

NOTE: Hmwrk 4 is published in the gradebook. Yay!!!!!



I REALLY NEED TO STOP USING DEPTH-FIRST SEARCHES.

Section 7: Dijkstra's

SLIDES ADAPTED FROM ALEX MARIAKAKIS

WITH MATERIAL KELLEN DONOHUE, DAVID MAILHOT, AND DAN GROSSMAN

Things to Discuss

Late days

- 4 assignments left, including Hmwrk 6
- Late Days are marked in Catalyst Updated through Hmwrk 4

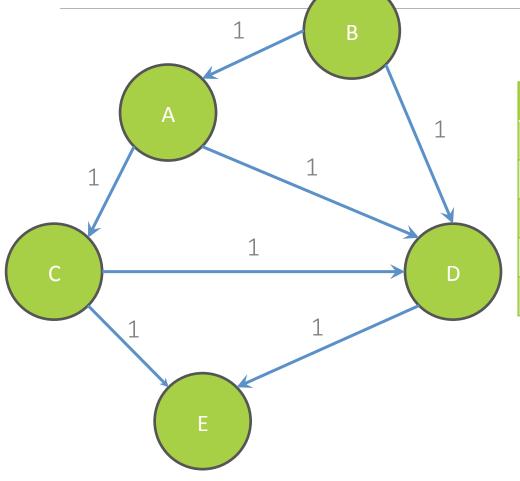
Hmwrk 4 is grades are published. Woot!

Hmwrk 5 is getting returned soon-ish. Finishing up grading now. Returning in time for you to check it again Hmwrk 6.

Hints from a Hmwrk-Grader:

- Answers.txt Hint:
 - "Name: <replace this with your name>"
- JavaDoc Comments Should contain a general overview of the method
- Minimize the asserts per test

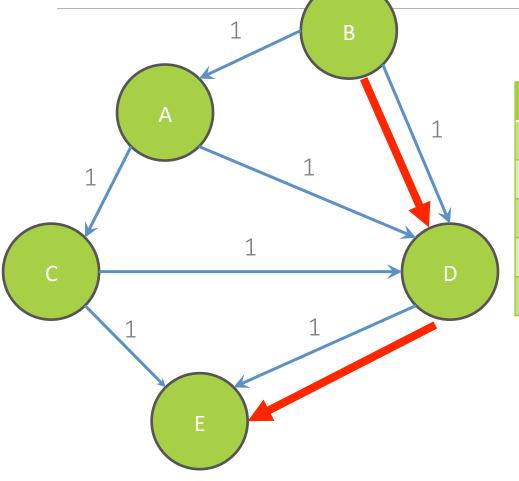
Review: Shortest Paths with BFS



From Node B

Destination	Path	Cost
А	<b,a></b,a>	1
В		0
С	<b,a,c></b,a,c>	2
D	<b,d></b,d>	1
Е	<b,d,e></b,d,e>	2

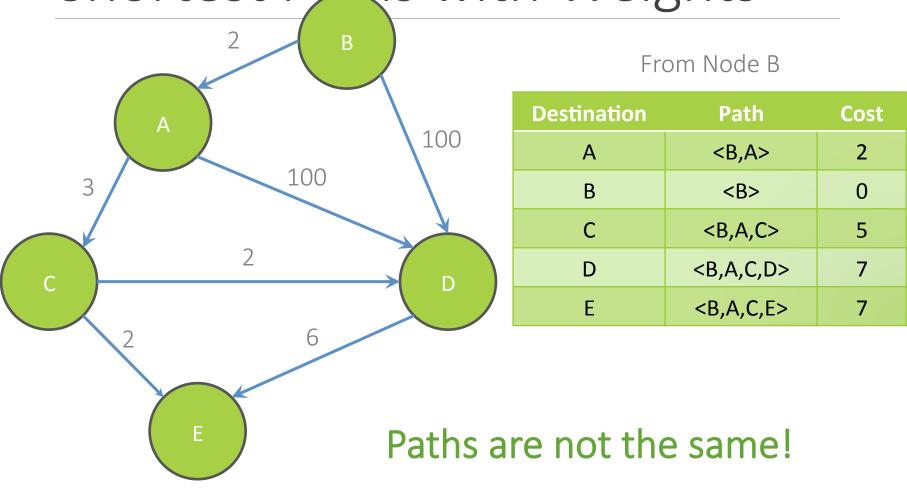
Review: Shortest Paths with BFS



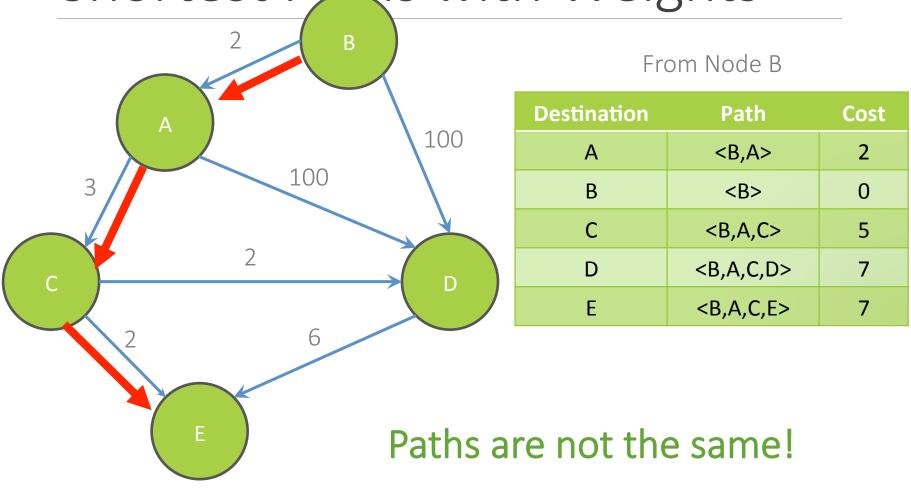
From Node B

Destination	Path	Cost
А	<b,a></b,a>	1
В		0
С	<b,a,c></b,a,c>	2
D	<b,d></b,d>	1
Е	<b,d,e></b,d,e>	2

Shortest Paths with Weights

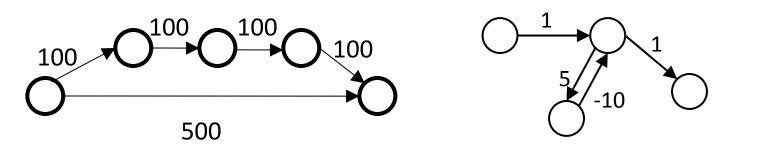


Shortest Paths with Weights



Goal: Smallest cost? Or fewest edges?

BFS vs. Dijkstra's



BFS doesn't work because path with minimal cost ≠ path with fewest edges Also, Dijkstra's works if the weights are non-negative

What happens if there is a negative edge?

Minimize cost by repeating the cycle forever

Dijkstra's Algorithm

Named after its inventor Edsger Dijkstra (1930-2002)

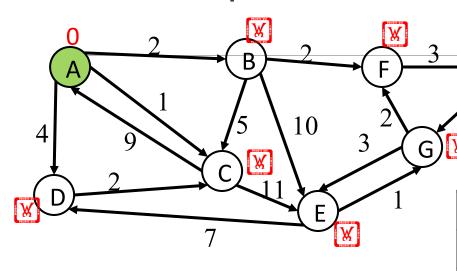
- Truly one of the "founders" of computer science;
- This is just one of his many contributions

The idea: reminiscent of BFS, but adapted to handle weights

- Grow the set of nodes whose shortest distance has been computed
- Nodes not in the set will have a "best distance so far"
- A PRIORITY QUEUE will turn out to be useful for efficiency We'll cover this later in the slide deck

Dijkstra's Algorithm

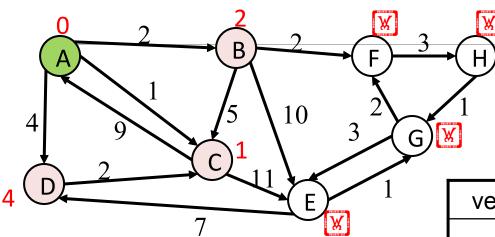
- 1. For each node v, set v.cost = ∞ and v.known = false
- 2. **Set** source.cost = 0
- 3. While there are unknown nodes in the graph
 - a) Select the unknown node v with lowest cost
 - b) Mark v as known
 - c) For each edge (v, u) with weight w,



Goal: Fully explore the graph

Order Added to Known Set:

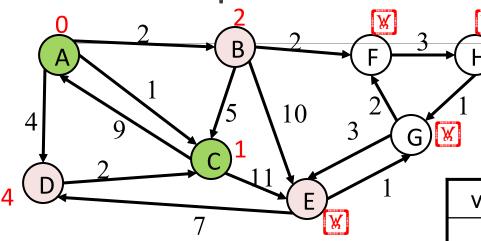
vertex	known?	cost	path
Α	Υ	0	
В		8	
С		8	
D		8	
Е		8	
F		8	
G		8	
Н		8	



Order Added to Known Set:

Α

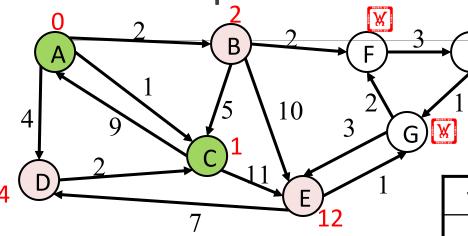
vertex	known?	cost	path
Α	Υ	0	
В		≤ 2	Α
С		≤ 1	Α
D		≤ 4	Α
Е		8	
F		8	
G		8	
Н		8	



Order Added to Known Set:

A, C

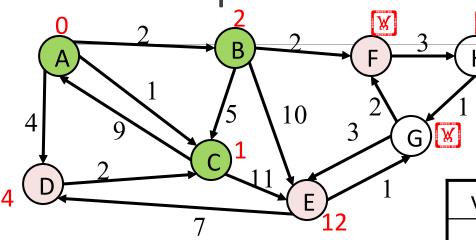
vertex	known?	cost	path
А	Υ	0	
В		≤ 2	Α
С	Υ	1	Α
D		≤ 4	Α
Е		8	
F		∞	
G		∞	
Н		∞	



Order Added to Known Set:

A, C

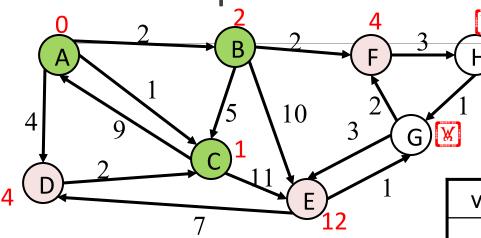
vertex	known?	cost	path
Α	Υ	0	
В		≤ 2	Α
С	Υ	1	Α
D		≤ 4	Α
Е		≤ 12	С
F		8	
G		8	
Н		8	



Order Added to Known Set:

A, C, B

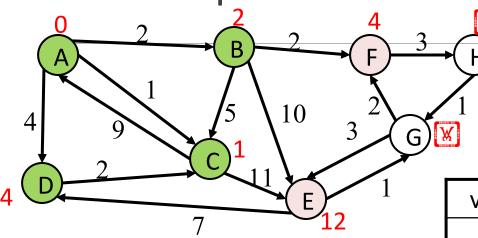
vertex	known?	cost	path
Α	Υ	0	
В	Υ	2	Α
С	Υ	1	Α
D		≤ 4	Α
Е		≤ 12	С
F		8	
G		8	
Н		8	



Order Added to Known Set:

A, C, B

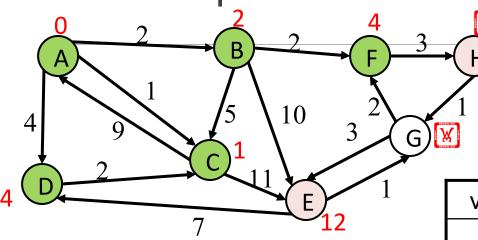
vertex	known?	cost	path
Α	Υ	0	
В	Υ	2	А
С	Υ	1	Α
D		≤ 4	Α
Е		≤ 12	С
F		≤ 4	В
G		8	
Н		8	



Order Added to Known Set:

A, C, B, D

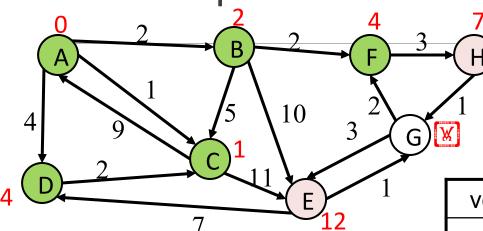
vertex	known?	cost	path
Α	Υ	0	
В	Υ	2	Α
С	Υ	1	Α
D	Υ	4	Α
Е		≤ 12	С
F		≤ 4	В
G		8	
Н		8	



Order Added to Known Set:

A, C, B, D, F

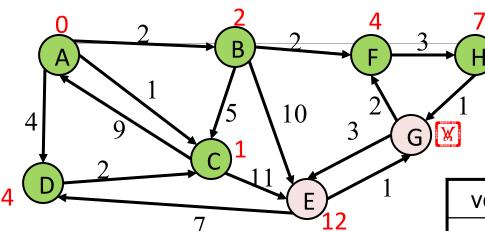
vertex	known?	cost	path
Α	Y	0	
В	Y	2	Α
С	Υ	1	Α
D	Υ	4	Α
Е		≤ 12	С
F	Y	4	В
G		8	
Н		8	



Order Added to Known Set:

A, C, B, D, F

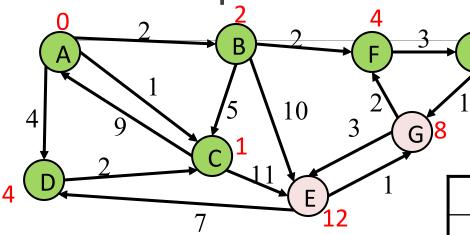
vertex	known?	cost	path
Α	Y	0	
В	Y	2	Α
С	Υ	1	Α
D	Υ	4	Α
Е		≤ 12	С
F	Y	4	В
G		8	
Н		≤ 7	F



Order Added to Known Set:

A, C, B, D, F, H

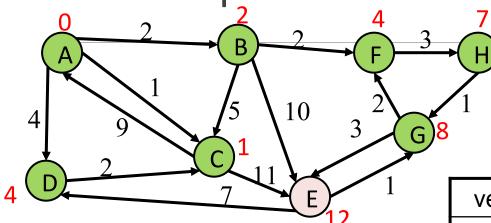
vertex	known?	cost	path
Α	Υ	0	
В	Υ	2	Α
С	Υ	1	Α
D	Υ	4	Α
Е		≤ 12	С
F	Υ	4	В
G		8	
Н	Y	7	F



Order Added to Known Set:

A, C, B, D, F, H

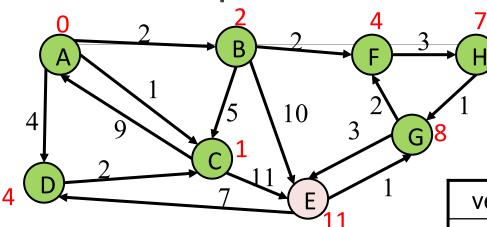
vertex	known?	cost	path
Α	Y	0	
В	Υ	2	Α
С	Y	1	Α
D	Υ	4	Α
Е		≤ 12	С
F	Y	4	В
G		≤ 8	Н
Н	Υ	7	F



Order Added to Known Set:

A, C, B, D, F, H, G

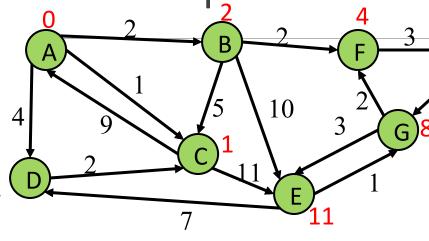
vertex	known?	cost	path
Α	Υ	0	
В	Υ	2	Α
С	Υ	1	Α
D	Y	4	Α
Е		≤ 12	С
F	Y	4	В
G	Y	8	Н
Н	Υ	7	F



Order Added to Known Set:

A, C, B, D, F, H, G

vertex	known?	cost	path
Α	Υ	0	
В	Υ	2	Α
С	Υ	1	Α
D	Υ	4	Α
Е		≤ 11	G
F	Υ	4	В
G	Y	8	Η
Н	Υ	7	F

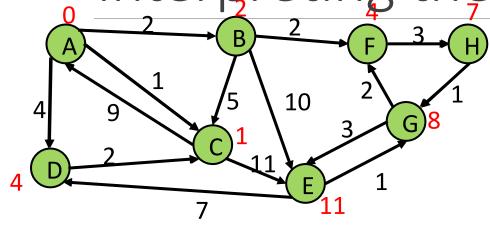


Order Added to Known Set:

A, C, B, D, F, H, G, E

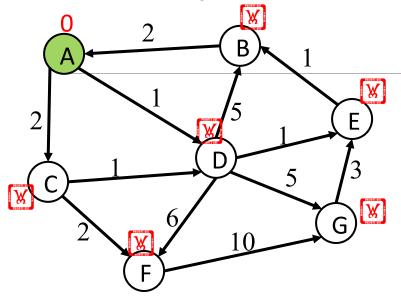
vertex	known?	cost	path
Α	Υ	0	
В	Υ	2	Α
С	Υ	1	Α
D	Υ	4	Α
Е	Y	11	G
F	Y	4	В
G	Y	8	Н
Н	Υ	7	F

Interpreting the Results



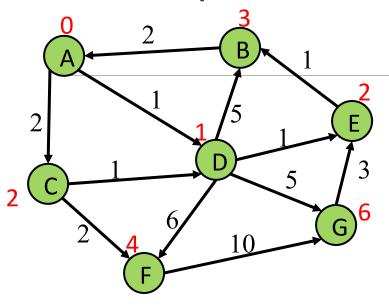
A	B B	2 F	3 H
4		3	G 1
D		E	

vertex	known?	cost	path
Α	Υ	0	
В	Υ	2	Α
С	Υ	1	Α
D	Υ	4	Α
E	Υ	11	G
F	Υ	4	В
G	Υ	8	Н
Н	Υ	7	F



Order Added to Known Set:

vertex	known?	cost	path
Α	Y	0	
В		8	
С		8	
D		8	
Е		8	
F		8	
G		8	



Order Added to Known Set:

A, D, C, E, B, F, G

vertex	known?	cost	path
А	Y	0	
В	Y	3	Е
С	Y	2	Α
D	Y	1	Α
Е	Y	2	D
F	Y	4	С
G	Y	6	D

Pseudocode Attempt #1

```
dijkstra(Graph G, Node start) {
  for each node: x.cost=infinity, x.known=false
  start.cost = 0
  while(not all nodes are known) {
    b = dequeue
    b.known = true
    for each edge (b,a) in G {
      if(!a.known) {
        if(b.cost + weight((b,a)) < a.cost){</pre>
          a.cost = b.cost + weight((b,a))
          a.path = b
```

Can We Do Better?

Increase efficiency by considering lowest cost unknown vertex with sorting instead of looking at all vertices

PriorityQueue is like a queue, but returns elements by lowest value instead of FIFO

Priority Queue

Increase efficiency by considering lowest cost unknown vertex with sorting instead of looking at all vertices

PriorityQueue is like a queue, but returns elements by lowest value instead of FIFO

Two ways to implement:

1. Comparable

- a) class Node implements Comparable<Node>
- b) public int compareTo(other)

2. Comparator

- a) class NodeComparator extends Comparator<Node>
- b) new PriorityQueue(new NodeComparator())

Pseudocode Attempt #2

```
dijkstra(Graph G, Node start) {
  for each node: x.cost=infinity, x.known=false
  start.cost = 0
  build-heap with all nodes
  while(heap is not empty) {
    b = deleteMin()
    if (b.known) continue;
    b.known = true
    for each edge (b,a) in G {
     if(!a.known) {
       add(b.cost + weight((b,a)) )
```

Homework 7

Modify your graph to use generics

Will have to update HW #5 and HW #6 tests

Implement Dijkstra's algorithm

- Search algorithm that accounts for edge weights
- Note: This should not change your implementation of Graph. Dijkstra's is performed on a Graph, not within a Graph.

Homework 7

The more well-connected two characters are, the lower the weight and the more likely that a path is taken through them

- The weight of an edge is equal to the inverse of how many comic books the two characters share
- Ex: If Amazing Amoeba and Zany Zebra appeared in 5 comic books together, the weight of their edge would be 1/5

Hw7 Important Notes!!!

DO NOT access data from hw6/src/data

- Copy over data files from hw6/src/data into hw7/src/data, and access data in hw7 from there instead
- Remember to do this! Or tests will fail when grading.

DO NOT modify ScriptFileTests.java

Hw7 Test script Command Notes

HW7 *LoadGraph* command is slightly different from HW6

- After graph is loaded, there should be at most one directed edge from one node to another, with the edge label being the multiplicative inverse of the number of books shared
- Example: If 8 books are shared between two nodes, the edge label will be
 1/8
- Since the edge relationship is symmetric, there would be another edge going the other direction with the same edge label

Generics

We will go over these in lecture tomorrow!