

## Proof By Cases

Let  $A = \{x : \text{Prime}(x)\}$ ,  $B = \{x : \text{Odd}(x) \vee \text{PowerOfTwo}(x)\}$

Where  $\text{PowerOfTwo}(x) := \exists c(\text{Integer}(c) \wedge x = 2^c)$

Prove  $A \subseteq B$

We need two different arguments – one for 2 and one for all the other primes...

## Divides

### Divides

For integers  $x, y$  we say  $x|y$  ("x divides y") iff there is an integer  $z$  such that  $xz = y$ .

Which of these are true?

$$2|4$$

$$4|2$$

$$2|-2$$

$$5|0$$

$$0|5$$

$$1|5$$

Claim: for all  $a, b, c, n \in \mathbb{Z}, n \geq 0$ :  $a \equiv b \pmod{n} \rightarrow a + c \equiv b + c \pmod{n}$

Before we start, we must know:

1. What every word in the statement means.
2. What the statement as a whole means.
3. Where to start.
4. What your target is.

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### Equivalence in modular arithmetic

Let  $a \in \mathbb{Z}, b \in \mathbb{Z}, n \in \mathbb{Z}$  and  $n > 0$ .  
We say  $a \equiv b \pmod{n}$  if and only if  $n|(b - a)$

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## You Try!

Claim: for all  $a, b, c, n \in \mathbb{Z}, n > 0$ : If  $a \equiv b \pmod{n}$  then  $ac \equiv bc \pmod{n}$

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