CSE 326 Data Structures Midterm Review

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Dates

- Midterm Friday!
- Project 2b due next Wednesday
- Homework 4
 - Out soon, due a week from Friday

Logistics

- Closed Notes
- Closed Book except for one 5x8 or smaller notecard with hand-written (only) notes
- Open Mind
- You may bring a calculator, though don't even think about loading it with notes or programs. And you probably won't find it of much use anyway.

Material Covered

- Everything we've talked/read in class up to AVL trees
 - And for AVL trees, up to inserting and rotations, but not implementations in Java

Material Not Covered

- We generally won't make you write syntactically correct Java code (pseudocode okay unless requested otherwise)
- We won't make you do a super hard proof
- We won't test you on the gory details of generics, interfaces, etc. in Java
 - But you should know the basic ideas since we spent lecture time on them and had to deal with them in project 2A

Order Notation: Definition

- **O(f(n))** : <u>a set or class of functions</u>
- $g(n) \in O(f(n))$ iff there exist consts *c* and n_0 such that:

 $g(n) \leq c f(n)$ for all $n \geq n_0$

Example: g(n) = 1000n vs. $f(n) = n^2$ Is $g(n) \in O(f(n))$? Pick: n0 = 1000, c = 1







Implementations of Priority Queue ADT

	insert	deleteMin
Unsorted list (Array)		
Unsorted list (Linked-List)		
Sorted list (Array)		
Sorted list (Linked-List)		
Binary Search Tree (BST)		
Binary Heap		



















Operations on *d*-Heap

- Insert : runtime =
- deleteMin: runtime =

Does this help insert or deleteMin more?



Leftist Heap Properties

- Heap-order property
 - parent's priority value is \leq to childrens' priority values
 - result: minimum element is at the root
- · Leftist property
 - For every node x, $npl(left(x)) \ge npl(right(x))$
 - <u>result</u>: tree is at least as "heavy" on the left as the right
 <u>Are leftist trees...</u>

Are leftist trees complete? balanced?











Skew Heaps Problems with <u>leftist</u> heaps – extra storage for npl – extra complexity/logic to maintain and check npl – right side is "often" heavy and requires a switch Solution: <u>skew</u> heaps – "blindly" adjusting version of leftist heaps – merge *always* switches children when fixing right

- merge *always* switches children when fixing right path
- $-\frac{\text{amortized time}}{n}$ for: merge, insert, deleteMin = O(log $\frac{n}{n}$)
- however, worst case time for all three = O(n)







































Balanced BST

Observation

- BST: the shallower the better!
- For a BST with *n* nodes
 - Average height is O(log *n*)
 - Worst case height is O(n)
- Simple cases such as insert(1, 2, 3, ..., n) lead to the worst case scenario

Solution: Require a Balance Condition that

- 1. ensures depth is O(log *n*) strong enough!
- 2. is easy to maintain not too strong!

The AVL Balance Condition

Left and right subtrees of *every node* have equal *heights* **differing by at most 1**

Define: **balance**(*x*) = height(*x*.left) – height(*x*.right)

AVL property: $-1 \le \text{balance}(x) \le 1$, for every node x

- · Ensures small depth
 - Will prove this by showing that an AVL tree of height *h* must have a lot of (i.e. O(2^h)) nodes
- · Easy to maintain
 - Using single and double rotations





















- 1. Find spot for new key
- 2. Hang new node there with this key
- 3. Search back up the path for imbalance
- 4. If there is an imbalance:

case #1: Perform single rotation and exit

• case #2: Perform double rotation and exit

Both rotations keep the subtree height unchanged. Hence only one (sinlge or double) rotation is sufficient!