

A Proof Outline

Claim: $\{0^k 1^k : k \geq 0\}$ is an irregular language.

Proof:

Suppose, for the sake of contradiction, that $\{0^k 1^k : k \geq 0\}$ is regular.

Then there is a DFA M such that M accepts exactly $\{0^k 1^k : k \geq 0\}$.

Let $S =$ [TODO]. *S is an infinite set of strings.*

Because the DFA is finite, there are two (different) strings x, y in S such that x and y go to the same state. *We don't get to choose x, y*

Consider the string $z =$ [TODO] *We do get to choose z depending on x, y*

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Full outline

1. Suppose for the sake of contradiction that L is regular. Then there is some DFA M that recognizes L .
2. Let S be [fill in with an infinite set of prefixes].
3. Because the DFA is finite and S is infinite, there are two (different) strings x, y in S such that x and y go to the same state when read by M [you don't get to control x, y other than having them not equal and in S]
4. Consider the string z [argue exactly one of xz, yz will be in L]
5. Since x, y both end up in the same state, and we appended the same z , both xz and yz end up in the same state of M . Since $xz \in L$ and $yz \notin L$, M does not recognize L . But that's a contradiction!
6. So L must be an irregular language.

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Let's Try another

The set of strings with balanced parentheses is not regular.

What do you want S to be? What would you have to count?

The number of unclosed parentheses.

Let $S = \dots$

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One more, just the key steps

What about $\{a^k b^k c^k : k \geq 0\}$?

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