

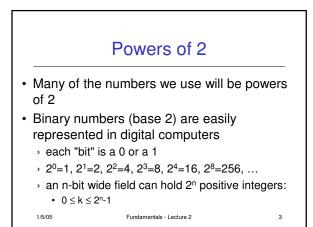
Mathematical Background

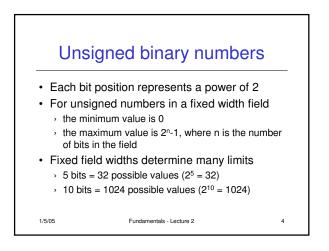
- Today, we will review:
 - Logs and exponents and series
 - Asymptotics and order of magnitude notation

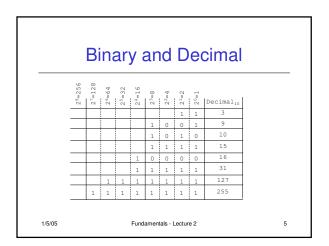
Fundamentals - Lecture 2

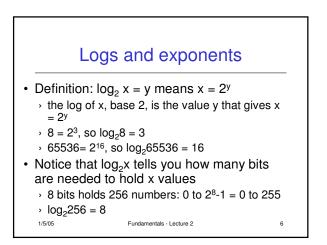
2

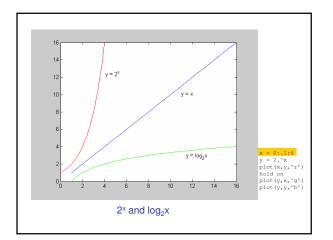
Solving recursive equations

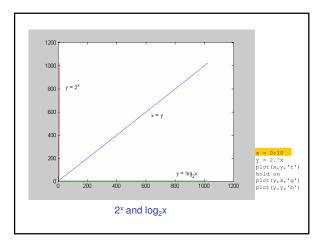


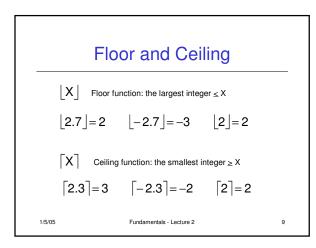


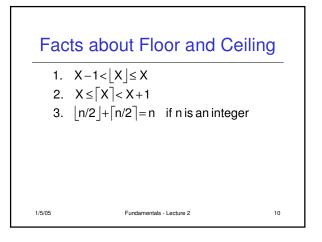


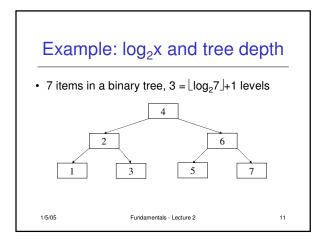


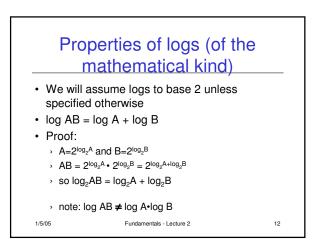


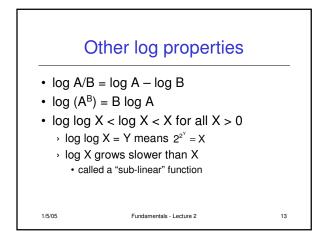


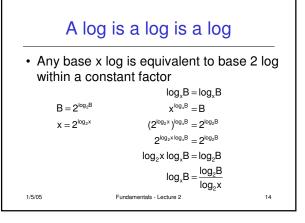


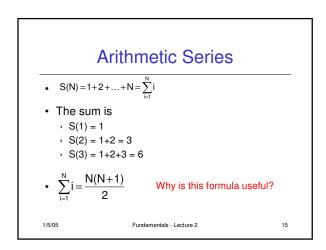


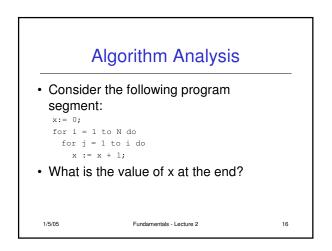


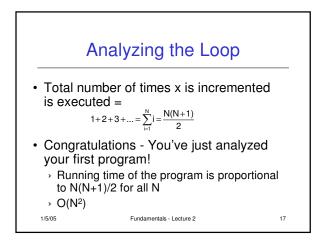


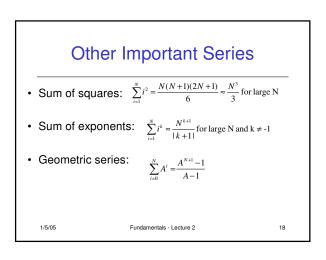


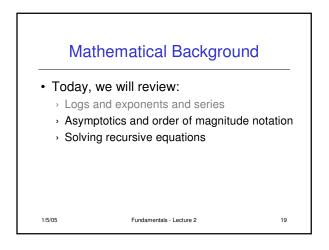


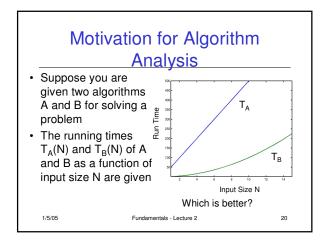


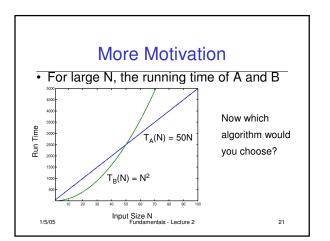


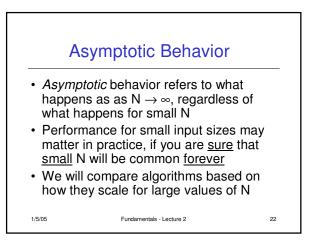


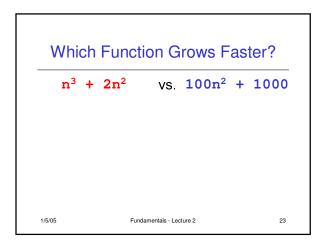


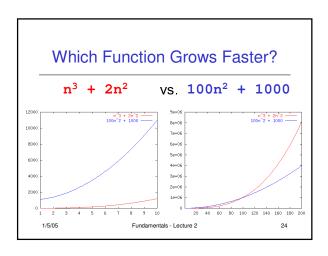


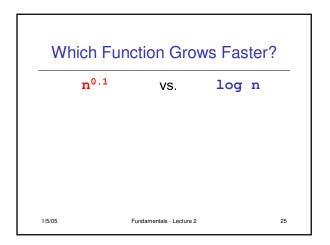


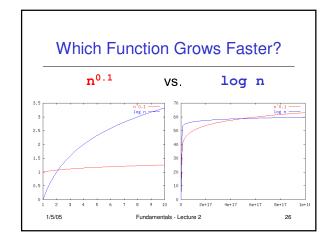


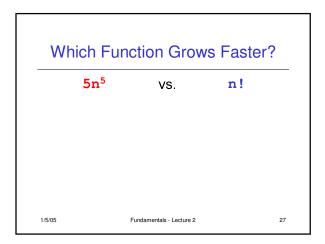


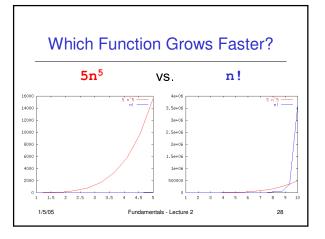


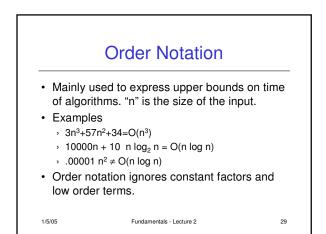


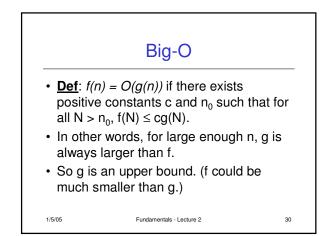




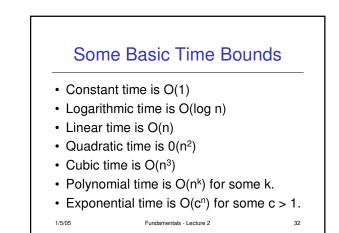


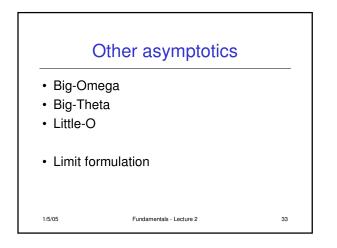


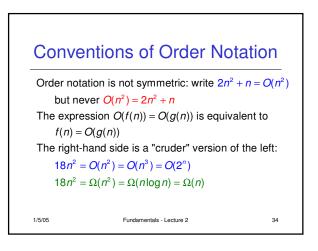


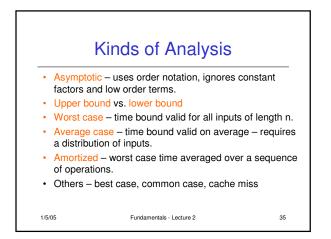


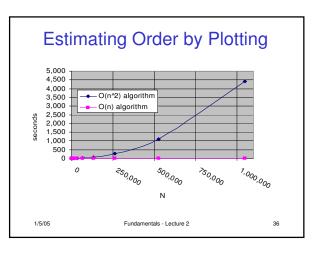
$16n^3\log_8(10n)$	$n^2)+100n^2=O(n^3\log n)$	g(<i>n</i>))
 Eliminate low order terms Eliminate constant coefficients 	$\frac{16n^{3} \log_{8}(10n^{2}) + 100n^{2}}{\Rightarrow 16n^{3} \log_{8}(10n^{2})}{\Rightarrow n^{3} \log_{8}(10n^{2})}{\Rightarrow n^{3} \left[\log_{8}(10) + \log_{8}(n^{2}) \right]}{\Rightarrow n^{3} \log_{8}(10) + n^{3} \log_{8}(n^{2})}{\Rightarrow n^{3} \log_{8}(10) + n^{3} \log_{8}(n^{2})}{\Rightarrow n^{3} 2\log_{8}(n)}{\Rightarrow n^{3} \log_{8}(n)}$	
1/5/05	$\Rightarrow n^3 \log_8(2) \log(n)$ $\Rightarrow n^3 \log(n)$ Fundamentals - Lecture 2	31

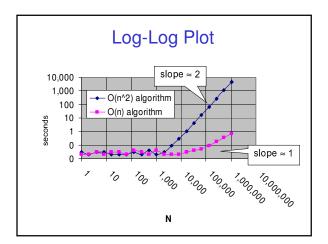


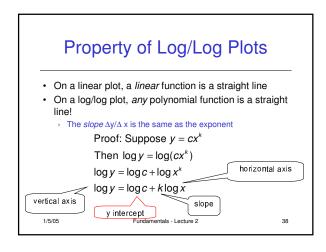


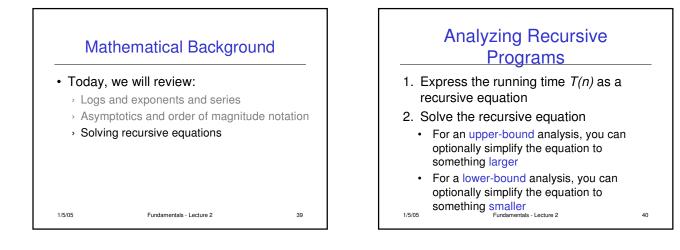


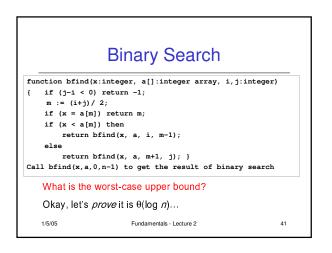


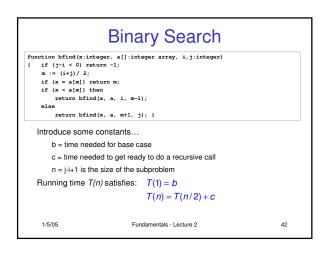




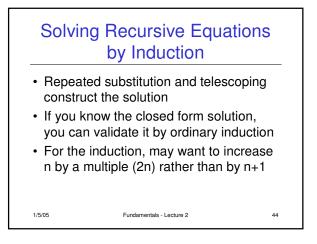








Solving Recursi (by Repeated S	
T(n) = T(n/2) + c	substitute for T(n/2)
T(n) = T(n/4) + c + c	
T(n) = T(n/4) + c + c	substitute for T(n/4)
T(n) = T(n/8) + c + c + c	
$T(n) = T(n/2^k) + kc$	"inductive leap"
$T(n) = T(n/2^{\log n}) + c\log n$	choose k=log n
$T(n) = T(n/n) + c \log n$	
$= T(1) + c\log n = b + c\log n =$	= <i>O</i> (log <i>n</i>)
1/5/05 Fundamentals - Le	cture 2 43



Inductive Proof		
$T(1) = b + c\log 1 = b$ Assume $T(n) = b + c\log n$ T(2n) = T(n) + c $T(2n) = (b + c\log n) + c$	base case hypothesis definition of T(n) by induction hypothesis	
$T(2n) = b + c((\log n) + 1)$ $T(2n) = b + c((\log n) + (\log n) + (\log n))$ $T(2n) = b + c\log(2n)$ Thus: $T(n) = \theta(\log n)$	2)) Q.E.D.	
1/5/05 Fundamer	itals - Lecture 2 4	