Quiz Section 2: Circuits and Predicate Logic

Task 1 – Translate to English

Translate these system specifications into English where F(p) is "Printer p is out of service", B(p) is "Printer p is busy", L(j) is "Print job j is lost," and Q(j) is "Print job j is queued". Let the domain be all printers and all print jobs.

- a) $\exists p \ (F(p) \land B(p)) \rightarrow \exists j \ L(j)$
- **b)** $(\forall j \ B(j)) \rightarrow (\exists p \ Q(p))$
- c) $\exists j (Q(j) \land L(j)) \rightarrow \exists p F(p)$
- **d)** $(\forall p \ B(p) \land \forall j \ Q(j)) \rightarrow \exists j \ L(j)$

Task 2 – Equivalences

Prove that each of the following pairs of propositional formulas are equivalent using the specified method(s).

a) $(p \rightarrow \neg p) \land (\neg p \rightarrow p)$ vs. F

Use cozy at the following url (https://tinyurl.com/CSE311S21a) to complete the problem online.

b) $\neg p \rightarrow (q \rightarrow r)$ vs. $q \rightarrow (p \lor r)$ using (i) truth tables and (ii) propositional equivalences.

Use cozy at the following url (https://tinyurl.com/CSE311S21b) to complete the problem online.

Task 3 – Non-equivalence

Prove that the following pairs of propositional formulas are not equivalent using a truth table and specifying an input they differ on.

a) $p \rightarrow r \text{ vs. } r \rightarrow p$

b) $a \rightarrow (b \land c)$ vs. $(a \rightarrow b) \land c$

Task 4 – More Circuits

- a) Let Q be defined by $Q(p,q) = (\neg p) \oplus q$. Using only NOT, OR and Q gates express the logical expression $(a \land b) \oplus c$.
- **b)** Draw a circuit that represents the logical expression from part a.

Task 5 – Boolean Algebra

For each of the following parts, write the logical expression using boolean algebra operators. Then, simplify it using axioms and theorems of boolean algebra.

a) $\neg p \lor (\neg q \lor (p \land q))$

b) $\neg (p \lor (q \land p))$

Task 6 – Canonical Forms

Consider the boolean functions F(A, B, C) and G(A, B, C) specified by the following truth table:

A	B	C	F(A, B, C)	G(A, B, C)
1	1	1	1	1
1	1	0	1	1
1	0	1	0	1
1	0	0	0	0
0	1	1	1	1
0	1	0	1	0
0	0	1	0	1
0	0	0	1	0

a) Write the DNF and CNF expressions for F(A, B, C).

- **b)** Write the DNF and CNF expressions in boolean algebra for G(A, B, C).
- c) Simplify your CNF form for G(A, B, C).