

```
if (justMetYou) {  
    crazy = true;  
    cout << number << endl;  
    int x = rand()%100;  
    if (x>=50)  
        callMe();  
}
```

**“Call Me Maybe”**

```
private function bad() {  
    break;  
}
```

**“Breaking Bad”**

```
class StarWars(int episode) {  
    if (episode == 6)  
        return Jedi;  
}
```

**“Star Wars: Episode VI – Return of the Jedi”**

```
try
{
    Assert(Life.Real);
    Assert(Life.Fantasy);
}
catch(LandSlideException ex)
{
    #region Reality
    while(true)
    {
        character.Eyes.ForEach(eye => eye.Open()).Orient(Direction.Sky).See(); );
        self.Wealth = null;
        self.Sex = Sex.Male;

        if(self.ComeDifficulty == Difficulty.Easy && self.GoDifficulty ==
Difficulty.Easy && self.High < 0.1 && self.Low < 0.1)
        {
            self.Sympathies.Clear();

            switch(wind.Direction)
            {
                case Direction.North:
                case Direction.East:
                case Direction.South:
                case Direction.West:
                default:
                    piano.Play();
                    break;
            }
        }
    }
    #endregion
}
```

**“Bohemian Rhapsody”**

# Section 1: Code Reasoning

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**INTRO +  
STORY TIME !!!**

# Reasoning About Code

- Two purposes
  - Prove our code is correct
  - Understand why code is correct
- Forward reasoning: determine what follows from initial conditions
- Backward reasoning: determine sufficient conditions to obtain a certain result

# Forward Reasoning

{ $x \geq 0, y \geq 0$ }

$y = 16;$

{ $x \geq 0, y = 16$ }

$x = x + y$

{ $x \geq 16, y = 16$ }

$x = \sqrt{x}$

{ $x \geq 4, y = 16$ }

$y = y - x$

{ $x \geq 4, y \leq 12$ }

# Forward Reasoning

```
{true}

if (x > 0) {
    {x > 0}
    abs = x
    {x > 0, abs = x}
}
else {
    {x <= 0}
    abs = -x
    {x <= 0, abs = -x}
}
{x > 0, abs = x OR x <= 0, abs = -x}

{abs = |x|}
```

# Backward Reasoning

{ $x + 3b - 4 > 0$ }

$a = x + b;$

{ $a + 2b - 4 > 0$ }

$c = 2b - 4$

{ $a + c > 0$ }

$x = a + c$

{ $x > 0$ }

# Backward Reasoning

```
{y > 15 || (y <= 5 && y + z > 17) }

if (y > 5) {
    {y > 15}
    x = y + 2
    {x > 17}

}
else {
    {y + z > 17}
    x = y + z;
    {x > 17}

}
{x > 17}
```

# Implication

- Hoare triples are just an extension of logical implication
  - Hoare triple:  $\{P\} S \{Q\}$
  - $P \rightarrow Q$  after statement  $S$
- Everything implies true
- False implies everything

P	Q	$P \rightarrow Q$
T	T	T
T	F	F
F	T	T
F	F	T

# Weaker vs. Stronger

- If  $P_1 \rightarrow P_2$ , then
  - $P_1$  is stronger than  $P_2$
  - $P_2$  is weaker than  $P_1$
- Weaker statements are more general
- Stronger statements are more restrictive



# Weaker vs. Stronger

$y \geq 16$

$y = 16$

$x$  is even,  $y = x + 1$

$x$  is even,  $y$  is odd

“Alex is an awesome TA”

“Alex is a TA”

# Weakest Precondition

- The most lenient assumptions such that a postcondition will be satisfied
- If  $P^*$  is the weakest precondition for  $\{P\} S \{Q\}$ , then  $P \rightarrow P^*$  for all  $P$  that make the Hoare triple valid
- Notation:  $WP = wp(S, Q)$

# Weakest Precondition

$\text{wp}(x = y * y, \ x > 4)$

$|y| > 2$

$\text{wp}(y = x + 1 ; z = y - 3, \ z = 10)$

$\text{wp}(y = x + 1, \ \text{wp}(z = y - 3, \ z = 10))$

$\text{wp}(y = x + 1, \ y - 3 = 10)$

$\text{wp}(y = x + 1, \ y = 13)$

$x = 12$