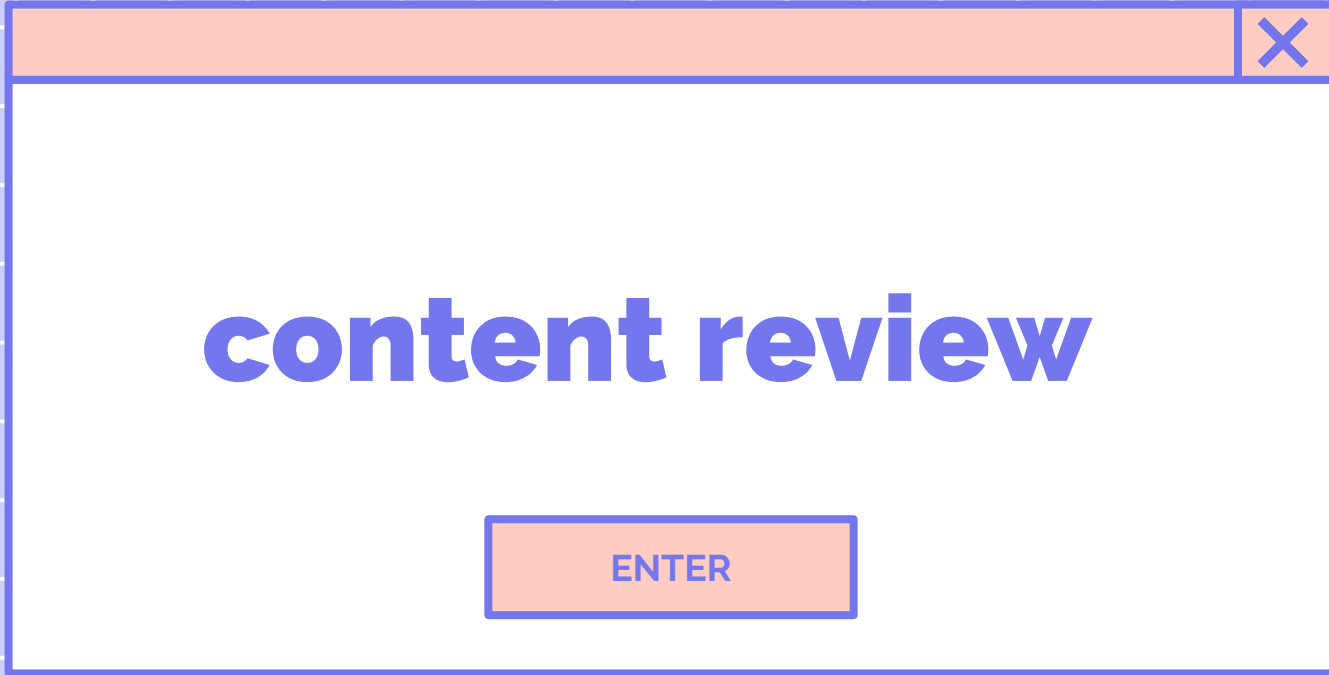


cse 312
winter 2024

ENTER



week 3 :)



content review

ENTER



What we talked about this week



01

Conditional probability

Bayes' rule

Law of total probability

Chain rule

02

03

More about events

04

Independence

Independence

Conditional independence



Conditional Probability



Credit: Super Mario Wiki



Conditional Probability



01

$P(A|B)$

probability of the event A occurring
given that
the event B occurs

02

“what is the probability that event A happens given that event B happened?”

03

04





Conditional Probability



01

$P(A|B)$

probability of the event A occurring
given that
the event B occurs

02

“what is the probability that event A happens after learning that event B happened?”

03

04

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$





Conditional Probability



01

$P(A|B)$

probability of the event A occurring
given that
the event B occurs

02

“what is the probability that event A happens given that event B happened?”

03

$$P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{P(B|A) P(A)}{P(B)}$$

-BAYES RULE-

04



TIPS:

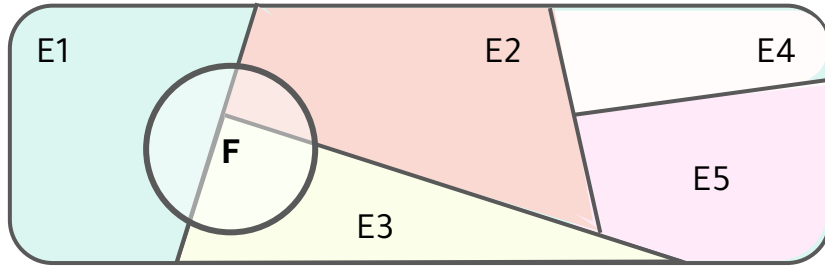
- start by writing all the probabilities you know
- write down what you want to find

Conditional Probability

We can use conditional probability to help calculate more complex probabilities!

Conditional Probability - LTP

we can *partition* a sample space into discrete events



$$\Omega = E1 \cup E2 \cup E3 \dots$$

divided the set of all possible outcomes into "disjoint" event sets

The probability of any other event F that is inside of this sample space Ω is

$$\begin{aligned} P(F) &= P(F \cap E1) + P(F \cap E2) \dots + P(F \cap E5) && \text{by definition of} \\ &= P(F | E1)P(E1) + P(F | E2)P(E2) + \dots + P(F | E5)P(E5) && \text{cond. probability ->} \end{aligned}$$

-LAW OF TOTAL PROBABILITY-

Conditional Probability - Chain Rule

sometimes we have a **sequential process** and want to find the probability of that
e.g., finding the probability that event E1 happened, then event E2 happens, then event En happens

$$P(E1 \cap E2 \cap E3 \cap \dots \cap En) =$$

$$P(E1) \cdot P(E2 | E1) \cdot P(E3 | E2 \cap E1) \cdot \dots \cdot P(En | E1 \cap E2 \cap \dots \cap E(n-1))$$

—CHAIN RULE—

watch out for sometimes when the counting method may be easier

multiplying probability of each event happening conditioned on all the previous events

Connecting Chain rule, Bayes' Rule, &

LTP

Chain Rule!

$P(A|B)$

$$= \frac{P(A \cap B)}{P(B)} = \frac{P(B|A) P(A)}{P(B|A) P(A) + P(B|A^c) P(A^c)}$$

Law of Total Probability!

Independence

Independence

two events are independent if there is no correlation between the events and they don't depend on each other

two events A, B are statistically **independent** if

$$P(A \cap B) = P(A) \cdot P(B)$$

or

$$P(A | B) = P(A) \text{ and } P(B | A) = P(B)$$

“knowing that B happened doesn't affect the probability that A will happen and vice versa”

“knowing that B happened doesn't give any new information about A”

Just because 2 events may “sound like” they're independent, that doesn't mean that they are *statistically* independent

Conditional Independence

two events A, B are conditionally independent if
$$P((A \cap B) | C) = P(A | C) \cdot P(B | C)$$

Just because 2 events may “sound like” they’re independent,
that doesn’t mean that they are *statistically* independent



Thank you!

OK

