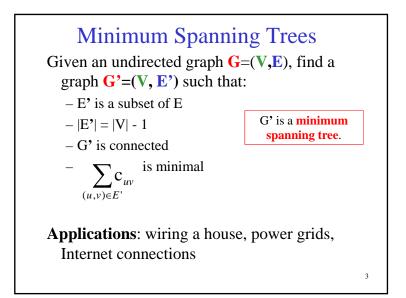


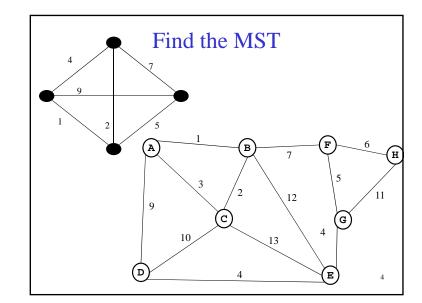
Spring 2007 Lectures 26

Today's Outline

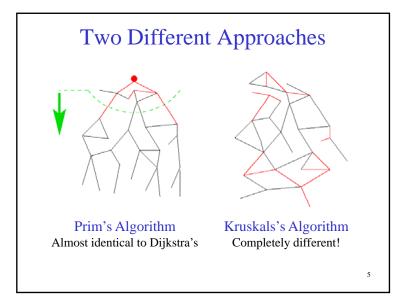
Minimum Spanning Tree 1. Prim's 2. Kruskal's

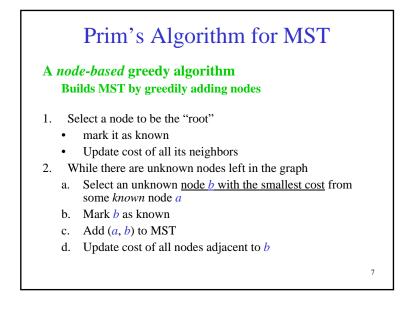
Reading: Weiss, Ch. 9

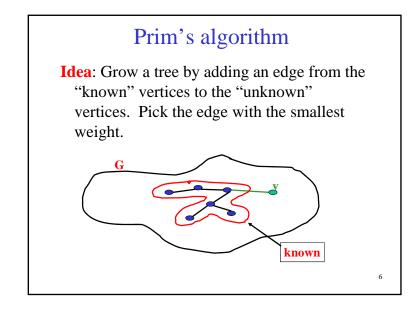


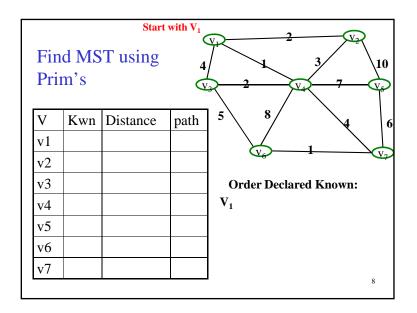


2











Running time:

Same as Dijkstra's: O(|H

 $O(|E| \log |V|)$

Correctness:

Proof is similar to Dijkstra's

Kruskal's Algorithm for MST

An *edge-based* greedy algorithm Builds MST by greedily adding edges

- 1. Initialize with
 - empty MST
 - all vertices marked unconnected
 - all edges unmarked
- 2. While there are still unmarked edges
 - a. Pick the <u>lowest cost edge</u> (u, v) and mark it
 - b. If **u** and **v** are not already connected, add (**u**, **v**) to the MST and mark **u** and **v** as connected to each other

Doesn't it sound familiar?

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Kruskal's MST Algorithm

Idea: Grow a forest out of edges that do not create a cycle. Pick an edge with the smallest weight.

G=(V,E)

