

CSE 312: Foundations of Computing II

**Instructor:** Alex Tsun

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**Lecture Topics:** 2.3 Independence, 3.1 Discrete Random Variables Basics

[Tags: Independence, Random Variables, PMFs, Expectation, PSet2 Q8 (Similar)]

1. There are 3 people in Alex's family; his mom, dad, and sister. Each family member decides whether or not they want to come to lunch in his social-distancing home restaurant, independently of the others.
  - Mom wants to come with probability **0.8**.
  - Dad wants to come with probability **0.6**.
  - Sister wants to come with probability **0.1**.

Unfortunately, if all 3 of them want to come, he must turn one of them away ☹ since the restaurant capacity is 2 guests. Otherwise, he will take everyone that comes. Let  $X$  be the number of customers that Alex serves at lunch.

- a. What is the range  $\Omega_X$ , the PMF  $p_X(k)$ , and the expectation  $E[X]$ ?
- b. If he charges everyone who comes \$10, but it costs him \$50 to make all the food, what is his expected profit?

[Tags: Chain Rule, Inclusion-Exclusion]

2. Suppose  $n$  people sit around a table. Each person orders a different dish, but the waiter did not mark positions unfortunately. He has the correct  $n$  dishes, but gives a random dish to each person (each of the  $n!$  assignments is equally likely). What is the probability that no one has the dish they ordered placed in front of them?

