

## How do we accomplish those steps?

That fact? You can prove it in the extra credit problem on HW5. It's a nice combination of lots of things we've done with modular arithmetic.

Let's talk about finding  $C = a^e \% n$ .

$e$  is a BIG number (about  $2^{16}$  is a common choice)

```
int total = 1;
for(int i = 0; i < e; i++){
    total = (a * total) % n;
}
```

## One More Example for Reference

Find  $3^{25} \% 7$  using the fast exponentiation algorithm.

$$3^1 \% 7 = 3$$

$$3^2 \% 7 = 2$$

$$3^4 \% 7 = 4$$

$$3^8 \% 7 = 2$$

$$3^{16} \% 7 = 4$$

$$\begin{aligned} 3^{25} \% 7 &= 3^{16+8+1} \% 7 \\ &= [(3^{16} \% 7) \cdot (3^8 \% 7) \cdot (3^1 \% 7)] \% 7 \\ &= [4 \cdot 2 \cdot 3] \% 7 \\ &= (1 \cdot 3) \% 7 = 3 \end{aligned}$$