1. Use the CLT to approximate the following probabilities. Don’t forget to apply the continuity correction (only if necessary).
   a. Suppose we roll a fair 10-sided die until we get 100 sevens. What is the probability it takes at least 1050 rolls until this happens?
   b. Let $X$ be the sum of 10,000 real numbers, and $Y$ be the same sum, but with each number rounded to the nearest integer before summing. If the fractions rounded off are independent and each one is uniformly distributed over $(-0.5, +0.5)$, use the Central Limit Theorem to estimate the probability that $|X - Y| > 50$. Noticing that $|X - Y|$ could have been as great as 5,000, look at your answer and think about what it says. (As a small example with sums of 4 real numbers, suppose that $X = 3.2 + 1.92 + (-3.6) + 5.7$. Then $Y$ would be the sum of each of those terms when rounded to the nearest integer: $Y = 3 + 2 + (-4) + 6 = 7$. So, $|X - Y| = 1.3$. The fractions rounded off in this case are $(0.2, -0.08, 0.4, -0.3)$ and the assumption is that these fractions are independent and uniformly distributed in the real interval $(-0.5, +0.5)$.

2. Megha has a health condition that requires unpredictable amounts of medication. Every day, there is a 20% chance that she feels perfectly fine and requires no medicine. Otherwise, she needs to take a dose of medication. The necessary dose is equally likely to be any value in the continuous range 1 to 5 ounces. How much medicine she needs on any given day is independent of all other days. Megha’s insurance will fully cover 90 ounces of medicine for each 30-day period. What is the probability that 90 ounces will be enough for the next 30 days? Make your life easier by using Central Limit Theorem.