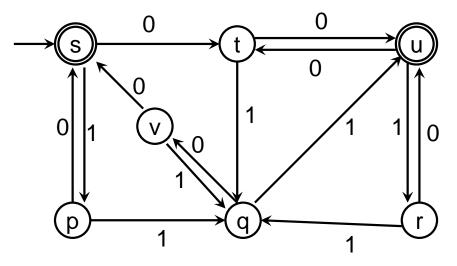
CSE 322 Winter 2008 Assignment #5

Due: Friday, February 22, 2008

Reading assignment: Read Section 2.1 of Sipser's book and the handout on Chomsky Normal Form.

Problems:

1. Apply the state minimization algorithm to the DFA below. Show each of your steps as in the example on the minimization handout.



- 2. Design context-free grammars that generate each of the following languages. Justify your grammar designs.
 - (a) The set $\{w \in \{0,1\}^* \mid w = w^R\}$.
 - (b) The complement of the language $\{a^nb^n \mid n \ge 0\}$ in $\{a, b\}^*$.
 - (c) The set $\{w \in \{0,1\}^* \mid w \text{ contains twice as many 1's as 0's}\}$.
- 3. Sipser's text, 2nd edition Problem 2.16 (1st edition Problem 2.15).
- 4. In class we gave the following grammar

$$S \to (S) \mid SS \mid \varepsilon$$

for the set of strings of balanced parentheses.

- (a) Show that this grammar is ambiguous.
- (b) Give a new unambiguous grammar for the same language.

5. Let $G = (V, \Sigma, R, \langle \text{STMT} \rangle)$ be the following grammar:

$\langle \text{STMT} \rangle$	\rightarrow	$\langle ASSIGN \rangle \mid \langle IF\text{-}THEN \rangle \mid \langle IF\text{-}THEN\text{-}ELSE \rangle$
$\langle \text{IF-THEN} \rangle$	\rightarrow	if condition then $\langle \mathrm{STMT} angle$
$\langle \text{IF-THEN-ELSE} \rangle$	\rightarrow	if condition then $\langle STMT\rangle$ else $\langle STMT\rangle$
$\langle ASSIGN \rangle$	\rightarrow	a := 1

$$\Sigma = \{i, f, c, o, n, d, t, h, e, l, s, a, .; =, 1\}$$

$$V = \{\langle ASSIGN \rangle, \langle STMT \rangle, \langle IF-THEN \rangle, \langle IF-THEN-ELSE \rangle, \langle ASSIGN \rangle \}$$

G is a natural-looking grammar for a fragment of a programming language, but G is ambiguous.

- (a) Show that G is ambiguous.
- (b) Give a new unambiguous grammar for L(G).
- 6. Sipser's text, 2nd edition Problem 2.26 (1st edition Problem 2.19).
- 7. (Extra credit) A CFG G = (V, Σ, R, S) is regular (also known as right-linear) iff every rule of G is of the form A → wB or A → w for w ∈ Σ* and A, B ∈ V. In class we showed that every regular language has a regular grammar. Show the converse, namely that for every regular grammar G, L(G) is regular, which together with what we showed in class shows that regular grammars generate precisely the regular languages.
- 8. (Extra credit) Sipser's text, 2nd edition Problem 2.19 (1st edition Problem 2.25).