

Outline • Math/Big-O – short summary & review • Priority Queues (Binary Min Heaps) - Reading: Weiss, Ch. 6 1/14/2008 2

Simplifying Recurrences

Given a recursive equation for the running time, can sometimes simplify it for analysis.

• For an upper-bound analysis, can optionally simplify to something larger, e.g.

```
T(n) = T(floor(n/2)) + 1 to T(n) \le T(n/2) + 1
```

For a lower-bound analysis, can optionally simplify to ٠ something smaller, e.g.

T(n) = 2T(n/2 + 5) + 1 to $T(n) \ge 2T(n/2) + 1$

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Priority Queue ADT **1. PQueue data** : collection of data with priority 2. PQueue operations insert _ - deleteMin (also: create, destroy, is empty) 3. PQueue property: for two elements in the queue, x and y, if x has a <u>lower</u> priority value than y, x will be deleted before y 1/14/2008 6

Implementations of	Priority Q	ueue AD
	insert	deleteMin
Unsorted list (Array)		
Unsorted list (Linked-List)		
Sorted list (Array)		
Sorted list (Linked-List)		
Binary Search Tree (BST)		

Applications of the Priority Q

- Select print jobs in order of decreasing length
- Forward packets on network routers in order of urgency
- Select most frequent symbols for compression
- Sort numbers, picking minimum first
- Anything greedy

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- A binary tree in which each node has *exactly zero or two children*.
- (also known as a proper binary tree)

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• (we will use this later for Huffman trees)

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Facts about Heaps

Observations:

- finding a child/parent index is a multiply/divide by two
- operations jump widely through the heap
- each percolate step looks at only two new nodes
- inserts are at least as common as deleteMins

Realities:

• division/multiplication by powers of two are equally fast

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- looking at only two new pieces of data: bad for cache!
- with huge data sets, disk accesses dominate 1/14/2008







