CSE 322 Spring 2005 Assignment #8

Due: Friday, June 3, 2005

Reading assignment: Read Chapter 4 of Sipser's text.

Problems:

- 1. Sipser's text, page 169, Exercise 4.7. (Note that infinite binary sequences are not strings since any string has finite length.)
- 2. Sipser's text, page 169, Exercise 4.8.
- 3. Sipser's text, page 169, Exercise 4.5.
- 4. Sipser's text, page 169, Problem 4.11.
- 5. Define a *queue* automaton $M = (Q, \Sigma, \Gamma, \delta, q_0, q_{accept}, q_{reject})$ where Q is the finite set of *states*, Σ is the *input alphabet*, Γ is the *queue alphabet*, q_0 is the *start state*, q_{accept} and q_{reject} are *accept* and *reject* states respectively, and

$$\delta: Q \times (\Sigma \cup \{\varepsilon\}) \times (\Gamma \cup \{\varepsilon\}) \to Q \times (\Gamma \cup \varepsilon).$$

A configuration of a queue automaton is an element of $Q \times \Sigma^* \times \Gamma^*$; configuration (q, y, z) represents that the current state is q, the remaining input is y, the current contents of the queue is z (with the left-most character on the left end of z).

If $\delta(p, a, A) = (q, B)$ where $A, B \in \Gamma \cup \{\varepsilon\}$ then its action on configurations is to take (p, ay, Az) to (q, y, zB).

That is, a queue automaton is like a DPDA except that it has a queue instead of a stack.

Sketch how queue automata are equivalent to Turing machines.

(HINT: to simulate one step of the TM might require going through the entire queue of the queue automaton.)

- 6. (Bonus) Sipser's text page 170, Problem 4.20
- 7. (Bonus) Sipser's text page 169, Problem 4.9