- 1. A license plate has the form AXYZBCD, where A, B, C, and D are integers and X, Y, and Z are upper case letters. What is the number of different license plates that can be created?
- 2. A chef is preparing desserts for the week, starting on a Sunday. On each day, only one of five desserts (apple pie, cherry pie, strawberry pie, pineapple pie, and cake) may be served. On Thursday there is a birthday, so cake must be served that day. On no two consecutive days can the chef serve the same dessert. How many dessert combinations are there for the week?
- 3. A store has 4 books, 14 movies, 6 toys, and 5 posters. In how many ways can a customer buy exactly 1 item from each of exactly 3 categories?
- 4. In Schnapsen, assuming the stock is not closed, no one has exchanged the jack of trumps, and no marriage has been declared, how many possible orderings of the cards face-down in the stock are there, given the cards you have seen . . .
 - (a) ... before trick 1?
 - (b) ... before trick 2?
 - (c) ... before trick 3?
 - (d) ... before trick 4?
 - (e) ... before trick 5?
- 5. In how many different ways can you arrange seven people around a circular table?
- 6. Suppose that 8 people, including you and a friend, line up for a picture. In how many ways can the photographer organize the line if she wants to have fewer than 2 people between you and your friend?
- 7. Your CSE 312 teaching staff lines up for a picture. How many possible arrangements are there with Maestro Tompa not at either end of the line?
- 8. How many ways are there to permute the 8 letters A, B, C, D, E, F, G, H so that A is not at the beginning and H is not at the end?
- 9. There are 40 seats and 40 students in a classroom. Suppose that the front row contains 10 seats, and there are 5 students who must sit in the front row in order to see the board clearly. How many seating arrangements are possible with this restriction?
- 10. Permutations of objects, some of which are indistinguishable.
 - (a) How many permutations are there of the letters in DAWGY?

- (b) How many permutations are there of the letters in DOGGY?
- (c) How many permutations are there of the letters in GODOGGY?
- 11. The game of bridge is played with a deck of 52 cards divided into 4 suits (black ♠, red ♡, black ♣, and red ◊) of 13 cards (2, 3, 4, 5, 6, 7, 8, 9, 10, J, Q, K, A) each. A bridge hand consists of 13 cards dealt from a shuffled deck. Given a bridge hand consisting of 5 spades, 2 hearts, 3 diamonds, and 3 clubs, in how many ways can the hand be arranged so that the cards of each suit are together...
 - (a) ... but not necessarily sorted by rank within each suit?
 - (b) ... and each suit is sorted in ascending rank order?
 - (c) ... and each suit is sorted in ascending rank order and the suits are arranged so that the suit colors alternate?
- 12. Suppose two cards are drawn in order from a bridge deck. In how many ways can the first card be a diamond and the second card a jack?
- 13. Rabbits Peter and Pauline have three offspring: Flopsie, Mopsie, and Cotton-tail. These five rabbits are to be distributed to four different pet stores so that no store gets both a parent and a child. It is not required that every store gets a rabbit. In how many different ways can this be done?
- 14. You are playing a game of Schnapsen against the Maestro. The cards you have not seen yet during the current deal are the following:
 - ♠ TKJ
 - ♥ ATOJ
 - ♣ AT
 - ♦ KQJ

Of the possible 5-card hands the Maestro could be holding, how many of them contain at least 18 trick points? Try to find the simplest way to solve this exercise.

- 15. You have 12 red beads, 16 green beads, and 20 blue beads. How many distinguishable ways are there to place the beads on a string, assuming that beads of the same color are indistinguishable? (The string has a loose end and a tied end, so that reversing the order of the beads gives a different arrangement, unless the pattern of colors happens to form a palindrome.) Try solving the problem two different ways, once using permutations and once using using combinations.
- 16. There are 12 points on a plane. Five of them are collinear and, other than these, no three are collinear.
 - (a) How many lines, each containing at least 2 of the 12 points, can be formed?
 - (b) How many triangles, each containing at least 3 of the 12 points, can be formed?

- 17. You have a triangular prism with top and bottom both being congruent equilateral triangles and the three sides being congruent rectangles. If you pick 5 out of 7 different colors, one to paint each of the 5 faces, how many differently painted triangular prisms can you get? Just rotating the prism does not constitute a different color scheme.
- 18. There are 6 men and 7 women in a ballroom dancing class. If 4 men and 4 women are chosen and paired off, how many pairings are possible?
- 19. How many ways are there to seat 10 people, consisting of 5 couples, in a row of 10 seats if ...
 - (a) ...the seats are assigned arbitrarily?
 - (b) ... all couples are to get adjacent seats?
 - (c) ...the seats are assigned arbitrarily, except that one couple insists on not sitting in adjacent seats?
- 20. How many bridge hands have a suit distribution of 5, 5, 2, 1? (That is, you have 5 cards of one suit, 5 cards of another suit, 2 of another suit, and 1 of the last suit.)
- 21. A hand in "draw poker" consists of 5 cards dealt from a shuffled 52-card bridge deck.
 - (a) How many different hands are there that form a flush? (A hand is said to form a flush if all 5 cards are from the same suit.)
 - (b) How many different hands are there that form a straight? (A hand is said to form a straight if the ranks of all 5 cards form an incrementing sequence. The suits do not matter. The lowest straight is A, 2, 3, 4, 5 and the highest straight is 10, J, Q, K, A.)
 - (c) How many different hands are there that form one pair? (This occurs when the cards have ranks a, a, b, c, d, where a, b, c, and d are all distinct. The suits do not matter.)
 - (d) How many different hands are there that form two pairs? (This occurs when the cards have ranks a, a, b, b, c, where a, b, and c are all distinct. The suits do not matter.)
 - (e) How many different hands are there that form three of a kind? (This occurs when the cards have ranks a, a, a, b, c, where a, b, and c are all distinct. The suits do not matter.)
 - (f) How many different hands are there that form a full house? (This occurs when the cards have ranks a, a, a, b, b, where a and b are distinct. The suits do not matter.)
 - (g) How many different hands are there that form four of a kind? (This occurs when the cards have ranks a, a, a, a, b. The suit do not matter.)