CSE 331
Software Design & Implementation

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Representation Invariants & Abstraction Functions

(Based on slides by Mike Ernst, Dan Grossman, David Notkin, Hal Perkins, Zach Tatlock)

Reminders

- Quiz 2 is due tonight
- HW4 due next Wednesday
  - start early
- Don't forget "ant validate"
  - (both in class and in industry)
- Remember that pseudocode is read by humans not computers
  - key is to be clear & complete
    - it's easy to assume the reader knows things they don't
  - also nice to be concise

Implementing a Data Abstraction (ADT)

To implement an ADT:

- select the representation of instances
- implement operations in terms of that representation

Choose a representation so that:

- it is possible to implement required operations
- the most frequently used operations are efficient / simple / …
  - abstraction allows the rep to change later
  - almost always better to start simple

Need to use reasoning to verify that the operations are correct

- two intellectual tools are helpful for this...

Connecting implementations to specs

For implementers / debuggers / maintainers of the implementation:

Representation Invariant: maps Object → boolean

- defines the set of valid concrete values
- must hold at all times (outside of mutators)
- **no object should *ever* violate the rep invariant**
  - such an object has no useful meaning

Abstraction Function: maps Object → abstract state

- says what the data structure *means* in vocabulary of the ADT
- **only defined** on objects meeting the rep invariant
- connects the concrete representation back to the specification
  - can check that the abstract value after each method meets the postcondition described in the specification

Example: Circle

```
/** Represents a mutable circle in the plane. For example,
  * it can be a circle with center (0,0) and radius 1. */
public class Circle {

  // Rep invariant: center != null and rad > 0
  private Point center;
  private double rad;

  // Abstraction function:
  // AF(this) = a circle with center at this.center
  //   and radius this.rad

  //  ...
}
```

Example: Circle 2

```
/** Represents a mutable circle in the plane. For example,
  * it can be a circle with center (0,0) and radius 1. */
public class Circle {

  // Rep invariant: center != null and edge != null
  //   and !center.equals(edge)
  private Point center, edge;

  // Abstraction function:
  // AF(this) = a circle with center at this.center
  //   and radius this.center.distanceTo(this.edge)

  //  ...
}
```

Example: Polynomial

```
/** An immutable polynomial with integer coefficients.
  * Examples include 0, 2x, and x + 3x^2 + 5x. */
public class IntPoly {

  // Rep invariant: coeffs != null
  private final int[] coeffs;

  // Abstraction function:
  // AF(this) = sum of this.coeffs[i] * x^i
  //   for i = 0 .. this.coeffs.length

  /** Returns the highest exponent with nonzero coefficient
    * or zero if none exists. */
  public int degree() { ... }

  //  ...
```

Example: Polynomial 2

```
/** An immutable polynomial with integer coefficients.
  * Examples include 0, 2x, and x + 3x^2 + 5x. */
public class IntPoly {

  // Rep invariant: terms != null
  private final List<IntTerm> terms;

  // Abstraction function:
  // AF(this) = sum of monomials in this.terms

  /** Returns the highest exponent with nonzero coefficient
    * or zero if none exists. */
  public int degree() { ... }

  //  ...
```

Example: Text File

Use case is writing an editor for an IDE:

MainActivity.java

```
1  package edu.washington.cs.testapp;
2
3  import android.support.constraint.ConstraintLayout;
4  import android.support.v7.app.AppCompatActivity;
5  import android.os.Bundle;
6  import android.widget.Button;
7  import android.widget.TextView;
8
9  public class MainActivity extends AppCompatActivity {
10
11     @Override
12     protected void onCreate(Bundle savedInstanceState) {
13         super.onCreate(savedInstanceState);
14         setContentView(R.layout.activity_main);
15
16         Button b = (Button) findViewById(R.id.my_btn);
17         //...
18     }
19 }
```

Example: Text File

Overview: telling users how to think about what this is

Option 1: sequence of characters & colors
Option 2: sequence of lines, each of which is a...
sequence of characters & colors

Both will probably require a method to take (line,col) to character

Key difference:

- Option 1 suggests you can remove, e.g., chars 100–200, which may span multiple lines
- That is not natural in Option 2

(Option 1 makes more sense for Microsoft Word.)

Example: Text File

Will use a sequence of lines.

What is each **line**?

Option 1: pair (sequence of characters, sequence of colors)

Option 2: sequence of pairs (character, color)

Option 3: sequence of pairs (sequence of characters, color)

Key differences:

- Option 1 must make clear that the sequences are same length
- Option 1 & 2 should let you insert (char, color) at given column
- Option 3 should let you find the (text, color) token containing a given column and then change its text to include a new char

Example: Text File

```
// Overview: Represents a text file, which is a sequence
// of lines of text. Each line of text is a sequence of
// (character, color) pairs.
//
// Example: [[(“a”, black), (“b”, red)], [(“c”, green)]]
// is the text:
//   ab
//   c
// (on two lines), where a is black, b is red, & c is green
public class TextFile {

  //  ...

}
```

Example: Text File

How would we actually represent this?

Probably okay to store lines in an array:

- most files have < 10k lines, so copying is not too expensive
- most characters are inserted into existing lines not creating new
- (always better to start simple... can change this later)

Example: Text File

How would we actually represent this?

Probably not okay to make each character an object

- object over head is at least 10 bytes per object
- 20 bytes * 10k lines * 50 characters = 10 Mb
- 100 files = 1 Gb = unhappy users

Instead store characters and colors in arrays

Old trick: have two arrays

- one is the beginning of the line
- one is the end of the line in reverse order
- easy to add new characters at the split between parts

Example: Text File

```
// Overview: Represents one line of the text file...
public class Line {

  // Representation invariant: all arrays are non-null and
  // and prefixCharsLen + suffixCharsLen equals
  //     prefixColorsLen + suffixColorsLen
  // and 0 <= prefixCharsLen <= prefixChars.length and ...
  private char[] prefixChars, suffixChars;
  private int[] prefixColors, suffixColors;
  private int prefixCharsLen, suffixCharsLen;
  private int prefixColorsLen, suffixColorsLen;

  // Abstraction function: AF(this) = zip sum of
  //   prefixChars[0..prefixCharsLen] + reverse(suffixChars[0..suffixCharsLen]) and
  //   prefixColors[0..prefixColorsLen] + reverse(suffixColors[0..suffixColorsLen])
  // (I.e., the list of pairs (char, color), where the i-th
  //  char is paired with the i-th color.)

  // ...
```

Example: CharSet ADT

```
// Overview: A CharSet is a finite mutable set of Characters

// @effects: creates a fresh, empty CharSet
public CharSet() {…}

// @modifies: this
// @effects: this_post = this_pre + {c}
public void insert(Character c) {…}

// @modifies: this
// @effects: this_post = this_pre - {c}
public void delete(Character c) {…}

// @return: (c in this)
public boolean member(Character c) {…}

// @return: cardinality of this
public int size() {…}
```

An implementation: Is it right?

```
class CharSet {
  private List<Character> elts =
      new ArrayList<Character>();
  public void insert(Character c) {
    elts.add(c);
  }
  public void delete(Character c) {
    elts.remove(c);
  }
  public boolean member(Character c) {
    return elts.contains(c);
  }
  public int size() {
    return elts.size();
  }
}
```

An implementation: Is it right?

```
class CharSet {
  private List<Character> elts =
      new ArrayList<Character>();
  public void insert(Character c) {
    elts.add(c);
  }
  public void delete(Ch
    elts.remove(c);
  }
  public boolean membe
    return elts.contai
  }
  public int size() {
    return elts.size()
  }
}
```

```
CharSet s = new CharSet();
Character a = new Character('a');
s.insert(a);
s.insert(a);
s.delete(a);
if (s.member(a))
    System.out.print("wrong");
else
    System.out.print("right");
```

An implementation: Is it right?

```
class CharSet {
  private List<Character> elts =
      new ArrayList<Character>();
  public void insert(Character c) {
    elts.add(c);
  }
  public void delete(Ch
    elts.remove(c);
  }
  public boolean membe
    return elts.contai
  }
  public int size() {
    return elts.size()
  }
}
```

```
CharSet s = new CharSet();
Character a = new Character('a');
s.insert(a);
s.insert(a);
s.delete(a);
if (s.member(a))
    System.out.print("wrong");
else
    System.out.print("right");
```

Where is the error?

Where Is the Error?

- Answer this and you know what to fix
- *Perhaps* **`delete`** is wrong
  - should remove all occurrences?
- *Perhaps* **`insert`** is wrong
  - should not insert a character that is already there?
- The representation invariant tells us which is correct
  - this is how we document our choice for "the right answer"

The representation invariant

- Defines data structure well-formedness
- Must hold before and after every **`CharSet`** operation
- Operations (methods) may depend on it
- Write it like this:

```
class CharSet {
    // Rep invariant:
    //   elts has no nulls and no duplicates
    private List<Character> elts = …
    …
```

Or, more formally (if you prefer):

for all indices i of elts, we have elts.elementAt(i) ≠ null

for all indices i, j of elts with i != j,

we have ! elts.elementAt(i).equals(elts.elementAt(j))

Now we can locate the error

```
// Rep invariant:
//   elts has no nulls and no duplicates

public void insert(Character c) {
  elts.add(c);
}

public void delete(Character c) {
  elts.remove(c);
}
```

Another example

```
class Account {
   private int balance;
   // history of all transactions
   private List<Transaction> transactions;
   …
}
```

Real-world constraints:

- Balance ≥ 0
- Balance = Σ_i transactions.get(i).amount

Implementation-related constraints:

- Transactions ≠ null
- No nulls in transactions

Checking rep invariants

Should you write code to check that the rep invariant holds?

- Yes, if it's inexpensive [depends on the invariant]
- Yes, for debugging [even when it's expensive]
- Often hard to justify turning the checking off
  - better argument is removing clutter (improve understandability)
- Some private methods need not check (Why?)

A great debugging technique:

Design your code to catch bugs by implementing and using a function to check the rep-invariant

Checking the rep invariant

Rule of thumb: check on entry *and* on exit (why?)

```
public void delete(Character c) {
  checkRep();
  elts.remove(c);

  // Is this guaranteed to get called?
  // (could guarantee it with a finally block)
  checkRep();
}
…
/** Verify that elts contains no duplicates. */
private void checkRep() {
  for (int i = 0; i < elts.size(); i++) {
    assert elts.indexOf(elts.elementAt(i)) == i;
  }
}
```

Practice *defensive programming*

- You **will** make mistakes
  - if you haven't made many yet, you haven't written enough code
  - "No physician is really good before he's killed a few patients" – Hindu Proverb
- Question is not: will you make mistakes? You will.
- Question is: will you **catch** those mistakes before customers do?
- Write and incorporate code designed to catch the errors you make
  - check rep invariant on entry and exit (of mutators)
  - check preconditions (don't trust other programmers)
  - check postconditions (don't trust yourself either)
- Checking the rep invariant helps *discover* errors while testing
- Reasoning about the rep invariant helps *discover* errors while coding

Practice *defensive programming*

- Checking pre- and post-conditions and rep invariants is one tip
- More of these in Effective Java
  - Reading Quiz #2 focuses on these

- In particular, focus on defensive programming against subtle bugs
  - obvious bugs (e.g. crashing every time) will be caught in testing
  - subtle bugs that only occasionally cause problems can sneak out
  - be especially defensive against these
  - tips in Reading Quiz #2 mainly combat these

Listing the elements of a CharSet

Consider adding the following method to **`CharSet`**

```
// returns: a List containing the members of this
public List<Character> getElts();
```

Consider this implementation:

```
// Rep invariant: elts has no nulls and no dups
private List<Character> elts;
public List<Character> getElts() { return elts; }
```

Does the implementation of **`getElts`** preserve the rep invariant?

Listing the elements of a CharSet

Consider adding the following method to **`CharSet`**

```
// returns: a List containing the members of this
public List<Character> getElts();
```

Consider this implementation:

```
// Rep invariant: elts has no nulls and no dups
private List<Character> elts;
public List<Character> getElts() { return elts; }
```

Does the implementation of **`getElts`** preserve the rep invariant?

Can't say!

Representation exposure

Consider this client code (outside the **`CharSet`** implementation):

```
CharSet s = new CharSet();
Character a = new Character('a');
s.insert(a);
s.getElts().add(a);
s.delete(a);
if (s.member(a)) …
```

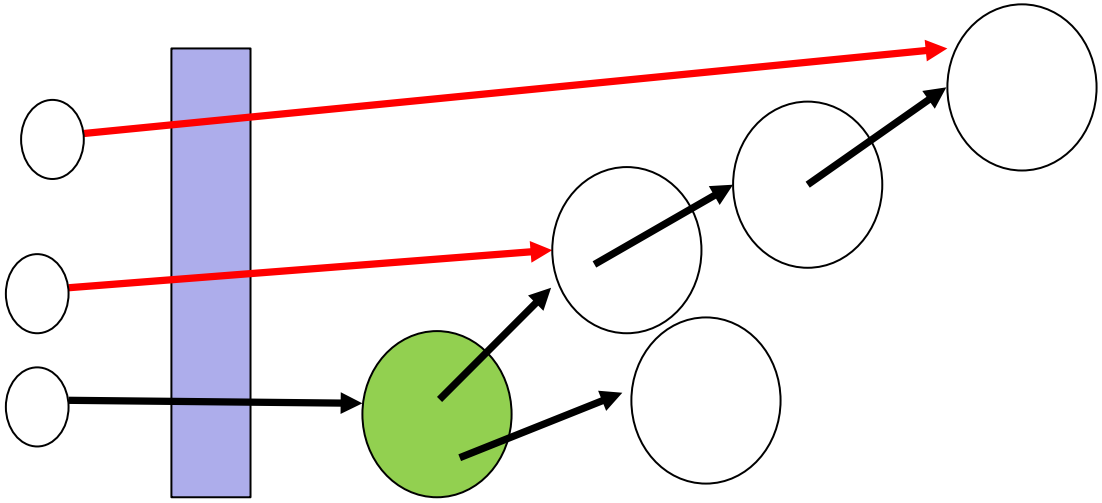
- Representation exposure is external access to the rep
- Representation exposure is almost always **EVIL**
  - can cause bugs that will be **very hard to detect**
- Rule #1: Don't do it!
- Rule #2: If you do it, document it clearly and then feel guilty about it!

Avoiding representation exposure

- *Understand* what representation exposure is
- *Design* ADT implementations to make sure it doesn't happen
- Treat rep exposure as a bug: *fix* your bugs
  - absolutely must avoid in libraries with many clients
  - can allow (but feel guilty) for code with few clients
- *Test* for it with *adversarial clients:*
  - pass values to methods and then mutate them
  - mutate values returned from methods

`private` is not enough

- Making fields **`private`** does *not* suffice to prevent rep exposure
  - see our example
  - issue is ***aliasing of mutable data outside the abstraction***



- So **`private`** is a hint to you: no aliases outside abstraction to references to mutable data reachable from **`private`** fields
- Two general ways to avoid representation exposure…

Avoiding rep exposure (way #1)

- One way to avoid rep exposure is to make copies of all data that cross the abstraction barrier
  - Copy in [parameters that become part of the implementation]
  - Copy out [results that are part of the implementation]

- Examples of copying (assume **`Point`** is a mutable ADT):

```
class Line {
   private Point s, e;
   public Line(Point s, Point e) {
      this.s = new Point(s.x,s.y);
      this.e = new Point(e.x,e.y);
   }
   public Point getStart() {
      return new Point(this.s.x,this.s.y);
   }
   …
```

Need deep copying

- "Shallow" copying is not enough
  - prevent any aliasing to mutable data inside/outside abstraction

- What's the bug (assuming **`Point`** is a mutable ADT)?

```
class PointSet {
   private List<Point> points = …
   public List<Point> getElts() {
      return new ArrayList<Point>(points);
   }
}
```

- Not in example: Also need deep copying on "copy in"

Avoiding rep exposure (way #2)

- One way to avoid rep exposure is to exploit the immutability of (other) ADTs the implementation uses
  - aliasing is no problem if nobody can change data
    - have to mutate the rep to break the rep invariant
- Examples (assuming **`Point`** is an *immutable* ADT):

```
class Line {
   private Point s, e;
   public Line(Point s, Point e) {
      this.s = s;
      this.e = e;
   }
   public Point getStart() {
      return this.s;
   }
   …
```

Why [not] immutability?

- Several advantages of immutability
  - aliasing does not matter
  - no need to make copies with identical contents
  - rep invariants cannot be broken
  - see CSE341 for more!

- Does require different designs (e.g., if **`Point`** immutable)

```
void raiseLine(double deltaY) {
    this.s = new Point(s.x, s.y+deltaY);
    this.e = new Point(e.x, e.y+deltaY);
}
```

- Immutable classes in Java libraries include **`String`**, **`Character`**, **`Integer`**, …

Deepness, redux

- An immutable ADT must be immutable "all the way down"
  - No references *reachable* to data that may be mutated

- So combining our two ways to avoid rep exposure:
  - Must copy-in, copy-out "all the way down" to immutable parts

Back to `getElts`

Recall our initial rep-exposure example:

```
class CharSet {
  // Rep invariant: elts has no nulls and no dups
  private List<Character> elts = …;

  // returns: elts currently in the set
  public List<Character> getElts() {
    return new ArrayList<Character>(elts); //copy out!
  }
  …
}
```

An alternative

```
// returns: elts currently in the set
public List<Character> getElts() { // version 1
  return new ArrayList<Character>(elts);//copy out!
}

public List<Character> getElts() { // version 2
  return Collections.unmodifiableList(elts);
}
```

From the JavaDoc for **`Collections.unmodifiableList`**:

Returns an unmodifiable view of the specified list. This method allows modules to provide users with "read-only" access to internal lists. Query operations on the returned list "read through" to the specified list, and attempts to modify the returned list… result in an **`UnsupportedOperationException`**.

The good news

```
public List<Character> getElts() { // version 2
  return Collections.unmodifiableList(elts);
}
```

- Clients cannot *modify (mutate)* the rep
  - cannot break the rep invariant
- (For long lists,) more efficient than copy out
- Uses standard libraries

The bad news

```
public List<Character> getElts() { // version 1
 return new ArrayList<Character>(elts);//copy out!
}

public List<Character> getElts() { // version 2
 return Collections.unmodifiableList(elts);
}
```

The two implementations do not do the same thing!

- both avoid allowing clients to break the rep invariant
- both return a list containing the elements

But consider:

```
xs = s.getElts();
s.insert('a');
xs.contains('a');
```

Version 2 is *observing* an exposed rep, leading to different behavior

Different specifications

Ambiguity of "returns a list containing the current set elements"

"returns a fresh mutable list containing the elements in the set *at the time of the call*"

versus

"returns read-only access to a list that the ADT *continues to update to hold the current elements in the set*"

A third spec weaker than both [but less simple and useful!]

"returns a list containing the current set elements. *Behavior is unspecified (!) if* client attempts to mutate the list or to access the list after the set's elements are changed"

Also note: Version 2's spec also makes changing the rep later harder

- only "simple" to implement with rep as a `List`

Suggestions

Best options for implementing `getElts()`

- if O(n) time is acceptable for relevant use cases, copy the list
  - safest option
  - best option for changeability
- if O(1) time is required, then return an unmodifiable list
  - prevents breaking rep invariant
  - clearly document that behavior is unspecified after mutation
  - ideally, write a your own unmodifiable view of the list that throws an exception on all operations after mutation
- if O(1) time is required and there is no unmodifiable version and you don't have time to write one, expose rep and feel guilty