# CSE 331 Software Design & Implementation

Hal Perkins Spring 2017 Abstraction Functions

# Connecting implementations to specs

#### **Representation Invariant**: maps Object $\rightarrow$ boolean

- Indicates if an instance is *well-formed*
- Defines the set of valid concrete values
- Only values in the valid set make sense as implementations of an abstract value
- For implementors/debuggers/maintainers of the abstraction: no object should ever violate the rep invariant
  - Such an object has no useful meaning

#### **Abstraction Function**: maps Object $\rightarrow$ abstract value

- What the data structure *means* as an abstract value
- How the data structure is to be interpreted
- Only defined on objects meeting the rep invariant
- For implementors/debuggers/maintainers of the abstraction:
   Each procedure should meet its spec (abstract values) by "doing the right thing" with the concrete representation

#### Rep inv. constrains structure, not meaning

An implementation of **insert** that preserves the rep invariant:

```
public void insert(Character c) {
    Character cc = new Character(encrypt(c));
    if (!elts.contains(cc))
        elts.addElement(cc);
    }
    public boolean member(Character s = new CharSet();
    s.insert('a');
    if (s.member('a'))
        ...
}
```

Program is still wrong

- Clients observe incorrect behavior
- What client code exposes the error?
- Where is the error?
- We must consider the *meaning*
- The abstraction function helps us

#### Abstraction function: rep $\rightarrow$ abstract value

The abstraction function maps the concrete representation to the abstract value it represents
AF: Object → abstract value
AF(CharSet this) = { c | c is contained in this.elts }
"set of Characters contained in this.elts"

Not executable because abstract values are "just" conceptual

The abstraction function lets us reason about what [concrete] methods do in terms of the clients' [abstract] view

### Abstraction function and insert

Goal is to satisfy the specification of insert:

// modifies: this
// effects: this<sub>post</sub> = this<sub>pre</sub> U {c}
public void insert (Character c) {...}

The AF tells us what the rep means, which lets us place the blame

AF(CharSet this) = { c | c is contained in this.elts }

Consider a call to **insert**:

On *entry*, meaning is AF(this<sub>pre</sub>) = elts<sub>pre</sub> On *exit*, meaning is AF(this<sub>post</sub>) = AF(this<sub>pre</sub>) U {encrypt('a')}

What if we used this abstraction function instead? AF(this) = { c | encrypt(c) is contained in this.elts } = { decrypt(c) | c is contained in this.elts } UW CSE 331 Spring 2017

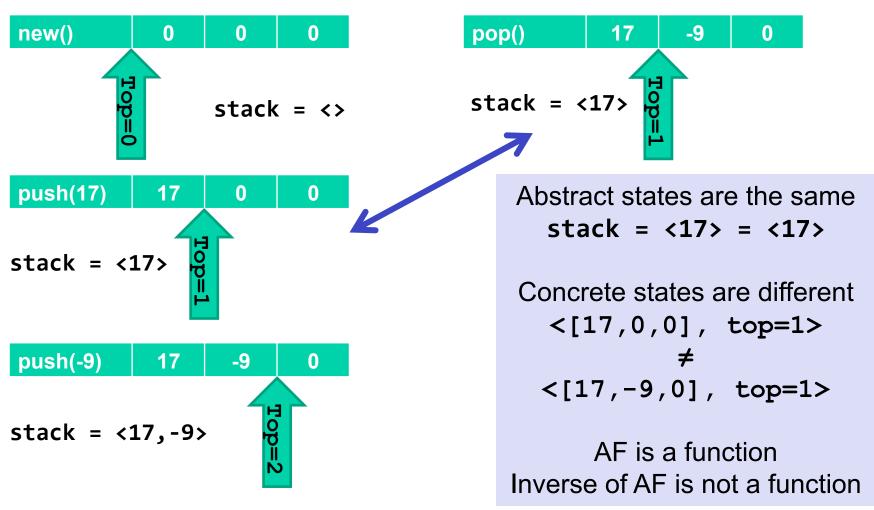
## The abstraction function is a function

Why do we map concrete to abstract and not vice versa?

- It's not a function in the other direction
  - Example: lists [a,b] and [b,a] might each represent the set {a,b}
- It's not as useful in the other direction
  - Purpose is to reason about whether our methods are manipulating concrete representations correctly in terms of the abstract specifications

#### Abstract stack with array and "top" index implementation

### Stack AF example

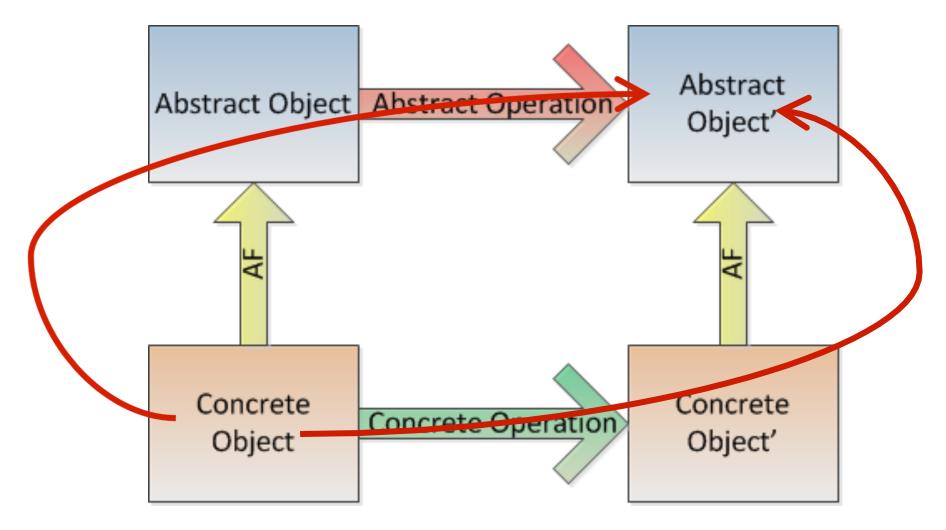


### **Benevolent side effects**

Different implementation of member: boolean member(Character c1) { int i = elts.indexOf(c1); if (i == -1) return false; // move-to-front optimization Character c2 = elts.elementAt(0); elts.set(0, c1); elts.set(i, c2); return true; }

- Move-to-front speeds up repeated membership tests
- Mutates rep, but does not change abstract value
  - AF maps both reps to the same abstract value
    - Precise reasoning/explanation for "clients can't tell"

#### For any correct operation...



# Writing an abstraction function

Domain: all representations that satisfy the rep invariant Range: can be tricky to denote

- For mathematical entities like sets: easy
- For more complex abstractions: give names to specification
- AF defines the value of each "specification field"
  - (Course notes have examples of complex AFs with many spec. fields, but it's possible to be too complex – go for simple, correct, understandable whenever possible)

Overview section of the specification should provide a notation for writing abstract values

- Could implement a method for printing in this notation
  - Useful for debugging
  - Often a good choice for toString

## Data Abstraction: Summary

Rep invariant

Which concrete values represent abstract values

Abstraction function

- For each concrete value, which abstract value it represents

Together, they modularize the implementation

- Neither one is part of the ADT's specification
- Both are needed to reason that an implementation satisfies the specification

In practice, representation invariants are documented more often and more carefully than abstraction functions

A more widely understood and appreciated concept