Section 5: HW6 and Midterm

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(with material from Alex Mariakakis, Kellen Donohue, David Mailhot, and Hal Perkins)

Breadth-First Search (BFS)

Often used for discovering connectivity

Calculates the shortest path if and only if all edges have same positive or no weight

Depth-first search (DFS) is commonly mentioned with BFS

BFS looks "wide", DFS looks "deep"

Can also be used for discovery, but not the shortest path

BFS Pseudocode

START:

Q: <A>

Pop: A, Q: <>

Q: <B, C>

Pop: B, Q: <C>

Q: <C>

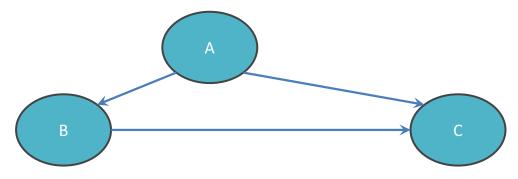
Pop: C, Q: <C>

Q: <>

DONE

Starting at A

Goal: Fully explore



Breadth-First Search with Cycle

START:

Q: <A>

Pop: A, Q: <>

Q:

Pop: B, Q: <>

Q: <C>

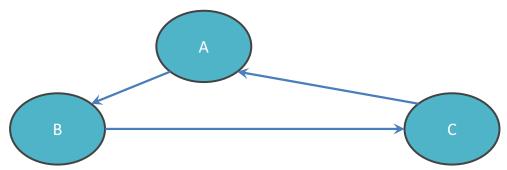
Pop: C, Q: <>

Q: <A>

NEVER DONE

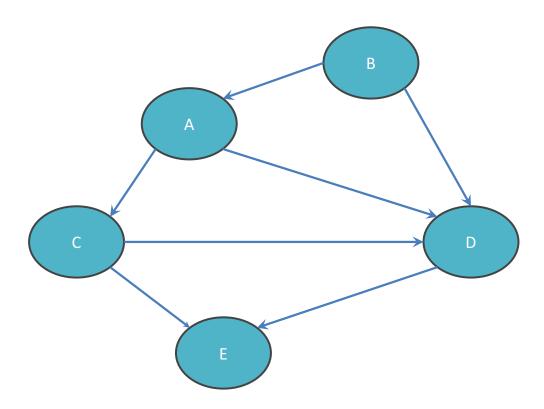
Starting at A

Goal: Fully Explore



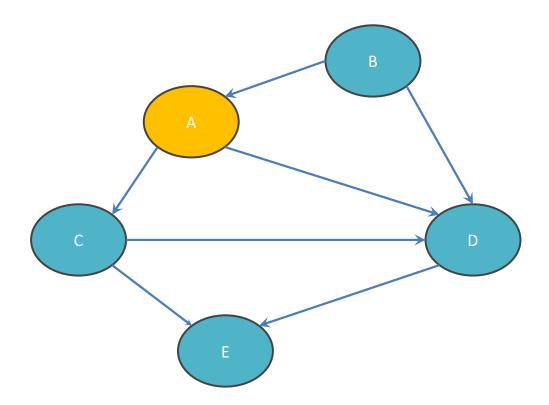
BFS Pseudocode





Q: <>

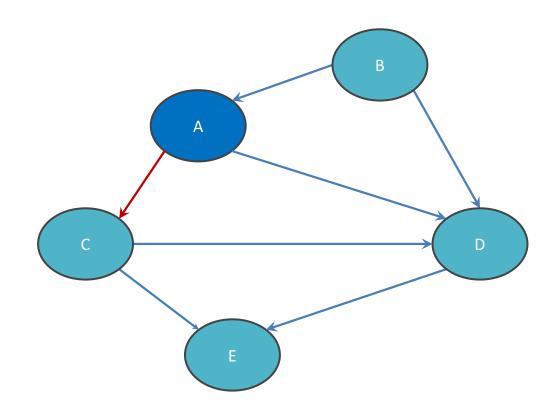
Q: <A>



Q: <>

Q: <A>

Q: <>

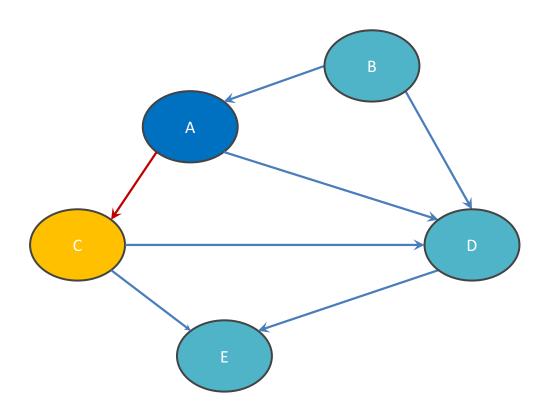


Q: <>

Q: <A>

Q: <>

Q: <C>



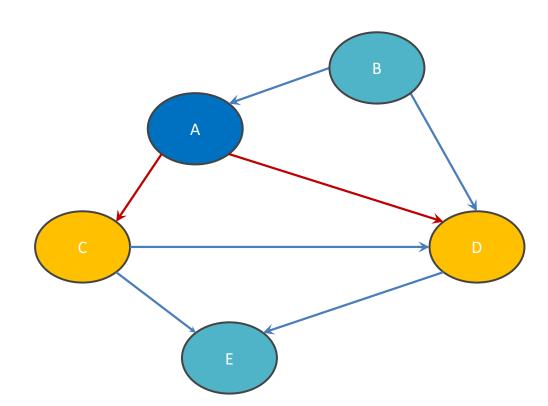


Q: <A>

Q: <>

Q: <C>

Q: <C ,D>





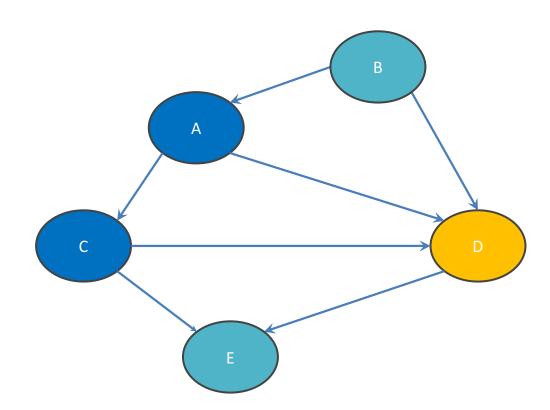
Q: <A>

Q: <>

Q: <C>

Q: <C ,D>

Q: <D>





Q: <A>

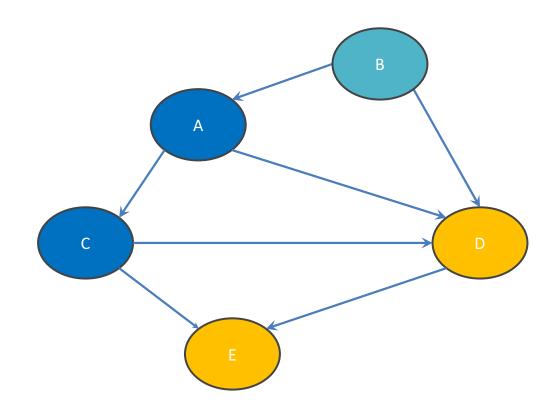
Q: <>

Q: <C>

Q: <C ,D>

Q: <D>

Q: <D, E>



Q: <>

Q: <A>

Q: <>

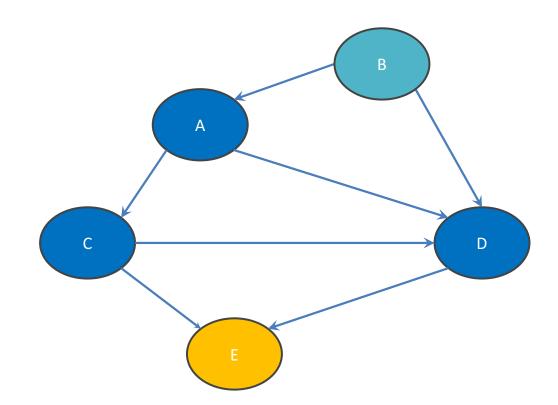
Q: <C>

Q: <C ,D>

Q: <D>

Q: <D, E>

Q: <E>



Q: <>

Q: <A>

Q: <>

Q: <C>

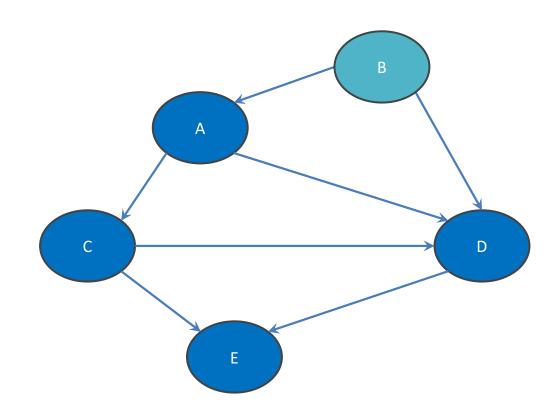
Q: <C ,D>

Q: <D>

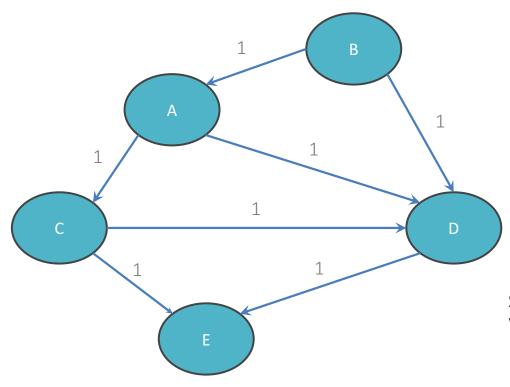
Q: <D, E>

Q: <E>

DONE



Shortest Paths with BFS

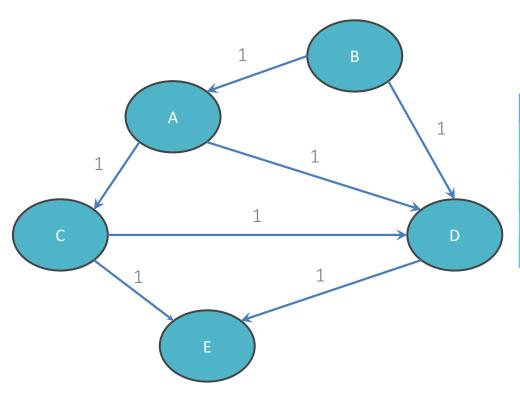


From Node B

Destination	Path	Cost
А	<b,a></b,a>	1
В		0
С	<b,a,c></b,a,c>	2
D		
E		

Shortest path to D? to E? What are the costs?

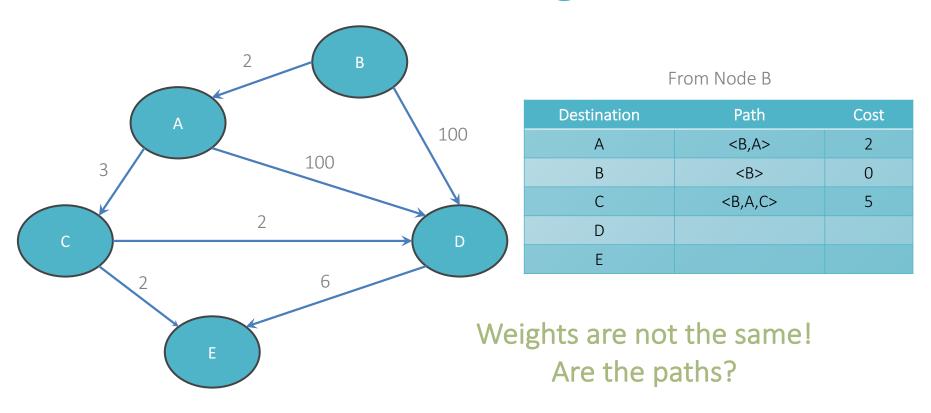
Shortest Paths with BFS



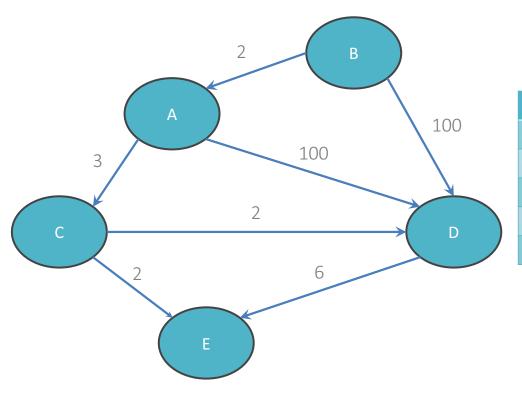
From Node B

Destination	Path	Cost
А	<b,a></b,a>	1
В		0
С	<b,a,c></b,a,c>	2
D	<b,d></b,d>	1
Е	<b,d,e></b,d,e>	2

Shortest Paths with Weights



Shortest Paths with Weights



From Node B

Destination	Path	Cost
А	<b,a></b,a>	2
В		0
С	<b,a,c></b,a,c>	5
D	<b,a,c,d></b,a,c,d>	7
E	<b,a,c,e></b,a,c,e>	7

Midterm review

Midterm topics

Reasoning about code

Identity & equality

Specification vs. Implementation

Testing

Abstract Data Types (ADTs)

```
{
z = x + y;
\{x > z - 3\}
y = z - 3;
\{x > y\}
```

```
{x > x + y - 3 \Rightarrow y < 3}

z = x + y;

{x > z - 3}

y = z - 3;

{x > y}
```

```
{
    p = a + b;
{
    q = a - b;
{p + q = 42}
```

```
{
p = a + b;
{p + a - b = 42}
q = a - b;
{p + q = 42}
```

```
{a + b + a - b = 42 \Rightarrow a = 21}

p = a + b;

{p + a - b = 42}

q = a - b;

{p + q = 42}
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

- A. @effects decreases balance by amount
- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>

Which specifications does this implementation meet?

```
I. void withdraw(int amount) {
      balance -= amount;
}
```

Another way to ask the question:

If the client does not know the implementation, will the method do what the client expects it to do based on the specification?

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

```
A. @effects decreases balance by amount 
    does exactly what the spec says
```

- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>

```
I. void withdraw(int amount) {
      balance -= amount;
}
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

- A. @effects decreases balance by amount
- ✓ does exactly what the spec says
- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- ✓ If the client follows the @requires
 precondition, the code will execute as expected

C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>

```
I. void withdraw(int amount) {
      balance -= amount;
}
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

- A. @effects decreases balance by amount
- ✓ does exactly what the spec says
- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- ✓ If the client follows the @requires precondition, the code will execute as expected
- C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>
- ✗ Method never throws an exception

```
I. void withdraw(int amount) {
      balance -= amount;
}
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

- A. @effects decreases balance by amount
- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>

```
II. void withdraw(int amount) {
    if (balance >= amount) balance -= amount;
}
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

```
A. @effects decreases balance by amount  balance does not always decrease
```

- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>

```
II. void withdraw(int amount) {
    if (balance >= amount) balance -= amount;
}
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

- A. @effects decreases balance by amount balance does not always decrease
- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- ✓ If the client follows the @requires precondition, the code will execute as expected

C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>

```
II. void withdraw(int amount) {
    if (balance >= amount) balance -= amount;
}
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

- A. @effects decreases balance by amount balance does not always decrease
- B. @requires amount >= 0 and amount <= balance @requires precondition, the code will execute as expected ✓

```
II. void withdraw(int amount) {
    if (balance >= amount) balance -= amount;
}
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

```
A. @effects decreases balance by amount
B. @requires amount >= 0 and amount <= balance
    @effects decreases balance by amount
C. @throws InsufficientFundsException
        if balance < amount
        @effects decreases balance by amount

Which specifications does this implementation meet?

III.void withdraw(int amount) {
        if (amount < 0) throw new IllegalArgumentException();
        balance -= amount;
    }
</pre>
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

```
A. @effects decreases balance by amount  balance does not always decrease
B. @requires amount >= 0 and amount <= balance @effects decreases balance by amount</li>
C. @throws InsufficientFundsException if balance < amount @effects decreases balance by amount</li>
Which specifications does this implementation meet?
III. void withdraw(int amount) { if (amount < 0) throw new IllegalArgumentException(); balance -= amount;</li>
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

```
A. @effects decreases balance by amount  balance does not always decrease
```

- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- ✓ If the client follows the @requires precondition, the code will execute as expected

C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>

```
III.void withdraw(int amount) {
     if (amount < 0) throw new IllegalArgumentException();
     balance -= amount;
   }</pre>
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

- A. @effects decreases balance by amount balance does not always decrease
- B. @requires amount >= 0 and amount <= balance @requires precondition, the code will execute as expected ✓
- - **X** Method throws wrong exception for wrong reason

```
III.void withdraw(int amount) {
     if (amount < 0) throw new IllegalArgumentException();
     balance -= amount;
   }</pre>
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

- A. @effects decreases balance by amount
- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>

```
IV. void withdraw(int amount) throws InsufficientFundsException {
    if (balance < amount) throw new InsufficientFundsException();
    balance -= amount;
}</pre>
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

```
A. @effects decreases balance by amount  balance does not always decrease
```

- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>

```
IV. void withdraw(int amount) throws InsufficientFundsException {
    if (balance < amount) throw new InsufficientFundsException();
    balance -= amount;
}</pre>
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

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A. @effects decreases balance by amount  balance does not always decrease
```

- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- ✓ If the client follows the @requires precondition, the code will execute as expected

C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>

```
IV. void withdraw(int amount) throws InsufficientFundsException {
    if (balance < amount) throw new InsufficientFundsException();
    balance -= amount;
}</pre>
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

```
A. @effects decreases balance by amount  balance does not always decrease
```

- B. @requires amount >= 0 and amount <= balance @requires precondition, the code will execute as expected ✓

```
IV. void withdraw(int amount) throws InsufficientFundsException {
    if (balance < amount) throw new InsufficientFundsException();
    balance -= amount;
}</pre>
```

Specifications 2

```
/**
 * An IntPoly is an immutable, integer-valued polynomial
 * with integer coefficients. A typical IntPoly value
 * is a_0 + a_1*x + a_2*x^2 + ... + a_n*x_n. An IntPoly
 * with degree n has coefficent a_n != 0, except that the
 * zero polynomial is represented as a polynomial of
 * degree 0 and a_0 = 0 in that case.
 */

public class IntPoly {
    int a[];
    // AF(this) = a has n+1 entries, and for each entry,
    // a[i] = coefficient a_i of the polynomial.
}
```

Specifications 2

```
/**
 * Return a new IntPoly that is the sum of this and other
 * @requires
 * @modifies
 * @effects
 * @return
 * @throws
 */
public IntPoly add(IntPoly other)
```

Specifications 2

```
/**
 * Return a new IntPoly that is the sum of this and other
 * @requires other != null
 * @modifies none
 * @effects none
 * @return a new IntPoly representing the sum of this and other
 * @throws none
 */
public IntPoly add(IntPoly other)
```

One of your colleagues is worried that this creates a potential representation exposure problem. Another colleague says there's no problem since an **IntPoly** is immutable. Is there a problem? Give a brief justification for your answer.

```
public class IntPoly {
    int a[];
    // AF(this) = a has n+1 entries, and for each entry,
    // a[i] = coefficient a_i of the polynomial.

    // Return the coefficients of this IntPoly
    public int[] getCoeffs() {
        return a;
    }
}
```

One of your colleagues is worried that this creates a potential representation exposure problem. Another colleague says there's no problem since an **IntPoly** is immutable. Is there a problem? Give a brief justification for your answer.

```
public class IntPoly {
    int a[];
    // AF(this) = a has n+1 entries, and for each entry,
    // a[i] = coefficient a_i of the polynomial.

    // Return the coefficients of this IntPoly
    public int[] getCoeffs() {
        return a; The return value is a reference to the same coefficient
        array stored in the IntPoly and the client code could
        alter those coefficients.
```

```
public class IntPoly {
    int a[];
    // AF(this) = a has n+1 entries, and for each entry,
    // a[i] = coefficient a_i of the polynomial.

    // Return the coefficients of this IntPoly
    public int[] getCoeffs() {
        return a;
    }
}
```

```
public int[] getCoeffs() {
    int[] copyA = new int[a.length];
    for (int i = 0; i < copyA.length; i++) {
        copyA[i] = a[i]
    }
    return copyA
}</pre>
```

We would like to add a method to this class that evaluates the **IntPoly** at a particular value x. In other words, given a value x, the method **valueAt(x)** should return $a_0 + a_1x + a_2x^2 + ... + a_nx^n$, where a_0 through an are the coefficients of this **IntPoly**.

For this problem, develop an implementation of this method and prove that your implementation is correct.

(see starter code on next slide)

```
/** Return the value of this IntPoly at point x */
public int valueAt(int x) {
    int val = a[0];
    int xk = 1;
    int k = 0;
    int n = a.length-1; // degree of this, n >=0
    {____}}
    while (k != n) {
        {_____}}
        xk = xk * x;
        {_____}}
        val = val + a[k+1]*xk;
        {_____}}
        k = k + 1;
        {_____}}
        return val;
}
```

```
/** Return the value of this IntPoly at point x */
public int valueAt(int x) {
    int val = a[0];
    int xk = 1;
    int k = 0;
    int n = a.length-1; // degree of this, n >=0
    {inv: xk = x^k && val = a[0] + a[1]*x + ... + a[k]*x^k}
    while (k != n) {
        {inv && k != n}
            xk = xk * x;
        {____}}
        val = val + a[k+1]*xk;
        {____}}
        k = k + 1;
        {____}}
    }
    return val;
}
```

```
/** Return the value of this IntPoly at point x */
public int valueAt(int x) {
    int val = a[0];
    int xk = 1;
    int k = 0;
    int n = a.length-1; // degree of this, n >=0
    {inv: xk = x^k && val = a[0] + a[1]*x + ... + a[k]*x^k}
    while (k != n) {
        {inv && k != n}
            xk = xk * x;
            {xk = x^(k+1) && val = a[0] + a[1]*x + ... + a[k]*x^k}
            val = val + a[k+1]*xk;
            {xk = x^(k+1) && val = a[0] + a[1]*x + ... + a[k+1]*x^(k+1)}
            k = k + 1;
            {_____}
}
return val;
}
```

```
/** Return the value of this IntPoly at point x */
public int valueAt(int x) {
   int val = a[0];
   int xk = 1;
   int k = 0;
   int n = a.length-1; // degree of this, n >=0
   while (k != n) {
       {inv && k != n}
       xk = xk * x;
       \{xk = x^{(k+1)} \& val = a[0] + a[1]*x + ... + a[k]*x^k\}
       val = val + a[k+1]*xk;
       \{xk = x^{(k+1)} \& val = a[0] + a[1]*x + ... + a[k+1]*x^{(k+1)}\}
       k = k + 1;
       {inv}
   return val;
```

```
/** Return the value of this IntPoly at point x */
public int valueAt(int x) {
   int val = a[0];
   int xk = 1;
   int k = 0;
   int n = a.length-1; // degree of this, n >=0
   while (k != n) {
       {inv && k != n}
       xk = xk * x;
       \{xk = x^{(k+1)} \& val = a[0] + a[1]*x + ... + a[k]*x^k\}
       val = val + a[k+1]*xk;
       \{xk = x^{(k+1)} \& val = a[0] + a[1]*x + ... + a[k+1]*x^{(k+1)}\}
       k = k + 1;
       {inv}
   \{inv \&\& k = n \Rightarrow val = a[0] + a[1]*x + ... + a[n]*x^n\}
   return val;
}
```

Suppose we are defining a class **StockItem** to represent items stocked by an online grocery store. Here is the start of the class definition, including the class name and instance variables:

```
public class StockItem {
    String name;
    String size;
    String description;
    int quantity;

    /* Construct a new StockItem */
    public StockItem(...);
}
```

A summer intern was asked to implement an equals function for this class that treats two StockItem objects as equal if their name and size fields match. Here's the result:

```
/** return true if the name and size fields match */
public boolean equals(StockItem other) {
    return name.equals(other.name) && size.equals(other.size);
}
```

This equals method seems to work sometimes but not always. Give an example showing a situation when it fails.

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/** return true if the name and size fields match */
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}
```

This equals method seems to work sometimes but not always. Give an example showing a situation when it fails.

```
Object s1 = new StockItem("thing", 1, "stuff", 1);
Object s2 = new StockItem("thing", 1, "stuff", 1);
System.out.println(s1.equals(s2));
```

A summer intern was asked to implement an equals function for this class that treats two StockItem objects as equal if their name and size fields match. Here's the result:

```
/** return true if the name and size fields match */
public boolean equals(StockItem other) { // equals is overloaded, not overridden
    return name.equals(other.name) && size.equals(other.size);
}
```

This equals method seems to work sometimes but not always. Give an example showing a situation when it fails.

```
Object s1 = new StockItem("thing", 1, "stuff", 1);
Object s2 = new StockItem("thing", 1, "stuff", 1);
System.out.println(s1.equals(s2));
```

Show how you would fix the equals method so it works properly (StockItems are equal if their names and sizes are equal)

/** return true if the name and size fields match */

Show how you would fix the equals method so it works properly (StockItems are equal if their names and sizes are equal)

```
/** return true if the name and size fields match */
@Override
public boolean equals(Object o) {
    if (!(o instanceof StockItem)) {
        return false;
    }
    StockItem other = (StockItem) o;
    return name.equals(other.name) && size.equals(other.size);
}
```

```
    return name.hashCode();
    return name.hashCode() * 17 + size.hashCode();
    return name.hashCode() * 17 + quantity;
    return quantity;
```

```
    return name.hashCode();  legal
    return name.hashCode() * 17 + size.hashCode();
    return name.hashCode() * 17 + quantity;
    return quantity;
```

```
    return name.hashCode();  legal
    return name.hashCode() * 17 + size.hashCode();  legal
    return name.hashCode() * 17 + quantity;
    return quantity;
```

```
    return name.hashCode();  legal
    return name.hashCode() * 17 + size.hashCode();  legal
    return name.hashCode() * 17 + quantity;  lllegal!
    return quantity;
```

```
    return name.hashCode();  legal
    return name.hashCode() * 17 + size.hashCode();  legal
```

- 3. return name.hashCode() * 17 + quantity;

 illegal!

not care about quantity

```
    return name.hashCode();  legal
    return name.hashCode() * 17 + size.hashCode();  legal
    return name.hashCode() * 17 + quantity;  llegal!
    return quantity;  llegal!
    The equals method does
```

Which implementation do you prefer?

```
public int hashCode() {
    return name.hashCode();
}

public int hashCode() {
    return name.hashCode()*17 + size.hashCode();
}
```

Which implementation do you prefer?

```
public int hashCode() {
    return name.hashCode();
}

same hashCode for StockItems that have different sizes
    as long as they have the same name, so it doesn't
    differentiate between different StockItems as well as (ii).

public int hashCode() {
    return name.hashCode()*17 + size.hashCode();
}
```