

This generalizes to n steps.

Ex: How many n -bit strings are there? 2^n
 $\underbrace{2 \cdot 2 \cdot 2 \cdots 2}_n$

Ex: How many subsets does an n -element set have? $\{a_1, a_2, \dots, a_n\}$. 2^n
 For each a_i , choose to put it in the subset or leave it out.

Ex: How many 4-character passwords, where each is either a lower-case letter or a digit, and the first has to be a letter? $26 \cdot 36^3$

Ex: Same, but no restriction on first character, and no character can be repeated? $36 \cdot 35 \cdot 34 \cdot 33$

Permutations:

How many ~~sequences~~ sequences using $\{1, 2, 3\}$ are there, in which each is used exactly once?
 $3 \cdot 2 \cdot 1 = 6$

How many using $\{1, 2, \dots, n\}$?

$$n(n-1)(n-2) \cdots 3 \cdot 2 \cdot 1 = n! \quad 0! = 1.$$

k-permutations: How many sequences of length k use the characters $\{1, 2, \dots, n\}$ each either 0 or 1 time?

$$P(n, k) = n(n-1)(n-2) \cdots (n-k+1) = \frac{n!}{(n-k)!}$$

Back to the password example:

$$P(36, 4) = \frac{36!}{32!}$$