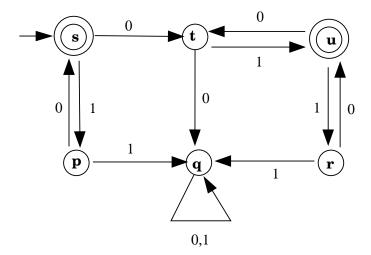
## CSE 322 Winter 2007 Assignment #5

Due: Friday, February 16, 2007

**Reading assignment:** Read Section 2.1 of Sipser's book and the handout on Chomsky Normal Form.

## **Problems:**

1. Apply the state minimization algorithm to the DFA below. Show each of your steps as in the example on the minimization handout.



- 2. Design context-free grammars that generate each of the following languages. Justify your grammar designs.
  - (a) The set  $\{w \in \{0,1\}^* \mid w = w^R\}$ .
  - (b) The complement of the language  $\{a^nb^n\mid n\geq 0\}$  in  $\{a,b\}^*$ .
  - (c) The set  $\{w \in \{0,1\}^* \mid w \text{ contains more 1's than 0's}\}.$
- 3. Sipser's text, 2nd edition Problem 2.16 (1st edition Problem 2.15).

4. Let  $G = (V, \Sigma, R, \langle STMT \rangle)$  be the following grammar:

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\begin{array}{rcl} \langle \text{STMT} \rangle & \rightarrow & \langle \text{ASSIGN} \rangle \mid \langle \text{IF-THEN} \rangle \mid \langle \text{IF-THEN-ELSE} \rangle \\ \langle \text{IF-THEN} \rangle & \rightarrow & \text{if condition then } \langle \text{STMT} \rangle \\ \langle \text{IF-THEN-ELSE} \rangle & \rightarrow & \text{if condition then } \langle \text{STMT} \rangle \mid \text{else } \langle \text{STMT} \rangle \\ \langle \text{ASSIGN} \rangle & \rightarrow & \text{a} := 1 \\ \\ \Sigma & = & \{\text{i,f,c,o,n,d,t,h,e,l,s,a,}, :, =, 1\} \\ \\ V & = & \{\langle \text{ASSIGN} \rangle, \langle \text{STMT} \rangle, \langle \text{IF-THEN} \rangle, \langle \text{IF-THEN-ELSE} \rangle, \langle \text{ASSIGN} \rangle \} \end{array}
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G is a natural-looking grammar for a fragment of a programming language, but G is ambiguous.

- (a) Show that G is ambiguous.
- (b) Give a new unambiguous grammar for L(G).
- 5. Convert the following grammar to Chomsky normal form using the procedure on the handout.

$$\begin{array}{cccc} S & \rightarrow & A \mid ABa \mid AbA \\ A & \rightarrow & Aa \mid \epsilon \\ B & \rightarrow & Bb \mid BC \\ C & \rightarrow & CB \mid CA \mid bB \end{array}$$

- 6. Sipser's text, 2nd edition Problem 2.26 (1st edition Problem 2.19).
- 7. (Extra credit) A CFG  $G=(V,\Sigma,R,S)$  is regular (also known as right-linear) iff every rule of G is of the form  $A\to wB$  or  $A\to w$  for  $w\in \Sigma^*$  and  $A,B\in V$ . In class we showed that every regular language has a regular grammar. Show the converse, namely that for every regular grammar G, L(G) is regular, which together with what we showed in class shows that regular grammars generate precisely the regular languages.
- 8. (Extra credit) Sipser's text, 2nd edition Problem 2.19 (1st edition Problem 2.25).