

# Biased

One property we might want from an estimator is for it to be **unbiased**.

**An estimator  $\hat{\theta}$  is “unbiased” if**  
$$\mathbb{E}[\hat{\theta}] = \theta$$

The expectation is taken over the randomness in the samples we drew.  
The formula is fixed, the data we draw to evaluate the formula becomes the source of the randomness.

So we're not consistently overestimating or underestimating.

If an estimator isn't unbiased then it's **biased**.

# Are our MLEs biased?

Our estimate for the coin-flips (if we generalized a bit) would be

$$\frac{\text{num heads}}{\text{total flips}}$$

Is this biased or unbiased?