# CSE 331 Software Design & Implementation

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Fall 2016
Abstraction Functions

# Connecting implementations to specs

#### **Representation Invariant**: maps Object → boolean

- Indicates if an instance is well-formed
- Defines the set of valid concrete values
- Only values in the valid set make sense as implementations of an abstract value
- For implementors/debuggers/maintainers of the abstraction:
   no object should ever violate the rep invariant
  - Such an object has no useful meaning

#### **Abstraction Function**: maps Object → abstract value

- What the data structure means as an abstract value
- How the data structure is to be interpreted
- Only defined on objects meeting the rep invariant
- For implementors/debuggers/maintainers of the abstraction:
   Each procedure should meet its spec (abstract values) by "doing the right thing" with the concrete representation

## Rep inv. constrains structure, not meaning

```
An implementation of insert that preserves the rep invariant:

public void insert(Character c) {

   Character cc = new Character(encrypt(c));

   if (!elts.contains(cc))

      elts.addElement(cc);
}

public boolean member(Character(encrypt(c));

if (!elts.contains(c));

charSet s = new CharSet();

s.insert('a');

if (s.member('a'))

...
```

#### Program is still wrong

- Clients observe incorrect behavior
- What client code exposes the error?
- Where is the error?
- We must consider the meaning
- The abstraction function helps us

## Abstraction function: rep→abstract value

The abstraction function maps the concrete representation to the abstract value it represents

```
AF: Object → abstract value

AF(CharSet this) = { c | c is contained in this.elts }

"set of Characters contained in this.elts"
```

Not executable because abstract values are "just" conceptual

The abstraction function lets us reason about what [concrete] methods do in terms of the clients' [abstract] view

### Abstraction function and insert

Goal is to satisfy the specification of insert:

```
// modifies: this
// effects: this<sub>post</sub> = this<sub>pre</sub> U {c}
public void insert (Character c) {...}
```

The AF tells us what the rep means, which lets us place the blame

```
AF(CharSet this) = { c | c is contained in this.elts }
```

Consider a call to insert:

```
On entry, meaning is AF(this_{pre}) = elts_{pre}
On exit, meaning is AF(this_{post}) = AF(this_{pre}) U \{encrypt('a')\}
```

What if we used this abstraction function instead?

```
AF(this) = { c | encrypt(c) is contained in this.elts }
= { decrypt(c) | c is contained in this.elts }
```

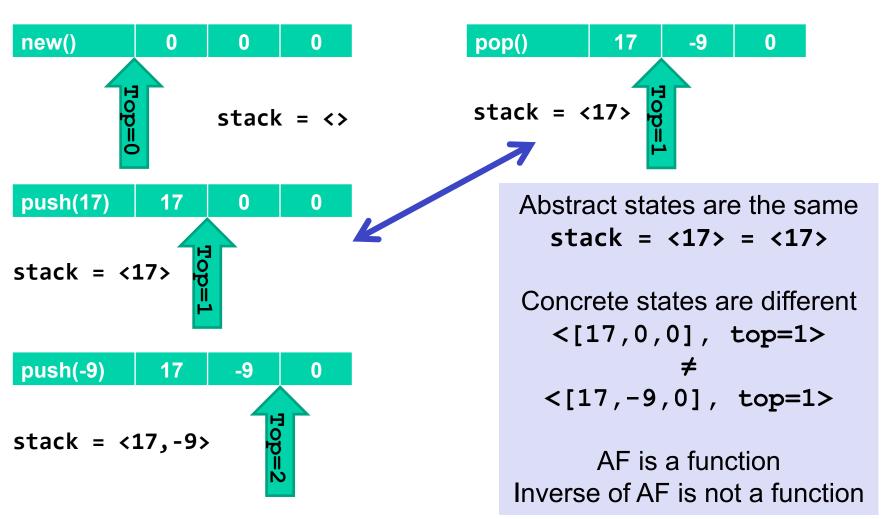
## The abstraction function is a function

Why do we map concrete to abstract and not vice versa?

- It's not a function in the other direction
  - Example: lists [a,b] and [b,a] might each represent the set {a,b}
- It's not as useful in the other direction
  - Purpose is to reason about whether our methods are manipulating concrete representations correctly in terms of the abstract specifications

## Stack AF example

Abstract stack with array and "top" index implementation



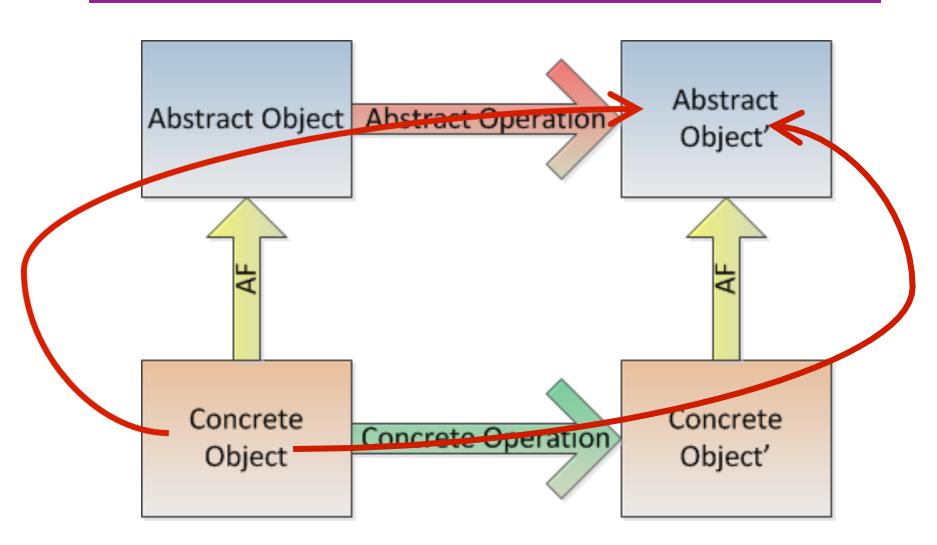
## Benevolent side effects

Different implementation of member:

```
boolean member(Character c1) {
  int i = elts.indexOf(c1);
  if (i == -1)
    return false;
  // move-to-front optimization
  Character c2 = elts.elementAt(0);
  elts.set(0, c1);
  elts.set(i, c2);
  return true;
}
```

- Move-to-front speeds up repeated membership tests
- Mutates rep, but does not change abstract value
  - AF maps both reps to the same abstract value
    - Precise reasoning/explanation for "clients can't tell"

# For any correct operation...



# Writing an abstraction function

Domain: all representations that satisfy the rep invariant

Range: can be tricky to denote

For mathematical entities like sets: easy

For more complex abstractions: give names to specification

- AF defines the value of each "specification field"
  - (Course notes have examples of complex AFs with many spec. fields, but it's possible to be too complex – go for simple, correct, understandable whenever possible)

Overview section of the specification should provide a notation of writing abstract values

- Could implement a method for printing in this notation
  - Useful for debugging
  - Often a good choice for toString

# Data Abstraction: Summary

#### Rep invariant

Which concrete values represent abstract values

#### Abstraction function

For each concrete value, which abstract value it represents

Together, they modularize the implementation

- Neither one is part of the ADT's specification
- Both are needed to reason an implementation satisfies the specification

In practice, representation invariants are documented more often and more carefully than abstraction functions

A more widely understood and appreciated concept