

CSE 331

Software Design & Implementation

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Abstraction Functions

(Based on slides by Mike Ernst, Dan Grossman, David Notkin, Hal Perkins)

Connecting implementations to specs

Representation Invariant: maps Object \rightarrow boolean

- Indicates if an instance is *well-formed*
- Defines the set of valid concrete values
- Only values in the valid set make sense as implementations of an abstract value
- **For implementors/debuggers/maintainers of the abstraction: no object should ever violate the rep invariant**
 - Such an object has no useful meaning

Abstraction Function: maps Object \rightarrow abstract value

- What the data structure *means* as an abstract value
- How the data structure is to be interpreted
- Only defined on objects meeting the rep invariant
- **For implementors/debuggers/maintainers of the abstraction:** Each procedure should meet its spec (abstract values) by “doing the right thing” with the concrete representation

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Rep inv. constrains structure, not meaning

An implementation of `insert` that preserves the rep invariant:

```
public void insert(Character c) {
    Character cc = new Character(encrypt(c));
    if (!elts.contains(cc))
        elts.addElement(cc);
}
public boolean member(Character c) {
    return elts.contains(c);
}
```

```
CharSet s = new CharSet();
s.insert('a');
if (s.member('a'))
    ...
```

Program is still wrong

- Clients observe incorrect behavior
- What client code exposes the error?
- Where is the error?
- We must consider the *meaning*
- The *abstraction function* helps us

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Abstraction function: rep \rightarrow abstract value

The *abstraction function* maps the concrete representation to the abstract value it represents

AF: Object \rightarrow abstract value

AF(CharSet this) = { c | c is contained in this.elts }
“set of Characters contained in this.elts”

Not executable because abstract values are “just” conceptual

The abstraction function lets us reason about what [concrete] methods do in terms of the clients' [abstract] view

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Abstraction function and `insert`

Goal is to satisfy the specification of `insert`:

```
// modifies: this
// effects: thispost = thispre U {c}
public void insert (Character c) {...}
```

The AF tells us what the rep means, which lets us place the blame

AF(CharSet this) = { c | c is contained in this.elts }

Consider a call to `insert`:

On *entry*, meaning is AF(this_{pre}) = elts_{pre}

On *exit*, meaning is AF(this_{post}) = AF(this_{pre}) U {encrypt('a')}

What if we used this abstraction function instead?

```
AF(this) = { c | encrypt(c) is contained in this.elts }
         = { decrypt(c) | c is contained in this.elts }
```

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The abstraction function is a function

Why do we map concrete to abstract and not vice versa?

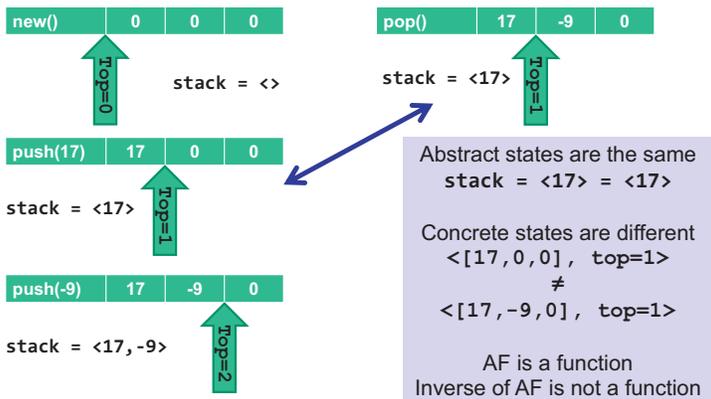
- It's not a function in the other direction
 - Example: lists [a, b] and [b, a] might each represent the set {a, b}
- It's not as useful in the other direction
 - Purpose is to reason about whether our methods are manipulating concrete representations correctly in terms of the abstract specifications

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Stack AF example

Abstract stack with array and "top" index implementation



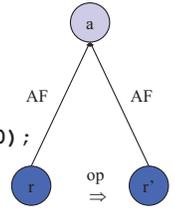
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Benevolent side effects

Different implementation of `member`:

```
boolean member(Character c1) {
    int i = elts.indexOf(c1);
    if (i == -1)
        return false;
    // move-to-front optimization
    Character c2 = elts.elementAt(0);
    elts.set(0, c1);
    elts.set(i, c2);
    return true;
}
```

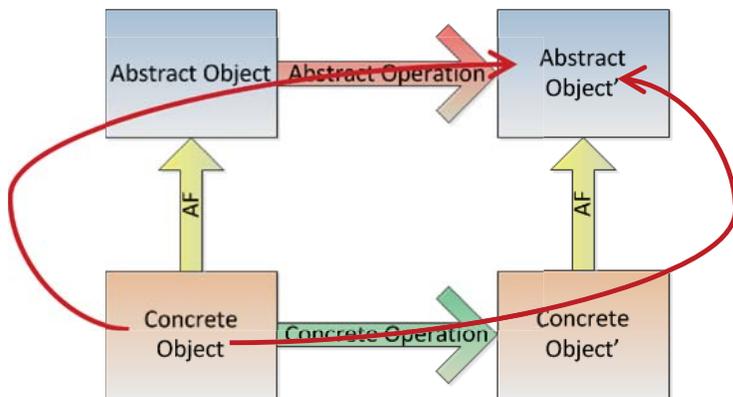


- Move-to-front speeds up repeated membership tests
- Mutates `rep`, but does not change *abstract* value
 - AF maps both *reps* to the same abstract value
 - Precise reasoning/explanation for “clients can’t tell”

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For any correct operation...



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Writing an abstraction function

Domain: all representations that satisfy the rep invariant

Range: can be tricky to denote

For mathematical entities like sets: easy

For more complex abstractions: give names to specification

- AF defines the value of each “specification field”

Overview section of the specification should provide a notation of writing abstract values

- Could implement a method for printing in this notation
 - Useful for debugging
 - Often a good choice for `toString`

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Data Abstraction: Summary

Rep invariant

- Which concrete values represent abstract values

Abstraction function

- For each concrete value, which abstract value it represents

Together, they modularize the implementation

- Neither one is part of the ADT’s specification
- Both are needed to reason an implementation satisfies the specification

In practice, representation invariants are documented more often and more carefully than abstraction functions

- A more widely understood and appreciated concept

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