

## Another Example

Suppose you shuffle a deck of cards so any arrangement is equally likely. What is the probability that the top two cards have the same value?

Sample Space

Probability Measure

Event

Probability

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## Uniform Probability Space

The most common probability measure is the **uniform** probability measure. In the uniform measure, for every event  $E$

$$\mathbb{P}(E) = \frac{|E|}{|\Omega|}.$$

Let your sample space be all possible outcomes of a sequence of 100 coin tosses. Assign the uniform measure to this sample space. What is the probability of the event "there are exactly 50 heads?"

A.  $\binom{100}{50}/2^{100}$

B.  $1/101$

C.  $1/2$

D.  $1/2^{50}$

E. There is not enough information in this problem.

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# Conditional Probability

## Conditional Probability

For an event  $B$ , with  $\mathbb{P}(B) > 0$ ,  
the “Probability of  $A$  conditioned on  $B$ ” is

$$\mathbb{P}(A|B) = \frac{\mathbb{P}(A \cap B)}{\mathbb{P}(B)}$$

Just like with the formal definition of probability, this is pretty abstract.  
It does accurately reflect what happens in the real world.

If  $\mathbb{P}(B) = 0$ , we can't condition on it (it can't happen! There's no point in defining probabilities where we know  $B$  has not happened) –  $\mathbb{P}(A|B)$  is **undefined** when  $\mathbb{P}(B) = 0$ .

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## Conditioning Practice

Red die 6  
conditioned on  
sum 7

Red die 6  
conditioned on  
sum 9

Sum 7 conditioned  
on red die 6

Take a few minutes to work on  
this with the people around you!  
(also on your handout)

	D2=1	D2=2	D2=3	D2=4	D2=5	D2=6
D1=1	(1,1)	(1,2)	(1,3)	(1,4)	(1,5)	(1,6)
D1=2	(2,1)	(2,2)	(2,3)	(2,4)	(2,5)	(2,6)
D1=3	(3,1)	(3,2)	(3,3)	(3,4)	(3,5)	(3,6)
D1=4	(4,1)	(4,2)	(4,3)	(4,4)	(4,5)	(4,6)
D1=5	(5,1)	(5,2)	(5,3)	(5,4)	(5,5)	(5,6)
D1=6	(6,1)	(6,2)	(6,3)	(6,4)	(6,5)	(6,6)

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