

the central limit theorem (CLT)

Consider i.i.d. (independent, identically distributed) random vars X_1, X_2, X_3, \dots *could be discrete.*

X_i has $\mu = E[X_i]$ and $\sigma^2 = \text{Var}[X_i]$

Unif(10, 11, 12, ..., 140)

As $n \rightarrow \infty$,

$$\frac{X_1 + X_2 + \dots + X_n - n\mu}{\sigma\sqrt{n}} \longrightarrow N(0, 1)$$

Restated: As $n \rightarrow \infty$,

$$M_n = \frac{1}{n} \sum_{i=1}^n X_i \rightarrow N\left(\mu, \frac{\sigma^2}{n}\right)$$

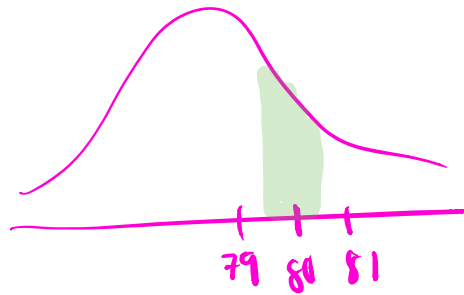
$$X_i \sim \text{Ber}(0.2)$$

$$\sum_{i=1}^{100} X_i \sim \text{Bin}(100, 0.2)$$

$$\Pr\left(\sum_{i=1}^{100} X_i = 80\right)$$



$$\approx \Pr(79.5 \leq \sum_{i=1}^{100} X_i \leq 80.5)$$



"continuity correction"

