

# CSE 331 Software Design & Implementation

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## Abstraction Functions

(Based on slides by Mike Ernst, David Notkin, Hal Perkins)

## Connecting implementations to specs

**Representation Invariant:** maps Object  $\rightarrow$  boolean

- Indicates if an instance is *well-formed*
- Defines the set of valid concrete values
- Only values in the valid set make sense as implementations of an abstract value
- **For implementors/debuggers/maintainers of the abstraction: no object should ever violate the rep invariant**
  - Such an object has no useful meaning

**Abstraction Function:** maps Object  $\rightarrow$  abstract value

- What the data structure *means* as an abstract value
- How the data structure is to be interpreted
- Only defined on objects meeting the rep invariant
- **For implementors/debuggers/maintainers of the abstraction:** Each procedure should meet its spec (abstract values) by “doing the right thing” with the concrete representation

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## Rep inv. constrains structure, not meaning

An implementation of `insert` that preserves the rep invariant:

```
public void insert(Character c) {
    Character cc = new Character(encrypt(c));
    if (!elts.contains(cc))
        elts.addElement(cc);
}
public boolean member(Character c) {
    return elts.contains(c);
}
```

```
CharSet s = new CharSet();
s.insert('a');
if (s.member('a'))
    ...
```

Program is still wrong

- Clients observe incorrect behavior
- What client code exposes the error?
- Where is the error?
- We must consider the *meaning*
- The *abstraction function* helps us

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## Abstraction function: rep $\rightarrow$ abstract value

The *abstraction function* maps the concrete representation to the abstract value it represents

AF: Object  $\rightarrow$  abstract value

AF(CharSet this) = { c | c is contained in this.elts }

“set of Characters contained in this.elts”

Not executable because abstract values are “just” conceptual

The abstraction function lets us reason about what [concrete] methods do in terms of the clients' [abstract] view

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## Abstraction function and `insert`

Goal is to satisfy the specification of `insert`:

```
// modifies: this
// effects: thispost = thispre U {c}
public void insert (Character c) {...}
```

The AF tells us what the rep means, which lets us place the blame

AF(CharSet this) = { c | c is contained in this.elts }

Consider a call to `insert`:

On *entry*, meaning is  $AF(this_{pre}) \approx elts_{pre}$

On *exit*, meaning is  $AF(this_{post}) = AF(this_{pre}) \cup \{encrypt('a')\}$

What if we used this abstraction function instead?

```
AF(this) = { c | encrypt(c) is contained in this.elts }
         = { decrypt(c) | c is contained in this.elts }
```

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## The abstraction function is a function

Why do we map concrete to abstract and not vice versa?

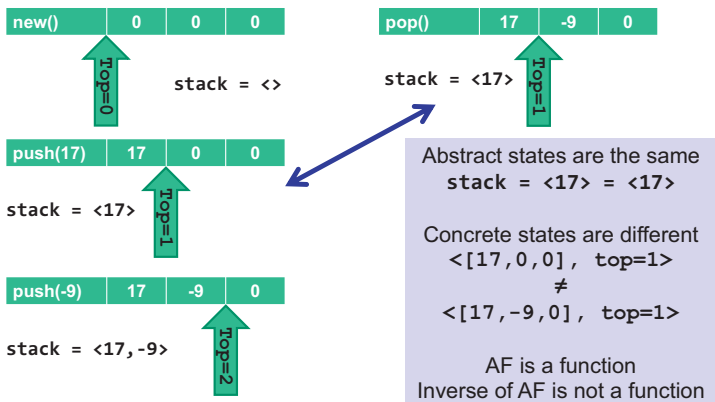
- It's not a function in the other direction
  - Example: lists [a, b] and [b, a] might each represent the set {a, b}
- It's not as useful in the other direction
  - Purpose is to reason about whether our methods are manipulating concrete representations correctly in terms of the abstract specifications

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## Stack AF example

Abstract stack with array and "top" index implementation



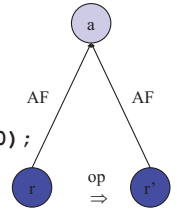
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## Benevolent side effects

Different implementation of `member`:

```
boolean member(Character c1) {
    int i = elts.indexOf(c1);
    if (i == -1)
        return false;
    // move-to-front optimization
    Character c2 = elts.elementAt(0);
    elts.set(0, c1);
    elts.set(i, c2);
    return true;
}
```

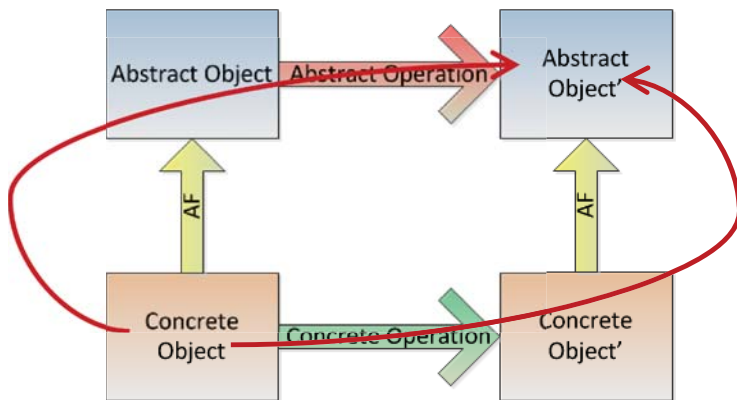


- Move-to-front speeds up repeated membership tests
- Mutates `rep`, but does not change *abstract* value
  - AF maps both *reps* to the same abstract value
    - Precise reasoning/explanation for “clients can’t tell”

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## For any correct operation...



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## Writing an abstraction function

**Domain:** all representations that satisfy the rep invariant

**Range:** can be tricky to denote

- For mathematical entities like sets: easy
- For more complex abstractions: give names to specification
  - AF defines the value of each “specification field”

Overview section of the specification should provide a notation of writing abstract values

- Could implement a method for printing in this notation
  - Useful for debugging
  - Often a good choice for `toString`

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## Data Abstraction: Summary

### Rep invariant

- Which concrete values represent abstract values

### Abstraction function

- For each concrete value, which abstract value it represents

Together, they modularize the implementation

- Neither one is part of the ADT’s specification
- Both are needed to reason an implementation satisfies the specification

In practice, representation invariants are documented more often and more carefully than abstraction functions

- A more widely understood and appreciated concept

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