

Axioms

Closure
$a + b$ is in \mathbb{B} $a \bullet b$ is in \mathbb{B}

Commutativity
$a + b = b + a$ $a \bullet b = b \bullet a$

Associativity
$a + (b + c) = (a + b) + c$ $a \bullet (b \bullet c) = (a \bullet b) \bullet c$

Identity
$a + 0 = a$ $a \bullet 1 = a$

Distributivity
$a + (b \bullet c) = (a + b) \bullet (a + c)$ $a \bullet (b + c) = (a \bullet b) + (a \bullet c)$

Complementarity
$a + a' = 1$ $a \bullet a' = 0$

Theorems

Null
$X + 1 = 1$ $X \bullet 0 = 0$

Idempotency
$X + X = X$ $X \bullet X = X$

Involution
$(X')' = X$

Uniting
$X \bullet Y + X \bullet Y' = X$ $(X + Y) \bullet (X + Y') = X$

Absorbtion
$X + X \bullet Y = X$ $(X + Y') \bullet Y = X \bullet Y$ $X \bullet (X + Y) = X$ $(X \bullet Y') + Y = X + Y$

DeMorgan
$(X + Y + \dots)' = X' \bullet Y' \bullet \dots$ $(X \bullet Y \bullet \dots)' = X' + Y' + \dots$

Consensus
$(X \bullet Y) + (Y \bullet Z) + (X' \bullet Z) = X \bullet Y + X' \bullet Z$ $(X + Y) \bullet (Y + Z) \bullet (X' + Z) = (X + Y) \bullet (X' + Z)$

Factoring
$(X + Y) \bullet (X' + Z) = X \bullet Z + X' \bullet Y$ $X \bullet Y + X' \bullet Z = (X + Z) \bullet (X' + Y)$