Section 7: Midterm

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(with material from Alex Mariakakis, Kellen Donohue, David Mailhot, and Hal Perkins)

Midterm review

Midterm topics

Reasoning about code

Subtypes & subclasses

Specification vs. Implementation

Exceptions & assertions

Abstract Data Types (ADTs)

Identity & equality

Testing

```
\{x > x + y - 3 \Rightarrow y < 3\}
z = x + y;
\{x > z - 3\}
y = z - 3;
\{x > y\}
```

```
{
p = a + b;
{p + a - b = 42}
q = a - b;
{p + q = 42}
```

```
{a + b + a - b = 42 \Rightarrow a = 21}

p = a + b;

{p + a - b = 42}

q = a - b;

{p + q = 42}
```

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

- A. @effects decreases balance by amount
- B. @requires amount >= 0 and amount <= balance
 @effects decreases balance by amount</pre>
- C. @throws InsufficientFundsException
 if balance < amount
 @effects decreases balance by amount</pre>

Which specifications does this implementation meet?

```
I. void withdraw(int amount) {
      balance -= amount;
}
```

Another way to ask the question:

If the client does not know the implementation, will the method do what the client expects it to do based on the specification?

Suppose we have a BankAccount class with instance variable balance. Consider the following specifications:

- A. @effects decreases balance by amount ✓ does exactly what the spec says
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✓ If the client follows the @requires
precondition, the code will execute as expected

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    if (balance >= amount) balance -= amount;
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- **X** Method never throws an exception

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IV. void withdraw(int amount) throws InsufficientFundsException {
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```

```
/**
 * An IntPoly is an immutable, integer-valued polynomial
 * with integer coefficients. A typical IntPoly value
 * is a_0 + a_1*x + a_2*x^2 + ... + a_n*x_n. An IntPoly
 * with degree n has coefficent a_n != 0, except that the
 * zero polynomial is represented as a polynomial of
 * degree 0 and a 0 = 0 in that case.
 */
public class IntPoly {
    int a[];
    // AF(this) = a has n+1 entries, and for each entry,
    // a[i] = coefficient a_i of the polynomial.
```

```
/**
 * Return a new IntPoly that is the sum of this and other
 * @requires
 * @modifies
 * @effects
 * @return
 * @throws
 */
public IntPoly add(IntPoly other)
```

```
/**
 * Return a new IntPoly that is the sum of this and other
 * @requires other != null
 * @modifies none
 * @effects none
 * @return a new IntPoly representing the sum of this and other
 * @throws none
 */
public IntPoly add(IntPoly other)
```

One of your colleagues is worried that this creates a potential representation exposure problem. Another colleague says there's no problem since an **IntPoly** is immutable. Is there a problem? Give a brief justification for your answer.

```
public class IntPoly {
    int a[];
    // AF(this) = a has n+1 entries, and for each entry,
    // a[i] = coefficient a_i of the polynomial.

    // Return the coefficients of this IntPoly
    public int[] getCoeffs() {
        return a;
    }
}
```

One of your colleagues is worried that this creates a potential representation exposure problem. Another colleague says there's no problem since an **IntPoly** is immutable. Is there a problem? Give a brief justification for your answer.

If there is a representation exposure problem, give a new or repaired implementation of **getCoeffs** that fixes the problem but still returns the coefficients of the **IntPoly** to the client. If it saves time you can give a precise description of the changes needed instead of writing the detailed Java code.

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public class IntPoly {
    int a[];
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```
public int[] getCoeffs() {
    int[] copyA = new int[a.length];
    for (int i = 0; i < copyA.length; i++) {
        copyA[i] = a[i]
    }
    return copyA
}</pre>
```

If there is a representation exposure problem, give a new or repaired implementation of **getCoeffs** that fixes the problem but still returns the coefficients of the **IntPoly** to the client. If it saves time you can give a precise description of the changes needed instead of writing the detailed Java code.

We would like to add a method to this class that evaluates the **IntPoly** at a particular value x. In other words, given a value x, the method **valueAt(x)** should return $a_0 + a_1x + a_2x^2 + ... + a_nx^n$, where a_0 through an are the coefficients of this **IntPoly**.

For this problem, develop an implementation of this method and prove that your implementation is correct.

(see starter code on next slide)

```
/** Return the value of this IntPoly at point x */
public int valueAt(int x) {
    int val = a[0];
    int xk = 1;
    int k = 0;
    int n = a.length-1; // degree of this, n >=0
    while (k != n) {
        xk = xk * x;
        val = val + a[k+1]*xk;
        k = k + 1;
    return val;
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    {inv: xk = x^k & val = a[0] + a[1]*x + ... + a[k]*x^k}
    while (k != n) {
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    while (k != n) {
        {inv && k != n}
        xk = xk * x;
        val = val + a[k+1]*xk;
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    while (k != n) {
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        xk = xk * x;
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    while (k != n)  {
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        xk = xk * x;
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        k = k + 1;
        {inv}
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        val = val + a[k+1]*xk;
        \{xk = x^{(k+1)} \& val = a[0] + a[1]*x + ... + a[k+1]*x^{(k+1)}\}
        k = k + 1;
        {inv}
    \{inv \&\& k = n \Rightarrow val = a[0] + a[1]*x + ... + a[n]*x^n\}
    return val;
```

Suppose we are defining a class **StockItem** to represent items stocked by an online grocery store. Here is the start of the class definition, including the class name and instance variables:

```
public class StockItem {
    String name;
    String size;
    String description;
    int quantity;

    /* Construct a new StockItem */
    public StockItem(...);
}
```

A summer intern was asked to implement an equals function for this class that treats two StockItem objects as equal if their name and size fields match. Here's the result:

```
/** return true if the name and size fields match */
public boolean equals(StockItem other) {
    return name.equals(other.name) && size.equals(other.size);
}
```

This equals method seems to work sometimes but not always. Give an example showing a situation when it fails.

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Object s1 = new StockItem("thing", 1, "stuff", 1);
Object s2 = new StockItem("thing", 1, "stuff", 1);
System.out.println(s1.equals(s2));
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```
/** return true if the name and size fields match */
public boolean equals(StockItem other) { // equals is overloaded, not overridden
    return name.equals(other.name) && size.equals(other.size);
}
```

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Object s1 = new StockItem("thing", 1, "stuff", 1);
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Show how you would fix the equals method so it works properly (StockItems are equal if their names and sizes are equal)

/** return true if the name and size fields match */

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```
/** return true if the name and size fields match */
@Override
public boolean equals(Object o) {
    if (!(o instanceof StockItem)) {
        return false;
    }
    StockItem other = (StockItem) o;
    return name.equals(other.name) && size.equals(other.size);
}
```

```
    return name.hashCode();
    return name.hashCode() * 17 + size.hashCode();
    return name.hashCode() * 17 + quantity;
    return quantity;
```

```
    return name.hashCode(); √ legal
    return name.hashCode() * 17 + size.hashCode();
    return name.hashCode() * 17 + quantity;
    return quantity;
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    return name.hashCode(); ✓ legal
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    return name.hashCode() * 17 + quantity;
    return quantity;
```

```
    return name.hashCode(); √ legal
    return name.hashCode() * 17 + size.hashCode(); √ legal
    return name.hashCode() * 17 + quantity; ✗ illegal!
    return quantity;
```

```
    return name.hashCode(); √ legal
    return name.hashCode() * 17 + size.hashCode(); √ legal
    return name.hashCode() * 17 + quantity; ✗ illegal!
    return quantity; ✗ illegal!
```

```
    return name.hashCode(); ✓ legal
    return name.hashCode() * 17 + size.hashCode(); ✓ legal
    return name.hashCode() * 17 + quantity; ✗ illegal!
    return quantity; ✗ illegal!
    The equals method does not care about quantity
```

Which implementation do you prefer?

```
public int hashCode() {
    return name.hashCode();
}

public int hashCode() {
    return name.hashCode()*17 + size.hashCode();
}
```

Which implementation do you prefer?

```
public int hashCode() {
    return name.hashCode();
}

hashCode for StockItems that have different sizes as long as they have the same name, so it doesn't differentiate between different StockItems as well as (ii).

public int hashCode() {
    return name.hashCode()*17 + size.hashCode();
}
```

Suppose we are specifying a method and we have a choice between either requiring a precondition (e.g., @requires: n > 0) or specifying that the method throws an exception under some circumstances (e.g., @throws IllegalArgumentException if n <= 0).

Assuming that neither version will be significantly more expensive to implement than the other and that we do not expect the precondition to be violated or the exception to be thrown in normal use, is there any reason to prefer one of these to the other, and, if so, which one?

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Note: You could just as easily argue the other way. It may be better to specify the precondition because once the exception is in the specification, it has to stay there because the client may expect it.

Suppose we are trying to choose between two possible specifications for a method. One of the specifications S is stronger than the other specification W, but both include the behavior needed by clients. In practice, should we always pick the stronger specification S, always pick the weaker one W, or is it possible that either one might be the suitable choice? Give a brief justification of your answer, including a brief list of the main criteria to be used in making the decision.

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Neither is necessarily better. What is important is picking a specification that is simple, promotes modularity and reuse, and can be implemented efficiently.

(Many answers focused narrowly on which would be easier to implement. While that is important – we don't want a specification that is impossible to build – it isn't the main thing that determines whether a system design is good or bad.)