


$$\exists x P(x)$$

$\exists$  an integer  $x$  st  $\sqrt{x}$  is rational

$$x = 4 \quad \sqrt{4} = 2$$


"constructive" proof

non-constructive existence pf

" $\exists x, y$  both irrational st.  $x^y$  is rational"

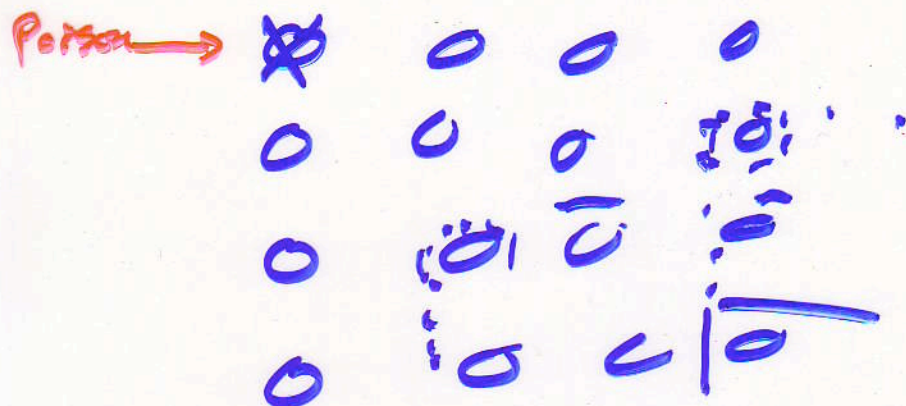
$$x = \sqrt{2}, y = \sqrt{2}$$

$$(\sqrt{2})^{\sqrt{2}}$$

$$x = (\sqrt{2})^{\sqrt{2}} \quad y = \sqrt{2}$$

$$x^y = ((\sqrt{2})^{\sqrt{2}})^{\sqrt{2}} = (\sqrt{2})^{\sqrt{2} \cdot \sqrt{2}} = \sqrt{2}^2 = 2$$

# "Chomp"

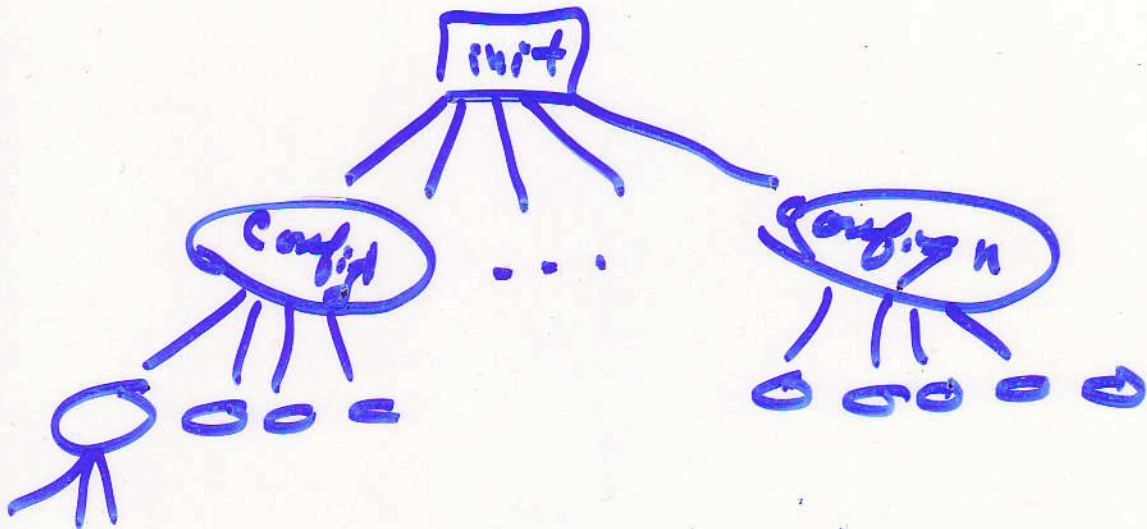


## Rules

- 2 players
- Your turn: pick a cookie, + all below & right of it
- Who ever takes last cookie loses & dies (yes, rated "M" for mature violence...)

Q: Does player 1 have a winning strategy?

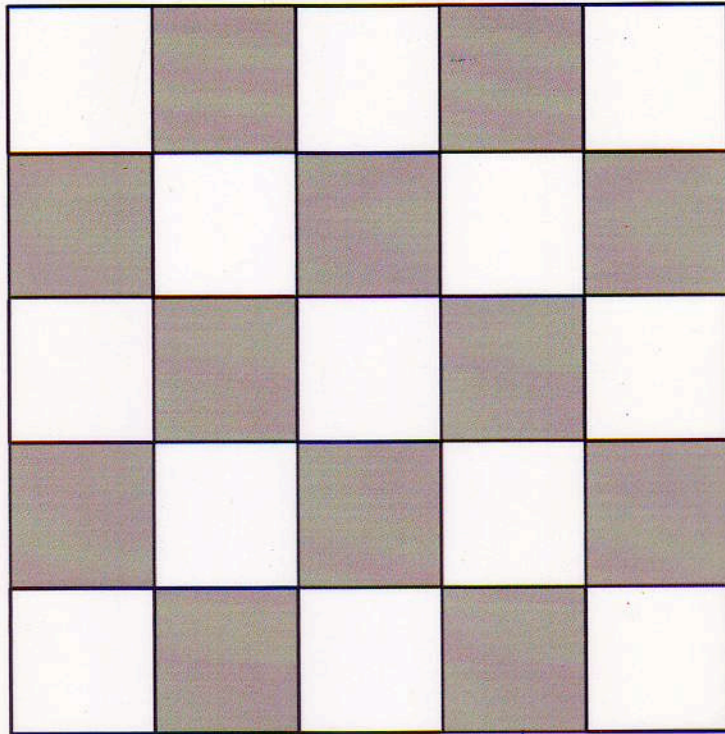
A: Yes! but non constructive...



...

#1  
dead  
F





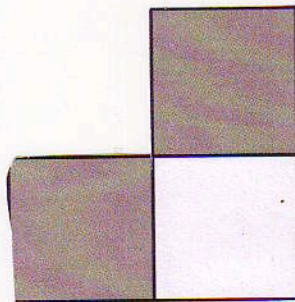
Various Questions:

What kinds/shapes of checkerboards  
can be tiled with

(a) dominoes



(b) tri-ominos



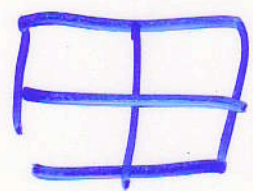
$P(n)$ : any  $2^n \times 2^n$  board missing any one square can be tiled with 'L's'.

Basic

$n=0$



$n=1$



~~$n=2$~~

~~$4 \times 4$~~

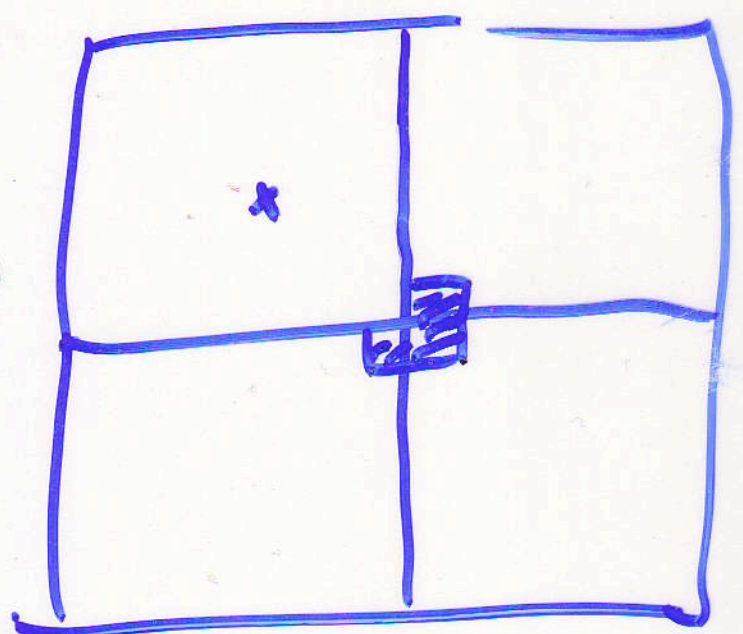
~~$2^{n+1} \times 2^{n+1}$~~



$P(n) \rightarrow P(n+1)$

allows hypothetical tilings of  $2^n \times 2^n$  boards to be used to build  $2^{n+1} \times 2^{n+1}$  tiling

$2^{n+1}$



ind. step

$\forall n P(n)$