

CSE 312

Probability: reasoning under uncertainty

Motivation:

CSE examples:

1. Performance: events happen randomly, such as component failures, arrivals of packets at servers, workloads
2. Patterns in data: data mining.
Amazon recommendations for products,
Netflix recommendations for movies,
spam filtering
3. Algorithm design: using random numbers to speed up algorithms.

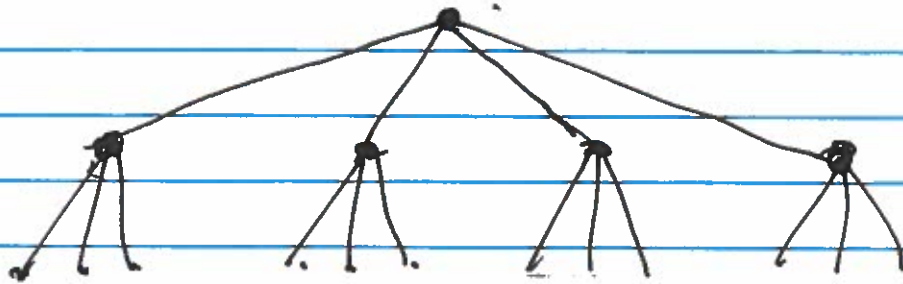
Counting.

Motivation: If some probabilistic experiment has a finite set Ω of equally likely outcomes (e.g., rolling a fair die), the probability of an event $A \subseteq \Omega$ is

$$P(A) = \frac{|A|}{|\Omega|}$$

Product rule: If there are m choices for step 1 and, for each choice, there are n choices for step 2, then there are mn choices in total.

2



Step 1
 $m=4$
Step 2
 $n=3$

$$mn = 12$$

Generalizes easily to s steps.

Ex: How many n -bit strings are there? $2^n = \overbrace{2 \cdots 2 \cdot 2}^n$

Ex: How many 7-digit phone numbers, if the first digit can't be 0 or 1? 8×10^6