Data Type** with a **Data Structure**
- Every Data Structure has a **Representation** that is a concrete way of representing an object's **abstract value**
- The representation allows concrete values that do not correspond to an abstract value
  - “gray area” ----->
- **Representation Invariant** describes what makes the concrete representation valid (green area)
- **checkRep()** method verifies that the rep is valid, throws exception if not, protects you from yourself
- Check your rep all the time!
  - generally at beginning and end of every public method



# Representation Exposure

# Listing the elements of a CharSet

Consider adding the following method to `CharSet`

```
// returns: a List containing the members of this  
public List<Character> getElts();
```

Consider this implementation:

```
// Rep invariant: elts has no nulls and no dups  
public List<Character> getElts() { return elts; }
```

Does the implementation of `getElts` preserve the rep invariant?

# Listing the elements of a CharSet

Consider adding the following method to `CharSet`

```
// returns: a List containing the members of this  
public List<Character> getElts();
```

Consider this implementation:

```
// Rep invariant: elts has no nulls and no dups  
public List<Character> getElts() { return elts; }
```

Does the implementation of `getElts` preserve the rep invariant?

Kind of, sort of, not really....

# Representation exposure

Consider this client code (outside the `CharSet` implementation):

```
CharSet s = new CharSet();  
Character a = new Character('a');  
s.insert(a);  
s.getElts().add(a);  
s.delete(a);  
if (s.member(a)) ...
```

Representation exposure is external access to the rep

Representation exposure is almost always **evil**

***A big deal, a common bug, you now have a name for it!***

If you do it, document why and how

- And feel guilty about it!

# Avoiding representation exposure

*Understand* what representation exposure is

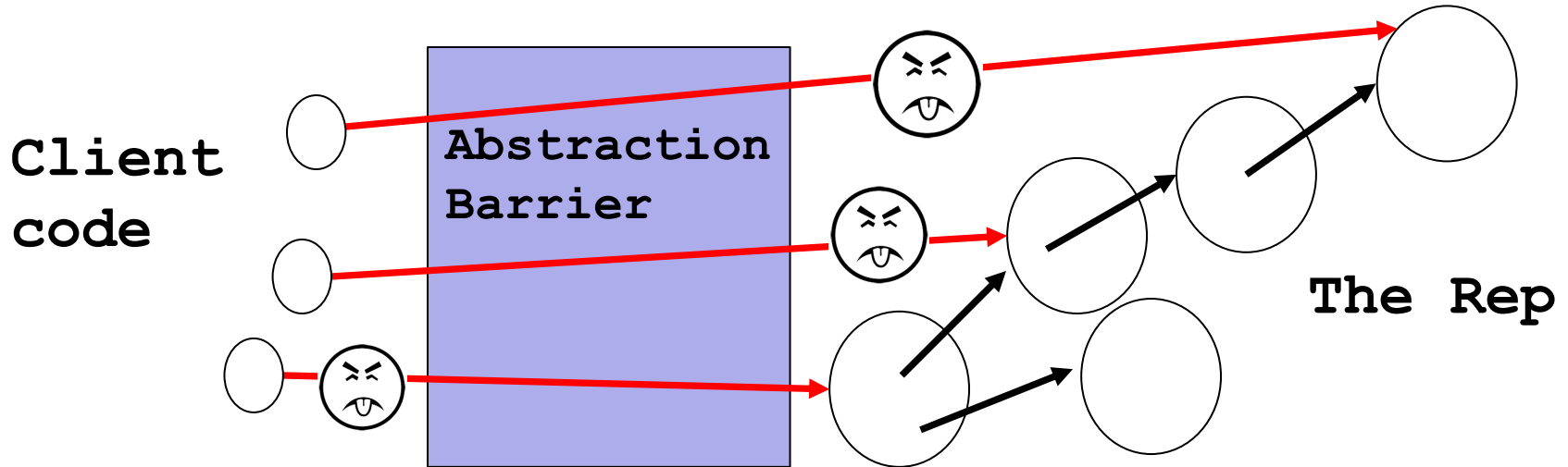
*Design* ADT implementations to make sure it doesn't happen

Treat rep exposure as a bug: *fix* your bugs

*Test* for it with *adversarial clients*:

- Pass values to methods and then mutate them
- Mutate values returned from methods

# private is not enough



- Making fields **private** does *not* suffice to prevent rep exposure
  - See our example
- So **private** is a hint to you: no aliases outside abstraction to references to mutable data reachable from **private** fields
- Two general ways to avoid representation exposure...



# Avoiding rep exposure (way #1)

One way to avoid rep exposure is to make **copies** of all data that cross the abstraction barrier

- **Copy in** [parameters that become part of the implementation]
- **Copy out** [results that are part of the implementation]

Examples of copying (assume **Point** is a mutable ADT):

```
class Line {  
    private Point s, e;  
    public Line(Point s, Point e) {  
        this.s = new Point(s.x,s.y);  
        this.e = new Point(e.x,e.y);  
    }  
    public Point getStart() {  
        return new Point(this.s.x,this.s.y);  
    }  
    ...  
}
```

copy in

copy out


# Need deep copying

“Shallow” copying is not enough

- Prevent any aliasing to mutable data inside/outside abstraction

What’s the bug (assuming `Point` is a mutable ADT)?

```
class PointSet {  
    private List<Point> points = ...  
    public List<Point> getElts() {  
        return new ArrayList<Point>(points) ;  
    }  
}
```



copy out?

Not in example: Also need deep copying on “copy in”

# Avoiding rep exposure (way #2)

One way to avoid rep exposure is to exploit the **immutability** of (other) ADTs the implementation uses

- Aliasing is no problem if nobody can change data
  - Have to mutate the rep to break the rep invariant

Examples (assuming `Point` is an *immutable* ADT):

```
class Line {  
    private Point s, e;  
    public Line(Point s, Point e) {  
        this.s = s;  
        this.e = e;  
    }  
    public Point getStart() {  
        return this.s;  
    }  
    ...  
}
```

# Why [not] immutability?

Several advantages of immutability

- Aliasing does not matter
- No need to make copies with identical contents
- Rep invariants cannot be broken
- Take CSE 341: Programming Languages for more!

Does require different designs (e.g., if `Point` immutable)

```
void raiseLine(double deltaY) {  
    this.s = new Point(s.x, s.y+deltaY);  
    this.e = new Point(e.x, e.y+deltaY);  
}
```

Immutable classes in Java libraries include `String`, `Character`, `Integer`, ...

# Deepness revisited

An immutable ADT must be immutable “all the way down”

- No references *reachable* to data that may be mutated


So combining our two ways to avoid rep exposure:

- Must copy-in, copy-out “all the way down” to immutable parts

# Back to getElts

Recall our initial rep-exposure example:

```
class CharSet {  
    // Rep invariant: elts has no nulls and no dups  
    private List<Character> elts = ...;  
  
    // returns: elts currently in the set  
    public List<Character> getElts() {  
        return new ArrayList<Character>(elts); }  
    ...  
}
```



copy out!

# An alternative

```
// returns: elts currently in the set
public List<Character> getElts() { // version 1
    return new ArrayList<Character>(elts); //copy out!
}

public List<Character> getElts() { // version 2
    return Collections.unmodifiableList<Character>(elts);
}
```

From the JavaDoc for `Collections.unmodifiableList`:

*Returns an unmodifiable view of the specified list. This method allows modules to provide users with "read-only" access to internal lists. Query operations on the returned list "read through" to the specified list, and attempts to modify the returned list... result in an `UnsupportedOperationException`.*

# The good news

```
public List<Character> getElts() { // version 2
    return Collections.unmodifiableList<Character>(elts);
}
```

Clients cannot *modify (mutate)* the rep

- So they cannot break the rep invariant

(For long lists,) more efficient than copy out

Uses standard libraries



# Caveat

```
public List<Character> getElts() { // version 1
    return new ArrayList<Character>(elts); //copy out!
}
```

```
public List<Character> getElts() { // version 2
    return Collections.unmodifiableList<Character>(elts);
}
```

The two implementations do not do the same thing!

- Both avoid allowing clients to break the rep invariant
- Both return a list containing the elements

But consider:

```
xs = s.getElts();
s.insert('a');
xs.contains('a');
```

Version 2 is *observing* an exposed rep, leading to different behavior

# Different specifications

Ambiguous spec: “returns a list containing the current set elements”

1. “returns a fresh mutable list containing the elements in the set  
*at the time of the call*”

versus

2. “returns read-only access to a list that the ADT  
*continues to update to hold the current elements in the set*”

3. A third spec weaker than both [but less simple and useful!]

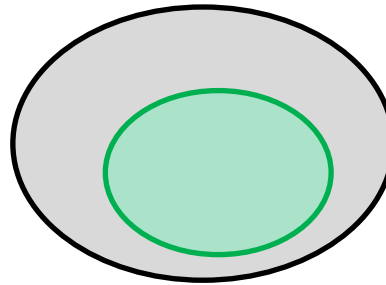
“returns a list containing the current set elements. *Behavior is unspecified (!) if client attempts to mutate the list or to access the list after the set’s elements are changed*”

Also note: Version 2’s spec also makes changing the rep later harder

- Only “simple” to implement with rep as a **List**

# Summary

- A data structure's **representation** allows **concrete values** that do not correspond to an **abstract value** allowed by the **ADT**
  - “gray area” ----->



- **Representation Invariant** describes what makes the concrete representation valid (green area)
- **checkRep()** method verifies that the rep is valid
- **Rep Exposure** occurs when a client can modify the rep
  - Never let this happen!!!!

# Closing

# Closing Announcements

- HW2 due Monday 10 pm
  - Start early!
  - Go to office hours today!
- Thank you for coming to class!
- Enjoy your weekend!