Splay Trees

CSE 326
Data Structures
Lecture 8

Readings and References

- Reading
 - > Sections 4.5-4.7

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Self adjustment for better living

- Ordinary binary search trees have no balance conditions
 - > what you get from insertion order is it
- Balanced trees like AVL trees enforce a balance condition when nodes change
 - > tree is always balanced after an insert or delete
- Self-adjusting trees get reorganized over time as nodes are accessed

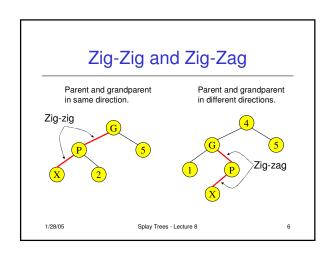
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Splay Trees

- · Splay trees are tree structures that:
 - › Are not perfectly balanced all the time
 - > Data most recently accessed is near the root.
- The procedure:
 - After node X is accessed, perform "splaying" operations to bring X to the root of the tree.
 - Do this in a way that leaves the tree more balanced as a whole

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Splay Tree Terminology • Let X be a non-root node with ≥ 2 ancestors. • P is its parent node. • G is its grandparent node. G G P P P P Splay Trees - Lecture 8 5



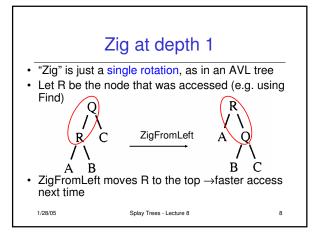
Splay Tree Operations

1. Helpful if nodes contain a parent pointer.



- 2. When X is accessed, apply one of six rotation routines.
- Single Rotations (X has a P (the root) but no G)
 ZigFromLeft, ZigFromRight
- Double Rotations (X has both a P and a G)
 ZigZigFromLeft, ZigZigFromRight
 ZigZagFromLeft, ZigZagFromRight

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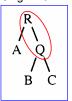




· Suppose Q is now accessed using Find



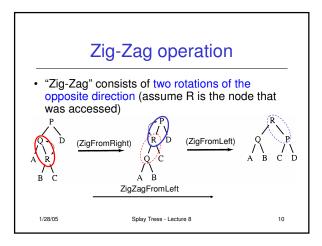
ZigFromRight



· ZigFromRight moves Q back to the top

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Zig-Zig operation

 "Zig-Zig" consists of two single rotations of the same direction (R is the node that was accessed)

was accessed)



R P A B C D





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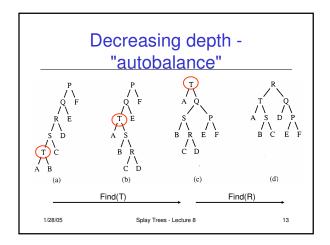
ZigZigFromLeft

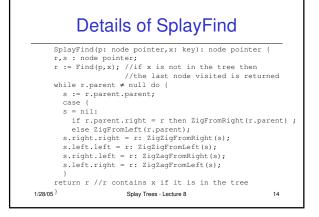
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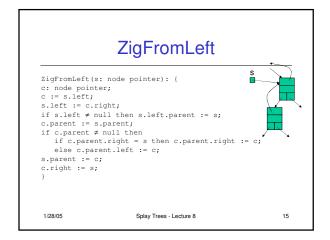
Find Operation

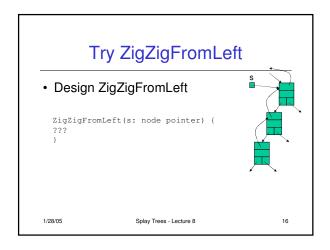
- · Find operation
 - > Do a normal find in the binary search tree
 - Splay the the node found to the root by a series of zig-zig and zig-zag operations with an additional zig at the end if the length of the path to the node is odd.
 - If nothing found splay the last node visited to the root.

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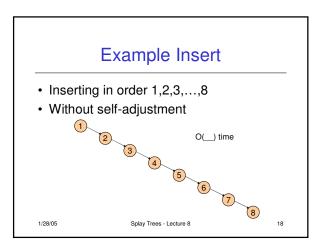




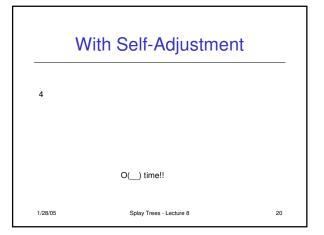




• Insert x • Insert x as normal then splay x to root.



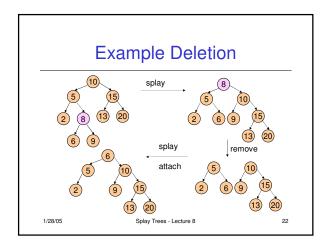
With Self-Adjustment 1 2 3 1/28/05 Splay Trees - Lecture 8 19

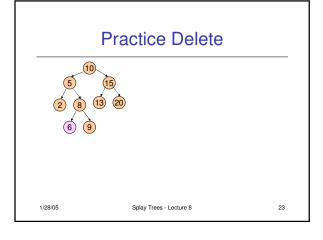


Splay Tree Deletion

- Delete
 - Splay x to root and remove it. Two trees remain, right subtree and left subtree.
 - > Splay the max in the left subtree to the root
 - Attach its right subtree to the new root of the left subtree and return it. The predecessor of x becomes the root.

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Analysis of Splay Trees Splay trees tend to be balanced M operations takes time O(M log N) for M ≥ N operations on N items. Amortized O(log n) time. Splay trees have good "locality" properties Recently accessed items are near the root of the tree. Items near an accessed node are pulled toward the root.

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