Implementing QuickSort with a Stack
CSE 326: Data Structures
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Section 3.3 of the textbook gives a very general, but not very simple, way of replacing recursion by use of a stack. Here is a simpler example. Consider the recursive version of QuickSort, taken right from the CSE 143 lecture slides:

```
procedure QuickSort(int lo, int hi)
{
    if lo <= hi
    {
        int pivotLocation = partition(lo, hi);
        QuickSort(lo, pivotLocation-1);
        QuickSort(pivotLocation+1, hi);
    }
}
```

The details of the function partition aren’t important for our purposes. All you need to know is that it rearranges the keys and returns an index $i$ with the property that all the keys at positions $lo, \ldots, i - 1$ are less than or equal to the key at position $i$, and all the keys at positions $i + 1, \ldots, hi$ are greater than or equal to the key at position $i$.

Here is a simple version of this procedure using a stack $S$ to implement the recursion. The entries on the stack will be pairs of integers.

```
procedure QuickSort(int lo, int hi)
{
    int pivotLocation;
    push(<0,-1>, S); // a marker to identify the bottom of the stack
    while !IsEmptyStack(S)
    {
        while lo <= hi
        {
            pivotLocation = partition(lo, hi);
            Push(<pivotLocation+1,hi>, S); // record second recursive call
            hi = pivotLocation-1; // execute first recursive call
        }
        <lo,hi> = Pop(S); // fetch next recursive call to execute
    }
}
```