CSE 321: Discrete Structures Assignment #1 September 28, 2007 Due: Friday, October 5

Reading Assignment: Read Sections 1.1-1.4 (make sure that you understand the examples).

Problems.

- 1. Let p, q, r be the propositions
 - p: You get sued by the Motion Picture Association of America (MPAA).
 - *q*: You illegally download *Dumb and Dumber 2* (DD2).
 - *r*: You go to prison for 2 years.

Write these propositions using p, q, r and logical connectives.

- (a) You go to prison for 2 years, but you do not illegally download DD2.
- (b) You are sued by the MPAA, you illegally download DD2, and you go to prison for 2 years.
- (c) To get sued by the MPAA, it is necessary for you to illegally download DD2.
- (d) You are sued by the MPAA, but you don't illegally download DD2; nevertheless, you go to prison for 2 years.
- (e) Getting sued by the MPAA and illegally downloading DD2 is sufficient to get you sent to prison for 2 years.
- (f) You will go to prison for 2 years if and only if you either illegally download DD2 or you are sued by the MPAA.
- 2. Write each of these statements in the form "if p, then q" in English. [Hint: Refer to the list of common ways to express conditional statements provide in Section 1.1]
 - (a) I will remember to send you the address only if you send me an e-mail message.
 - (b) To be a citizen of this country, it is sufficient that you were born in the U.S.
 - (c) If you keep your textbook, it will be a useful reference in your future courses.
 - (d) The Sonics will move to New Orleans unless they get a new arena.
 - (e) That you get the job implies that you had the best résumé.
 - (f) The beach erodes whenever there is a storm.
 - (g) It is necessary to have a valid password to log on to the server.
 - (h) You will reach the summit unless you begin your climb too late.

- 3. State in English the converse and contrapositive of each of the following implications.
 - (a) If a is pushed onto the stack before b, then b is popped before a.
 - (b) If the input is correct and the program terminates, then the output is correct. (Be sure to use De Morgan's Law to simplify the contrapositive.)
- 4. On the island of Homvurkia, knights always tell the truth and knaves always lie. You encounter two people, A and B. Determine, if possible, what A and B are if they address you in the ways described. If you cannot determine what these two people are, can you draw any conclusions?
 - (a) A says "The two of us are both knights" and B says "A is a knave."
 - (b) Both A and B say "I am a knight."
- 5. The following two statements form the basis of the most important methods for automated theorem proving. Use truth tables to prove that they are tautologies.
 - (a) Resolution: $((p \lor q) \land (\neg q \lor r)) \rightarrow (p \lor r)$
 - (b) Modus ponens: $((p \land (p \rightarrow q)) \rightarrow q$
- 6. Show that Modus ponens is a tautology without using a truth table. Show each step and indicate which logical equivalences you use.
- 7. Show that $(p \to q) \lor (p \to r)$ and $p \to (q \lor r)$ are logically equivalent.
- 8. Give the negation of each of the following statements.
 - All good students study hard.
 - Some birds fly south for the winter.
 - No liberal arts majors are unable to use a computer.
 - $\forall x \exists y \ x = y^2$
- 9. Extra Credit: You have two memory registers, each with the same number of bits. You have an operation, ZOR (R1, R2), which takes two registers, R1 and R2, and stores R1 ⊕ R2 in R1, where x̄ flips all the bits in x and ⊕ is the exclusive-OR operator. Show how you can swap the contents of the two registers using a sequence of ZOR instructions without temporary memory registers. Explain why this works.