CSE 312: Foundations of Computing II
Quiz Section \#3

1. Given 3 spades and 3 hearts, shuffle them. Compute $\mathrm{P}(E)$, where $E$ is the event that the suits of the shuffled cards are in alternating order. What is your sample space?
2. Suppose you pick two cards from a well-shuffled Schnapsen deck. What is the probability that they are both queens?
3. Suppose you deal 13 cards from a well-shuffled bridge deck of 52 cards. What is the probability that the distribution of suits is $4,4,3,2$ ? (That is, you have 4 cards of one suit, 4 cards of another suit, 3 cards of another suit, and 2 cards of the last suit.)
4. Novice poker players are often confused about whether a flush beats a straight. For draw poker (see quiz section \#2 worksheet, exercise \#9):
(a) Compute the probability of being dealt a flush.
(b) Compute the probability of being dealt a straight.
(c) Which of these hands should beat the other, given your answers to (a) and (b)?
5. In Schnapsen, suppose that $\boldsymbol{J}$ is the face-up trump and you are dealt 5 nontrump cards. Let $E$ be the event that the top 4 cards in the stock are all trumps. Let the sample space be all possible orderings of all the cards in the stock. Compute $\mathrm{P}(E)$. (Notice that your solution suggests a different and simpler sample space.)
6. Suppose you are taking a multiple-choice test that has $c$ answer choices for each question. In answering a question on this test, the probability that you know the correct answer is $p$. If you don't know the answer, you choose one at random. What is the probability that you knew the correct answer to a question, given that you answered it correctly?
7. An urn contains 3 black balls and 4 white balls.
(a) Suppose 3 balls are drawn from the urn without replacement. What is the probability that all 3 are white? Try computing this in the sample space where the order of the 3 draws does not matter, and then in the sample space where the order does matter.
(b) Suppose 3 balls are drawn from the urn with replacement. What is the probability that all 3 are white? Describe the sample space precisely.
8. (Challenge problem) $n$ people at a reception give their hats to a hat-check person. When they leave, the hat-check person gives each of them a hat chosen at random. What is the probability that no one gets their own hat back?
