| Name | |
|------|--|
| | |

There are 9 questions worth a total of 110 points. Please budget your time so you get to all of the questions. Keep your answers brief and to the point.

The exam is closed book, closed notes, closed electronics, closed mouth, open mind.

Many of the questions have short solutions, even if the question is somewhat long. Don't be alarmed.

For all of the questions involving proofs, assertions, invariants, and so forth, you should assume that all numeric quantities are unbounded integers (i.e., overflow can not happen) and that integer division is truncating division as in Java, i.e., 5/3 evaluates to 1.

If you don't remember the exact syntax of some command or the format of a command's output, make the best attempt you can. We will make allowances when grading.

Relax, you are here to learn.

Please wait to turn the page until everyone is told to begin.

| Score / | 110 |
|---------|-----|
|---------|-----|

| 1. | / 12 | 6/ 12 |
|----|------|-------|
| 2. | / 12 | 7/ 12 |
| 3. | / 12 | 8/ 10 |
| 4. | / 12 | 9/ 12 |
| 5. | / 16 | |

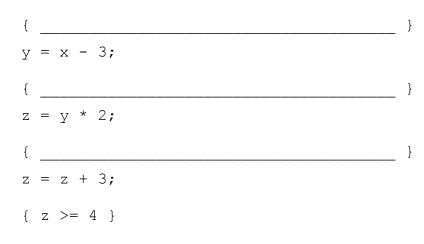
Remember: For all of the questions involving proofs, assertions, invariants, and so forth, you should assume that all numeric quantities are unbounded integers (i.e., overflow can not happen) and that integer division is truncating division as in Java, i.e., 5/3 => 1.

Question 1. (12 points) (Forward reasoning) Using forward reasoning, write an assertion in each blank space indicating what is known about the program state at that point, given the precondition and the previously executed statements. Your final answers should be simplified. Be as specific as possible, but be sure to retain all relevant information.

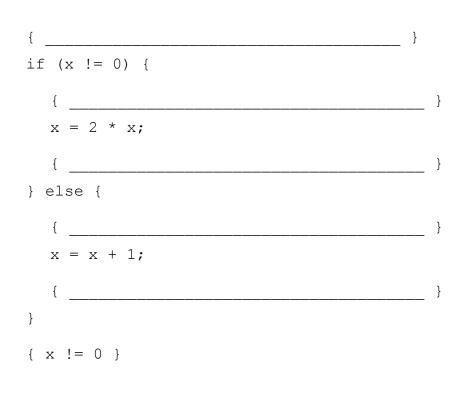
| (a) (5 points) { x != 0 } | |
|---------------------------------------|---|
| $y = x \star x;$ | |
| { | } |
| x = y - 1; | |
| { | } |
| x = x + y; | |
| { | } |
| (b) (7 points) { x > 3 && x < 10 } | |
| if $(x > y)$ | |
| { | } |
| y = x - 2; | |
| { | } |
| else | |
| { | } |
| y = y - x; | |
| { | } |
| | |

Question 2. (12 points) (assertions) Using backwards reasoning, find the weakest precondition for each sequence of statements and postcondition below. Insert appropriate assertions in each blank line. You should simplify your final answers if possible.

(a) (5 points)



(b) (7 points)



The next few questions concern the following partially complete Java class that was begun by one of the summer interns who left before finishing the job. (Not a UW intern, clearly.) The Department of Software Archeology and Reverse Engineering has turned to you for help.

We know that the code is supposed to implement a bag of strings, i.e., a set that allows duplicate elements, sometimes called a multiset. The representation uses an array to hold the elements and has an associated integer variable to record the size of the bag (the number of elements being used in the array). Presumably the array size will be adjusted as needed if (when?) new elements are added to the bag. Here's the code that we have:

```
import java.util.*;
public class StringBag {
 private int size; // # of strings in this bag
private String[] items; // the strings
  // constructor
  public StringBag(String[] vals) {
    size = vals.length;
    items = Arrays.copyOf(vals, size); // new array copy of vals
  }
  // delete strings with length > n
  public void deleteLongStrings(int n) {
    int k = 0;
    while (k < size) {
      if (items[k].length() > n) {
        items[k] = items[size-1];
        size = size -1;
      } else {
        k = k + 1;
      }
    }
  }
  // add string to bag (expand bag as needed) and return success
  public boolean add(String s) {
    // not implemented
    return false;
  }
}
```

In the following questions, assume that this code should work as currently written and that it is correct as far as it goes. This code does compile and execute without errors.

Answer questions about this code on the next few pages. You can remove this page from the exam for reference if you'd like.

Question 3. (12 points) (a) (3 points) Give a suitable abstract description of the class as would be written in the JavaDoc comment above the StringBag class heading.

(b) (5 points) Give a suitable Representation Invariant (RI) for this class. (Remember that this RI should be sufficient to guarantee that the existing code executes successfully.)

(c) (4 points) Give a suitable Abstraction Function (AF) for this class relating the RI to the abstract value of a StringBag.

Question 4. (12 points) Specification. None of the methods in the StringBag are specified properly. Below, supply proper JavaDoc comments for the constructor and deleteLongStrings methods for the code on previous pages. Leave any unneeded parts blank. The summary comments at the beginning of each JavaDoc block are supplied for you. Hint: the answers probably won't need all of this space.

```
/** Construct a new StringBag with contents from the
 *
    given String array.
 *
 * @param vals
 *
 *
 * @requires
 *
 *
  Qmodifies
 *
 *
   @effects
 *
 *
  Qthrows
 *
 * @returns
 *
 */
public StringBag(String[] vals) { constructor implementation omitted }
/** Delete long strings from this Stringbag.
 * @param n
 *
 *
  @requires
 *
 *
 *
   Qmodifies
 *
 *
 *
   @effects
 *
 * @throws
 *
 * @returns
 *
 * /
public void deleteLongStrings(int n) { implementation omitted }
```

Question 5. (16 points) Proof. The implementation of deleteLongStrings seems to be okay, but we'd like to be sure. For this problem, give a proof that the code works properly. You will need to provide appropriate assertions, pre- and post-conditions, and loop invariants for your proof. Write your proof in between the lines of code below

```
// delete strings with length > n
public void deleteLongStrings(int n) {
  int k = 0;
  while (k != size) {
    if (items[k].length() > n) {
      items[k] = items[size-1];
      size = size -1;
    } else {
      k = k + 1;
    }// end if
  } // end loop
```

}

Question 6. (12 points, 3 each) Testing. To increase our confidence that the code is correct, we need testing to complement proofs and analysis. For this question, describe four separate, distinct "black box" tests for the deleteLongStrings method that you proved correct on the previous page. For each test give the input values and expected result(s). You do not need to write JUnit tests or other Java code – just give a precise, concise description. Also, don't worry about what observer methods might exist – it's good enough to describe the abstract state of the set before and after the test.

(a)

(b)

(c)

(d)

Question 7. (12 points) Something to add. The Software Archeology department is happy with the work you've done so far. But they've discovered another client request that will require an addition to the StringBag class. The client would like us to add an observer method that returns an array with the Strings that are currently in the StringBag. We would like to add the following method:

```
// return the current strings in this StringBag to the caller
public String[] getItems() {
   return items;
}
```

(a) (4 points) Is this method correct? In other words, does it return the correct information to the client?

(b) (4 points) Are there any potential representation exposure or other problems with this method? If so, what can go wrong? If not, say so and give a brief reason.

(c) (4 points) If there are problems with this method (identified in parts (a) and/or (b)), describe how to fix them and still provide an observer method that supplies the information desired by the caller. Please describe briefly what needs to be done to fix the problems. You do not need to write any code, but you can if it helps illustrate your answer.

Question 8. (10 points) Comparing specifications. This question does not concern the StringBag ADT or any other code from the previous questions.

Here are parts of four possible specifications for a method that has a parameter n.

```
A. @param n
  @requires n % 2 = 0 && n > 0
  \operatorname{Qreturn} an integer > 0
B. @param n
  @requires n > 0
  \operatorname{Qreturn} an integer > 0
C. @param n
  @throws IllegalArgumentException if n % 2 != 0 or n <= 0</pre>
  \operatorname{Qreturn} an integer > 0
D. @param n
  @requires n > 0
  Qreturn an integer >= 0
(a) List all of the specification that are stronger than A.
(b) List all of the specification that are stronger than B.
(c) List all of the specification that are stronger than C.
(d) List all of the specification that are stronger than D.
(e) Is it possible for a single method to satisfy A and B? (yes or no)
```

(f) Is it possible for a single method to satisfy A and C? (yes or no) _____

Question 9. (12 points, 3 each) Overload? Override? You decide! Suppose we have the following class and method definitions.

```
class A {
  void p(int n) { System.out.println("A.p(int)"); }
  void p(String s) { System.out.println("A.p(String)"); }
  void q() { System.out.println("A.q()"); }
}
class B extends A {
  void p() { System.out.println("B.p()"); }
  void p(int n) { p("hello"); System.out.println("B.p(int)"); }
  void r(double d) { System.out.println("B.r(double)"); }
}
class C extends B {
  void p(String s) { System.out.println("C.p(String)"); }
  void q(int n) { System.out.println("C.q(int)"); }
}
```

For each of the following groups of statements, write down the output produced when the statements are executed or, if there is a compile-time or run-time error, explain in a sentence what is wrong.

- (a) C c1 = new C(); c1.p(17);
- (b) B b1 = new C(); b1.q(17);
- (c) B b2 = new B(); A a2 = b2; a2.p(17);
- (d) A a3 = new B(); B b3 = a3; b3.r(3.14);