

# Boolean Algebra Reference Sheet

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## Axioms

### Closure

$$a + b \text{ is in } \mathbb{B}$$
$$a \bullet b \text{ is in } \mathbb{B}$$

### Commutativity

$$a + b = b + a$$
$$a \bullet b = b \bullet a$$

### Associativity

$$a + (b + c) = (a + b) + c$$
$$a \bullet (b \bullet c) = (a \bullet b) \bullet c$$

### Identity

$$a + 0 = a$$
$$a \bullet 1 = a$$

### Distributivity

$$a + (b \bullet c) = (a + b) \bullet (a + c)$$
$$a \bullet (b + c) = (a \bullet b) + (a \bullet c)$$

### Complementarity

$$a + a' = 1$$
$$a \bullet a' = 0$$

## Theorems

### Null

$$X + 1 = 1$$
$$X \bullet 0 = 0$$

### Idempotency

$$X + X = X$$
$$X \bullet X = X$$

### Involution

$$(X')' = X$$

### Uniting

$$X \bullet Y + X \bullet Y' = X$$
$$(X + Y) \bullet (X + Y') = X$$

### Absorption

$$X + X \bullet Y = X$$
$$(X + Y') \bullet Y = X \bullet Y$$
$$X \bullet (X + Y) = X$$
$$(X \bullet Y') + Y = X + Y$$

### DeMorgan

$$(X + Y + \dots)' = X' \bullet Y' \bullet \dots$$
$$(X \bullet Y \bullet \dots)' = X' + Y' + \dots$$

### Consensus

$$(X \bullet Y) + (Y \bullet Z) + (X' \bullet Z) = X \bullet Y + X' \bullet Z$$
$$(X + Y) \bullet (Y + Z) \bullet (X' + Z) = (X + Y) \bullet (X' + Z)$$

### Factoring

$$(X + Y) \bullet (X' + Z) = X \bullet Z + X' \bullet Y$$
$$X \bullet Y + X' \bullet Z = (X + Z) \bullet (X' + Y)$$