

## Discrete Distributions

Distribution	Parameters	Description	Range $\Omega_X$	$\mathbb{E}[X]$	$\text{Var}(X)$	PMF $p_X(k)$ for $k \in \Omega_X$
Uniform (disc)	$X \sim \text{Unif}(a, b)$ for $a, b \in \mathbb{Z}$ and $a \leq b$	Equally likely to be any integer in $[a, b]$	$\{a, \dots, b\}$	$\frac{a+b}{2}$	$\frac{(b-a)(b-a+2)}{12}$	$\frac{1}{b-a+1}$
Bernoulli	$X \sim \text{Ber}(p)$ for $p \in [0, 1]$	Takes value 1 with prob $p$ and 0 with prob $1-p$	$\{0, 1\}$	$p$	$p(1-p)$	$p^k(1-p)^{1-k}$
Binomial	$X \sim \text{Bin}(n, p)$ for $n \in \mathbb{N}, p \in [0, 1]$	Sum of $n$ iid $\text{Ber}(p)$ rvs. # of heads in $n$ independent coin flips with $\mathbb{P}(\text{head}) = p$	$\{0, 1, \dots, n\}$	$np$	$np(1-p)$	$\binom{n}{k} p^k (1-p)^{n-k}$
Poisson	$X \sim \text{Poi}(\lambda)$ for $\lambda > 0$	# of events that occur in one unit of time independently with rate $\lambda$ per unit time	$\{0, 1, \dots\}$	$\lambda$	$\lambda$	$e^{-\lambda} \frac{\lambda^k}{k!}$
Geometric	$X \sim \text{Geo}(p)$ for $p \in [0, 1]$	# of independent Bernoulli trials with parameter $p$ up to and including first success	$\{1, 2, \dots\}$	$\frac{1}{p}$	$\frac{1-p}{p^2}$	$(1-p)^{k-1} p$

## Continuous Distributions

Distribution	Parameters	Description	Range $\Omega_X$	$\mathbb{E}[X]$	$\text{Var}(X)$	PDF $f_X(x)$ for $x \in \Omega_X$	CDF $F_X(x) = \mathbb{P}(X \leq x)$
Uniform	$X \sim \text{Unif}(a, b)$ for $a < b$	Equally likely to be any real number in $[a, b]$	$[a, b]$	$\frac{a+b}{2}$	$\frac{(b-a)^2}{12}$	$\frac{1}{b-a}$	$\begin{cases} 0 & \text{if } x < a \\ \frac{x-a}{b-a} & \text{if } a \leq x < b \\ 1 & \text{if } x \geq b \end{cases}$
Exponential	$X \sim \text{Exp}(\lambda)$ for $\lambda > 0$	Time until first event in Poisson process	$[0, \infty)$	$\frac{1}{\lambda}$	$\frac{1}{\lambda^2}$	$\lambda e^{-\lambda x}$	$\begin{cases} 0 & \text{if } x < 0 \\ 1 - e^{-\lambda x} & \text{if } x \geq 0 \end{cases}$
Normal	$X \sim N(\mu, \sigma^2)$ for $\mu \in \mathbb{R},$ $\sigma^2 > 0$	Standard bell curve	$(-\infty, \infty)$	$\mu$	$\sigma^2$	$\frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$	$\Phi\left(\frac{x-\mu}{\sigma}\right)$